

Homework #12

1. Shared session key establishment using a Key Distribution Center (KDC). Using the following table, illustrate how Alice can initiate a secure session with Bob with the help of KDC.

Alice	KDC	Bob
Kek: $k_a = A6 = 1010\ 0110$	$K_a = A6 = 1010\ 0110$ $K_b = D8 = 1101\ 1000$	$K_b = D8 = 1101\ 1000$
	Alice sends a message to KDC requesting between Alice and Bob	
	$K_{ses} = 7B = 0111\ 1011$	
	$y_a \rightarrow e_{K_a}(k_{ses}) = 1010\ 0110(0111\ 1011)$ $LC = 1010 \text{ xor } 0111 = 0001$ $RC = 0110 \text{ xor } 0111 = 0001$ $y_a = 00010001 = 11 \text{ (hexa)}$	
	$y_b \rightarrow e_{K_b}(k_{ses}) = 1101\ 1000(0111\ 1011)$ $LC = 1101 \text{ xor } 0111 = 0110$ $RC = 1000 \text{ xor } 0111 = 1111$ $y_b = 01101111\ 6F \text{ (hexa)}$	
KDC send $y_a = 11$ to alic		
	KDC send $y_b = 6F$ to bob	
Decrupt K_a $LB = 0001 \text{ xor } 0111 = 1010$ $RB = 0001 \text{ xor } 0111 = 0110$ $k_A = 10100110\ A6 \text{ (hexa)}$		K_b $LB = LC \text{ xor } RK$ $LB = 0110 \text{ xor } 0111 = 1101$ $RB = RC \text{ xor } LK$ $RB = 1111 \text{ xor } 0111 = 1000$ $k_B = 1101\ 1000 = D8$
$m = 45 \rightarrow 0100\ 0101$		
$y = e_{k_{ses}}(m)$ $LC = LB \text{ xor } RK$ $LC = 0100 \text{ xor } 0111 = 1111$ $RC = 0101 \text{ xor } 0111 = 0010$ $y = 11110010\ F2 \text{ (hexa)}$		
Alice send $y = F2$ to bob		
		$m = C = LC \parallel RC$

		$F2 = 1111\ 0010$ $LB = 1111 \text{ xor } 0010 = 0100$ $RB = 0010 \text{ xor } 0111 = 0101$ $m = 0100\ 0101$ is 45
		Verify, yes $m=45$

2. Man-in-the-middle attack when Alice and Bob employ Diffie-Hellman key exchange

Alice	Carol	Bob
	$P = 17$ and $a = 4$	
Choose $a = 7$		$b=8$
Alice's public key: $k_{pub,A} = A = a^a \text{ mod } p = 4^7 \text{ mod } 17 = 13$	Send A to Bob intercepted by carol	Bob's public key: $k_{pub,B} = B = a^b \text{ mod } p = 4^8 \text{ mod } 17 = 1$
	Send B Alice	
	Carol chooses $c = 6$ $a^c \text{ mod } p = 4^6 \text{ mod } 17 = 16$	
		Carol sends A to Bob as if it is A from Alice
Carol send B' to alic as if is from bob		
Alice derives the shared secret key as $K1 = B'^a \text{ mod } p$ $K1 = 16^7 \text{ mod } 17 = 16$	Carol derives $K1 = A^c \text{ mod } p,$ $K1 = 13^6 \text{ mod } 17 = 16$ $K2 = B^c \text{ mod } p$ $K2 = 1^6 \text{ mod } 17 = 1$	Bob derives the shared secret key as $K2 = A'^b \text{ mod } p = 16^8 \text{ mod } 17 = 1$
	Verify that alic and carol have derived the same key $K1$, yes they have the same key $K1 = 16$	
		Verify that carol and bob have derived the same key $K2 = 1$ yes they have the same key