

$$1) \mathbb{Z}_{13} = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$$

$$\mathbb{Z}_{13}^* = \{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12\}$$

$$2) \mathbb{Z}_{18} = \{0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17\}$$

$$\mathbb{Z}_{18}^* = \{1, 5, 7, 11, 13, 17\}$$

$$3) 5^1 = 5$$

$$5^2 = 25 \equiv \text{mod } 13 = 12$$

$$5^3 = 125 \text{ mod } 13 = 8$$

$$5^4 = 625 \text{ mod } 13 = 1$$

$$\text{order}(5) = 2_{13} = \boxed{4}$$

$$4) 5 \in \mathbb{Z}_{13}$$

$$5x = 1 \text{ mod } 13$$

$x = 1$	$x = 2$	$x = 3$	$x = 4$
$5 * x$	$5 * 2$	$5 * 3$	$5 * 4$
$5 * 1$	$10 \neq 1$	$15 > 13$	$20 > 13$
$5 \neq 1$		$15 \text{ mod } 13$	$20 \text{ mod } 13$
		$2 \neq 1$	$7 \neq 1$

$$x = 5$$

$5 * 5$	$x = 6$	$x = 7$	$x = 8$
$25 > 13$	$15 * 6$	$5 * 7$	$5 * 8$
$25 \text{ mod } 13$	$30 \text{ mod } 13$	$35 \text{ mod } 13$	$40 \text{ mod } 13$
$12 \neq 1$	$4 \neq 1$	$9 \neq 1$	$31 = 1$

$$\boxed{x = 8}$$