

MET 350 HW 3.3

13.30

$$CO_2 : \frac{P_{CO_2}}{P_t} = \frac{20}{100} = .2$$

$$O_2 : \frac{P_{O_2}}{P_t} = \frac{30}{100} = .3$$

$$N_2 : \frac{P_{N_2}}{P_t} = \frac{50}{100} = .5$$

$$P_{total} = P_{O_2} + P_{CO_2} + P_{N_2} = 100 \text{ kPa}$$

$$m_{CO_2} = NM = (20 \text{ kmol})(44 \text{ kg/kmol}) = 880 \text{ kg}$$

$$m_{O_2} = (30 \text{ kmol})(32 \text{ kg/kmol}) = 960 \text{ kg}$$

$$m_{N_2} = (50 \text{ kmol})(28 \text{ kg/kmol}) = 1400 \text{ kg}$$

$$\text{total mass} = 1400 + 960 + 880 = 3240 \text{ kg}$$

Mass fractions

$$m_{CO_2} = \frac{m_{CO_2}}{m} = \frac{880}{3240} = .2716$$

$$CO_2 = \frac{880}{3240} = .2716$$

$$N_2 = \frac{1400}{3240} = .4321$$

$$M_m = \frac{3240}{100} = 32.4 \text{ kg/kmol}$$

Constant volume $\rightarrow C_v = m_{CO_2} C_{v,CO_2} + (for O_2) + (for N_2)$

$$C_v = (.2716 \times .657) + (.2963 \times .658) + (.4321 \times .743)$$

$$C_v = .69 \text{ kJ/kgK}$$

Gas Constant $= R = \frac{R_u}{M_m} = .256 \text{ kJ/kgK}$

$$C_p = C_v + R = .951 \text{ kJ/kgK}$$

$$k = \frac{C_p}{C_v} = 1.376$$

13-39

15% CH₄
85% Air

$$y_{\text{air}} = 1 - y_{\text{CH}_4} = .85$$

$$m_m = .15 (M_{\text{CH}_4}) + .85 (M_{\text{air}})$$

$$m_m = .15 (16) + .85 (28.97)$$

$$m_m = 27.02 \text{ g/mol}$$

$$V = \frac{n v_d}{2} = \frac{(3000)(.005)}{2 \text{ rev/s}} = 7.5 \text{ m}^3/\text{min}$$

$$v = \frac{R u_T}{M_m P} = \frac{(8.314)(293)}{27.02 \times 10^3} = 1.127 \text{ m}^3/\text{kg}$$

$$m = \frac{V}{v} = 7.5 / 1.127 = \boxed{6.65 \text{ kg/min}}$$

13-54

molar mass	specific h
NE = 20.18	.6179
AR = 39.95	.3122

$$\text{Mole Number} : N_{\text{NE}} = \frac{P V_i}{R T_i} = \frac{(100 \text{ kPa})(.45)}{(8.314)(293)} = .0185 \text{ kmol}$$

$$N_{\text{AR}} = \frac{(20)(.45)}{(8.314)(293)} = .0355 \text{ kmol}$$

$$N_t = .0520 \text{ kmol}$$

A)

$$E_m - E_{\text{out}} = \Delta E_{\text{system}} \rightarrow -Q_{\text{out}} = \Delta U = \Delta U_{\text{NE}} + \Delta U_{\text{AR}}$$

$$-Q_{\text{out}} = (m c_v (T_m - T_i))_{\text{NE}} + (m c_v (T_m - T_i))_{\text{AR}}$$

$$T_m = \boxed{16.2^\circ \text{C}}$$

$$B) P_m = \frac{N_m R_u T_m}{V_m} = \frac{(.052)(8.314)(289.2)}{.9 \text{ m}^3} = \boxed{138.9 \text{ kPa}}$$

13.59

	<u>Molar Mass</u>	<u>mole Number</u>	
CH ₄	16.0	$60/16 = 3.75 \text{ kmol}$	$N_{M\text{total}} = 4.57 \text{ kmol}$ $M_m = 100/4.57 = 21.85 \text{ kg/kmol}$
C ₃ H ₈	44.0	$23/44 = .5682 \text{ kmol}$	
C ₄ H ₁₀	58.0	$15/58 = .2586 \text{ kmol}$	

$$R = \frac{R_u}{M_m} = 8.314/21.85 = .3805 \text{ kg/kmol}$$

$$w_m = RT \ln \left(\frac{P_u}{P_i} \right) = \boxed{287 \text{ kJ/kg}} \quad (\text{computed via desmos})$$

$$E_m = E_{out} \quad \text{therefore } w_m = q_{out} \quad q_{out} = 287$$

$$\text{therefore } \boxed{w_m = 287 \text{ kJ/kg}}$$