

HW 3.1

Group 2: Sanchez, Perkins, Ashley, Wells, Watts

11.5 Oil is flowing at the rate of $0.015 \text{ m}^3/\text{s}$ in the system shown in Fig. P11.5. Data for the system are as follows:

- Oil specific weight = 8.80 kN/m^3
- Oil kinematic viscosity = $2.12 \times 10^{-5} \text{ m}^2/\text{s}$
- Length of DN 150 pipe = 180 m
- Length of DN 50 pipe = 80 m
- Elbows are long-radius type
- Pressure at B = 12.5 MPa

$$V_A = \frac{Q}{A} = \frac{0.015 \text{ m}^3/\text{s}}{\pi \times 0.15^2} = 0.212 \text{ m/s}$$

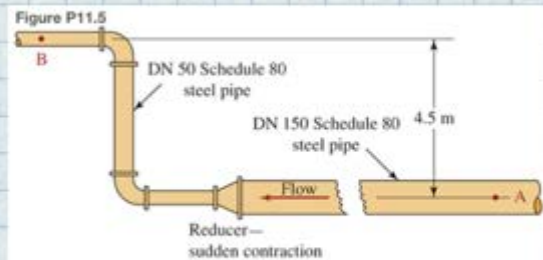
$$V_B = \frac{0.015}{\pi \times 0.05^2} = 1.91 \text{ m/s}$$

$$h_{fA} = 0.026 \left(\frac{180}{0.15} \right) \times \left(\frac{0.212^2}{2(9.81)} \right) = 0.0713$$

$$h_{fB} = 0.026 \left(\frac{80}{0.05} \right) \times \left(\frac{1.91^2}{2(9.81)} \right) = 0.774$$

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B + h_{fA-B}$$

$$P_A = \frac{12.5}{8.8 \times 10^3} + \frac{(0.212)^2}{2(9.81)} + \frac{(1.91)^2}{2(9.81)} + 4.5 + 0.0713 + 0.774 = 13.9 \text{ MPa}$$



11.13 A device designed to allow cleaning of walls and windows on the second floor of homes is similar to the system shown in Fig. P11.13. Determine the velocity of flow from the nozzle if the pressure at the bottom is (a) 20 psig and (b) 80 psig. The nozzle has a loss coefficient K of 0.15 based on the outlet velocity head. The tube is smooth drawn aluminum and has an ID of 0.50 in. The 90° bend has a radius of 6.0 in. The total length of straight tube is 20.0 ft. The fluid is water at 100°F .

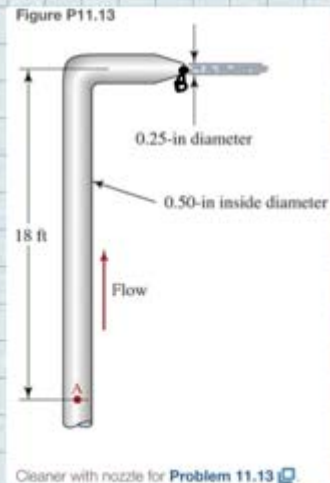
$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B + h_L$$

$$\text{where } h_L = K \frac{V_B^2}{2g} + f \left(\frac{L}{D} \right) \frac{V_A^2}{2g}$$

$$V_A \left(\frac{D_B^2}{4} \right) = V_B \left(\frac{D_A^2}{4} \right) \rightarrow V_A = \frac{D_B^2}{D_A^2} V_B$$

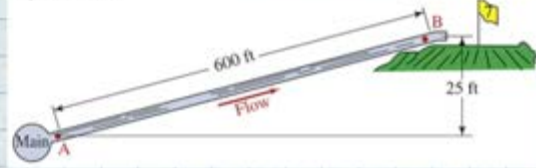
$$\text{where } V_B = \sqrt{\frac{2g(P_B/\gamma + z_B - z_A)}{1 + \frac{K D_A^4}{D_B^4} + f \frac{L D_A^5}{D_B^5}}} = 30.41 \text{ ft/s}$$

$$V_A = 74.42 \text{ ft/s}$$



11.20 Figure P11.20 shows a pipe delivering water to the putting green on a golf course. The pressure in the main is at 80 psig and it is necessary to maintain a minimum of 60 psig at point B to adequately supply a sprinkler system. Specify the required size of Schedule 40 steel pipe to supply 0.50 ft³ of water at 60 °F.

Figure P11.20



$$V = \frac{4Q}{\pi D^2}, \quad V^2 = \frac{16Q^2}{\pi^2 D^4}$$

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B + h_{L-A-B}$$

$$Re = \frac{\rho V D}{\mu} = \frac{V D}{\nu} \quad \text{where } V = \frac{4(0.5)/\pi}{0.321} = 6.173 \text{ ft/s}$$

$$\frac{\Delta P}{\gamma} - z_B = f \frac{8LQ^2}{g\pi^2} \frac{1}{D^5}$$

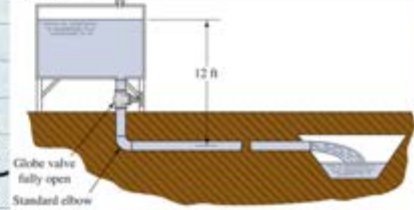
$$D = \sqrt[5]{\frac{f \frac{8LQ^2}{g\pi^2}}{\frac{P_A - P_B}{\gamma} - z_B}} \quad \text{where } f = \frac{25}{\left[\log\left(\frac{1}{3.7(D/\epsilon)} + \frac{5.74}{Re^{0.9}}\right)\right]^2} \quad \text{where } D/\epsilon = \frac{0.321 \text{ ft}}{0.00015 \text{ ft}} = 2140.8$$

$$D = \sqrt[5]{\frac{0.01913 \frac{8(600)(0.5)}{(32.2)(\pi^2)}}{\frac{(80-60)}{62.4} - 25}} \quad f = \frac{0.25}{\log\left(\frac{1}{3.7(D/\epsilon)} + \frac{5.74}{Re^{0.9}}\right)^2} \quad \text{where } Re = \frac{(6.173)(0.321)}{1.21 \times 10^{-5}}$$

$$\Downarrow \quad D = 0.321 \text{ ft} \quad \Downarrow \quad f = 0.0191$$

11.22 The tank shown in Fig. P11.22 is to be drained to a sewer. Determine the size of new Schedule 40 steel pipe that will carry at least 400 gal/min of water at through the system shown. The total length of pipe is 75 ft.

Figure P11.22



$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B + h_L$$

$$\frac{16Q^2}{\pi^2 D^4} \frac{1}{2g} + 0.5 \frac{16Q^2}{\pi^2 D^4} \frac{1}{2g} + 340 \text{ ft} \frac{16Q^2}{\pi^2 D^4} \frac{1}{2g} + f \frac{L}{D} \frac{16Q^2}{\pi^2 D^4} \frac{1}{2g} + 30 \text{ ft} \frac{16Q^2}{\pi^2 D^4} \frac{1}{2g}$$

$$\frac{16Q^2}{\pi^2 D^4} \frac{1}{2g} (1 + 0.5 + 340 \text{ ft} + f \frac{L}{D} + 30 \text{ ft}) = -12$$

LHS RHS

L	75 ft	Roughness	0.00015 ft	
D	0.039 ft			
Q	0.891204 ft ³ /s			
V	32.2 ft/s			
f	0.025			
Z	12 ft			
Kinematic V	0.0000121 ft ² /s			
LHS		RHS		
P1	P2	P3	P1	P2
106259.1763	0.015528	42.52966102		
	LHS	RHS	% diff	
	70173.397	12	-584679%	
	70173.397			
	70173.397			
	70173.397			
	70173.397			
	70173.397			
	70173.397			
	Re	Di	f	new f vs old f
	518123256.1	393.33333	0.0249892	0%

$$D = 0.039 \text{ ft}$$

11.23 Figure P11.23 depicts gasoline flowing from a storage tank into a truck for transport. The gasoline has a specific gravity of 0.68 and the temperature is 25°C. Determine the required depth h in the tank to produce a flow of 1500 L/min into the truck. Because the pipes are short, neglect the energy losses due to pipe friction, but do consider minor losses.

$$A = \frac{\pi}{4} d^4 = \frac{\pi}{4} (0.90)^2 = 6.581 \times 10^{-3} \text{ m}^2$$

$$V_0 = \frac{Q}{A} = \frac{1500}{6.581 \times 10^{-3}} = 3.92 \text{ m/s}$$

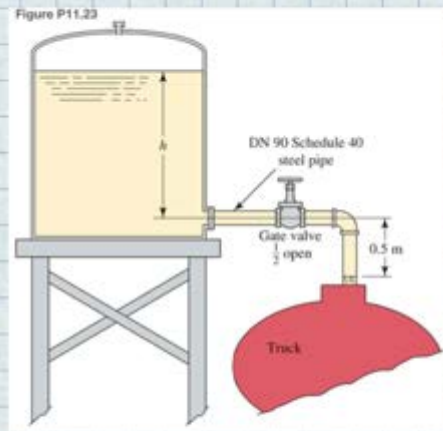
$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + h_L$$

$$h_L = 0.5 \frac{V^2}{2g} + 160 f_f \frac{V_0^2}{2g} + 30 f_r \frac{V^2}{2g}$$

$$\rightarrow h_L = 0.5 \frac{(3.92)^2}{9.8} + 160(0.018) \frac{(3.92)^2}{9.8} + 0.44 = 3.06 \text{ m}$$

$$3.06 + \frac{3.92^2}{9.8} = 3.84 = h + 0.5$$

$$\rightarrow h = 3.5 \text{ m}$$



Weekly Reflection

In the recent lessons, we focused on series pipeline systems, covering three main problem types: calculating energy losses, determining flow rates, and figuring out pipe diameters. We learned that to find the right flow rate and pipe diameter, iterations in Excel are necessary, highlighting the importance of trial and error in these calculations. Specifically, we looked at scenarios where either the flow rate or the pipe diameter was known, and we had to compute the other. Using Excel was particularly helpful for these exercises, as it allowed us to efficiently perform iterations and calculate percentage differences, making it a valuable tool for tackling the complexities of fluid mechanics problems.