

Name: **Frank Nguyen** UIN: **00980645**

MET 330 Fluid Mechanics
Dr. Orlando Ayala
Spring 2017
Test 2

Take home – Due Sunday March 19th 2017 before midnight.

READ FIRST

1. RELAX!!!! DO NOT OVERTHINK THE PROBLEMS!!!! There is nothing hidden. The test was designed for you to pass and get the maximum number of points, while learning at the same time. HINT: THINK BEFORE TRYING TO USE/FIND EQUATIONS (OR EVEN FIND SIMILAR PROBLEMS)
2. The total points on this test are one hundred (100). FOR THE “WORKFORCE” SYLLABUS STUDENTS: Ten (10) points are from your HW assignments, and ten (10) other points are based on the basis of technical writing. The other eighty (80) points will come from the problem solutions. FOR THE “OTHER” SYLLABUS STUDENTS: Ten (10) other points are based on the basis of technical writing. The other eighty (90) points will come from the problem solutions. For the technical writing I will follow the attached rubric.
3. There are 2 problems to solve, each worth (80/2) points for “Workforce” syllabus students and (90/2) for the “Other” syllabus students.
4. What you turn in should be only your own work. You cannot discuss the exam with anyone, except me. Call me, skype me, text me, email me, come to my office, if you have any question.
5. I do not read minds. You should be explicit and organized in your answers. Use drawings/figures. If you make a mistake, do not erase it. Rather use that opportunity to explain why you think it is a mistake and show the way to correct the problem.
6. You have to turn in your test ON TIME and ONLY through BLACKBOARD. You must submit only one file and it has to be a pdf file. For the ePortfolio you are also supposed to upload this artifact to your Google drive. When you are done solving the test, please go ahead and upload it now before you forget.
7. Do not start at the last minute so you can handle anything that could happen. Late tests will not be accepted. Test submitted through email will not be accepted either.
8. Cheating is completely wrong. The ODU Student Honor Pledge reads: "I pledge to support the honor system of Old Dominion University. I will refrain from any form of academic dishonesty or deception, such as cheating or plagiarism." By attending Old Dominion University you have accepted the responsibility to abide by this code. This is an institutional policy approved by the Board of Visitors. It is important to remind you the following part of the Honor Code:

IX. PROHIBITED CONDUCT

A. Academic Integrity violations, including:

1. *Cheating*: Using unauthorized assistance, materials, study aids, or other information in any academic exercise (Examples of cheating include, but are not limited to, the following: using unapproved resources or assistance to complete an assignment, paper, project, quiz or exam; collaborating in violation of a faculty member's instructions; and submitting the same, or substantially the same, paper to more than one course for academic credit without first obtaining the approval of faculty).

With that said, you are NOT authorized to use any online source of any type, unless is ODU related.

① Purpose

- Determine the size of the pipe (steel pipe schedule 40) before and after the pump for the new pump system that needs 30 gpm for each machine exactly instead of 20 gpm and 10 gpm.
- Determine the total head on the pump and the power delivered by the pump to the coolant with the new 30 gpm.
- Determine the pressure at the inlet of the pump.

Sources

- Mott, R. Unterr, J.A. "Applied Fluid Mechanics", 7th edition Pearson Education Inc (2015)
- Blackboard notes

Design Considerations

- Constant properties • Constant temp. • Pipe friction
- Incompressible fluid • Steady state

Data and Variables

$$Q = 60 \text{ gal/min} \approx 1.336 \text{ ft}^3/\text{s}$$

$$\gamma = .92$$

$$f_r = 1.85$$

$$n = 3.6 \times 10^{-5}$$

$$z = 1.5 \times 10^{-4}$$

$$K_{\text{gate valve}} = 85 \quad \left. \begin{array}{l} \\ \end{array} \right\} \text{table } 10.4$$

$$K_{\text{swing check valve}} = 100 f_t$$

$$K_{\text{entrance}} = .5 (f_r \log)$$

$$K_{\text{exit}} = 1 (f_r \log)$$

$$V = 3 \text{ m/s} \approx 9.84 \text{ ft/s}$$

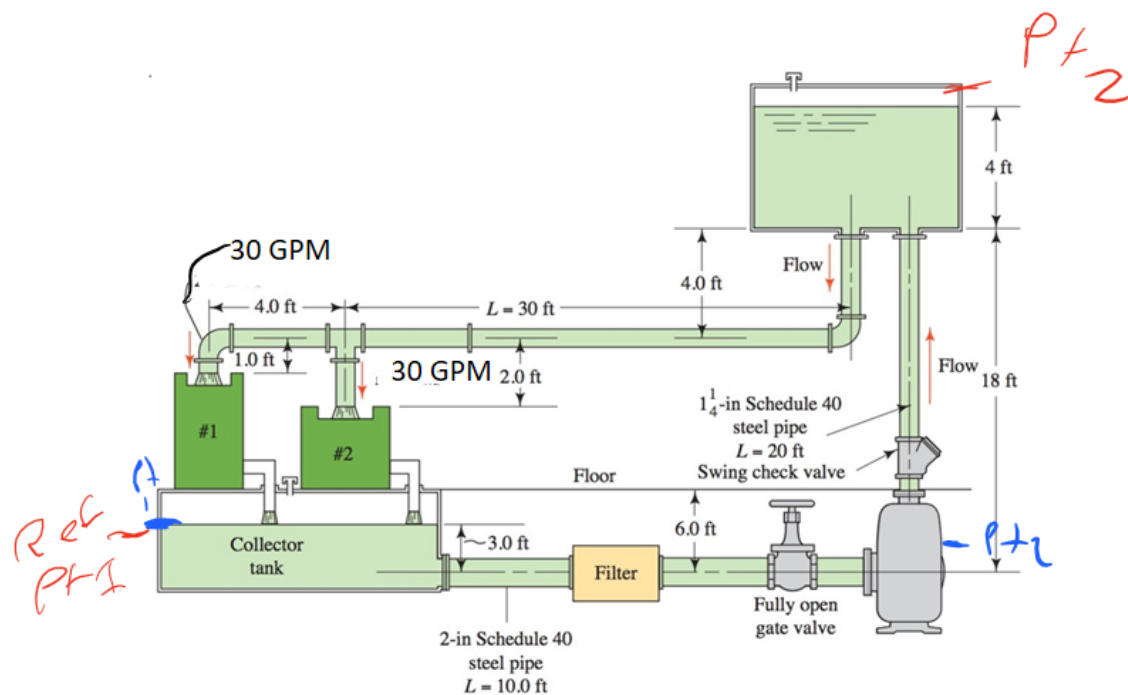
(we use for our class)

$$\frac{V^2}{2g} = 1.5 \text{ ft}$$

Materials

- Schedule 40 Steel • Valve
- Coolant
- Pump

Drawings and Diagrams



Red = Ref. points for
1 part a) and b)

Blue = Ref points for
1 part c

Procedure and Calculations

a) For this part I will apply Bernoulli's from the collector tank surface to the upper tank surface. That Bernoulli will lead to find pipe size (D) by iterating equations. Then use the class III equation to solve for D.

- Apply Bernoulli from 1 to 2, I get:

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2 + h_{L1-2} \quad P_1 - P_2 = 0$$

$$\frac{P_1 - P_2}{\gamma} = h_{L1-2}$$

now solve for head loss.

$$h_L = \underbrace{h_1}_{\text{entrance loss}} + \underbrace{h_2}_{\text{energy loss in pipe}} + \underbrace{h_3}_{\text{energy loss in elbow}} + \underbrace{h_4}_{\text{energy loss in fully open gate valve}} + \underbrace{h_5}_{\text{energy loss in swing check valve}} + \underbrace{h_6}_{\text{friction loss in section pipe}} + \underbrace{h_7}_{\text{exit loss}}$$

$$h_1 = K \left(\frac{V^2}{2g} \right) = (5)(1.50) = .75 \text{ ft}$$

$$h_2 = f \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = f \left(\frac{10}{D} \right) 1.50 \text{ ft} = f \left(\frac{10}{D} \right) 1.50$$

$$h_3 = f_r \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (1.85)(1.50 \text{ ft}) = 2.775 \text{ ft}$$

$$h_4 = f_{24} \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = f(8)(1.50 \text{ ft}) = f(8)(1.50) = 12 \text{ ft}$$

$$h_5 = f_{d4} \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = f(100)(1.50 \text{ ft}) = 150 \text{ ft}$$

$$h_6 = f \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = f \left(\frac{18}{D} \right) 1.50 \text{ ft} = f \left(\frac{18}{D} \right) 1.50$$

$$h_7 = 1 \left(\frac{V^2}{2g} \right) = 1(1.50 \text{ ft}) = 1.50 \text{ ft}$$

$$h_L = \underbrace{h_1}_{.75 \text{ ft}} + \underbrace{h_2}_{f \left(\frac{10}{D} \right) 1.50} + \underbrace{h_3}_{2.775 \text{ ft}} + \underbrace{h_4}_{12 \text{ ft}} + \underbrace{h_5}_{150 \text{ ft}} + \underbrace{h_6}_{f \left(\frac{18}{D} \right) 1.50} + \underbrace{h_7}_{1.50 \text{ ft}}$$

$$h_L = 5.025 + 162 \text{ ft} + \frac{28f}{D}$$

- Put D on the other side.

$$D = 5.025 + 162f + 28f$$

1) assume f

2) Calculate D

3) Calculate Re and $\frac{D}{\epsilon}$

4) Calculate f

5) If f from 4) equals f from 1, Calculate D . - then

assume f	D	Re	D/ϵ	f
.0261	9.84	4.4×10^4	62.6	.009 x
.015	7.975	3.76×10^4	42.5	.05 x
.052	15.665	7.53×10^6	100	.052 ✓

$$D = 5.025 + 162 \overset{f}{(.052)} + 28 \overset{f}{(.052)}$$

$$D = 14.905 \text{ ft}$$

$$h_L = 5.025 + 162(.052) + \frac{28(.052)}{14.905}$$

$$h_L = 13.55 \text{ ft}$$

$$\text{Class III} = D = .66 \left[\epsilon^{1.25} \left(\frac{LQ}{\phi h} \right)^{4.75} + VQ^{9.4} \left(\frac{L}{\phi h} \right)^{5.2} \right]^{.04}$$

$$D = .66 \left[(1.5 \times 10^{-9})^{1.25} \left(\frac{(30 \text{ ft})(.1336 \text{ ft}^3/\text{s})}{(32.2 \text{ ft/s})(13.55 \text{ ft})} \right)^{4.75} + (9.84 \text{ ft/s})^{9.4} \left(\frac{.1336 \text{ ft}^3/\text{s}}{(32.2 \text{ ft/s})(13.55 \text{ ft})} \right)^{5.2} \right]^{.04}$$

$$D = .66 [2.47 \times 10^{-19} + 5.38 \times 10^{-14}]^{.04}$$

$$D = .66(.295)$$

$$D = .1947 \text{ ft (inside)}$$

- Next largest pipe size has an inside $D = .2058 \text{ ft}$.

Pipe used is $\left(2 \frac{1}{2} \text{ Schedule 40 steel pipe} \right)$

b) use bernoulli's again to find total head on pump.

$$\frac{p_1}{\rho} + z_1 + \frac{v_1^2}{2g} - h_L + h_p = \frac{p_2}{\rho} + z_2 + \frac{v_2^2}{2g} \quad p_1 = p_2 = 0$$

$$h_A = h_L + (z_2 - z_1)$$

$$z_2 - z_1 = 19 \text{ ft}$$

- h_L similar to part a) but now we have 2 1/2 in schedule 40 pipe to count for before and after the pump.

2 1/2" schedule 40:

$$D = .2058 \text{ ft} \quad A = .03326 \text{ ft}^2 \quad (\text{from table F.1})$$

$$V = \frac{1336 \text{ ft}^3/\text{s}}{.03326 \text{ ft}^2} = V = 4.02 \text{ ft/s}, \quad \frac{V^2}{2g} = .251 \text{ ft}$$

- use N_R and D/ϵ to find f .

$$N_R = \frac{VD\rho}{\mu} = \frac{(4.02 \text{ ft/s})(.2058 \text{ ft})(.92)(1.49 \text{ slug/ft}^3)}{3.6 \times 10^{-5}} = 4.09 \times 10^4$$

$$\frac{D}{\epsilon} = \frac{.2058 \text{ ft}}{1.5 \times 10^{-4}} = 1372$$

$$D/\epsilon = 1372$$

$$f = .024 \quad (\text{from moody's diagram})$$

- h_L same as part a) and use same ref. points.

$$h_1 = K \left(\frac{V^2}{2g} \right) = .5 (.251 \text{ ft}) = .1255 \text{ ft}$$

$$h_2 = f \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (.024) \left(\frac{10 \text{ ft}}{.2058 \text{ ft}} \right) (.251 \text{ ft}) = .293 \text{ ft}$$

$$h_3 = f_r \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (1.85) (.251 \text{ ft}) = .464 \text{ ft}$$

$$h_4 = f_{\text{el}} \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (.019)(6)(.251) = .038 \text{ ft}$$

$$h_5 = f_{\text{el}} \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (.022)(100)(.251) = .552 \text{ ft}$$

$$h_6 = f \left(\frac{L}{D} \right) \left(\frac{V^2}{2g} \right) = (.024) \left(\frac{18 \text{ ft}}{.2058 \text{ ft}} \right) (.251) = .527 \text{ ft}$$

$$h_7 = 1 \left(\frac{V^2}{2g} \right) = .251 \text{ ft}$$

$$h_L = \overset{h_1}{.1255} + \overset{h_2}{.293} + \overset{h_3}{.464} + \overset{h_4}{.038} + \overset{h_5}{.552} + \overset{h_6}{.527} + \overset{h_7}{.251}$$

$$h_L = 2.25 \text{ ft}$$

- Total head =

$$h_a = h_c + (z_2 - z_1) \\ = 2.25 + 19 \text{ ft}$$

$$h_a = 21.25 \text{ ft}$$

- Power of pump to maintain.

$$P = h_a \gamma Q$$

$$P = (21.25 \text{ ft}) \left(-92 \frac{62.4 \text{ lb}}{\text{ft}^3} \right) \left(\frac{-1.336 \text{ ft}^3}{\text{s}} \right) \frac{1 \text{ hp}}{550 \text{ ft} \cdot \text{lb}} \cdot \frac{1}{\text{s}}$$

$$P = .296 \text{ hp}$$

c) again we manipulate Bernoulli's to find pressure at inlet pump.

- Reference points: point 1 at collector tank surface point 2 at pump inlet

$$\frac{P_1}{\gamma} + z_1 + \frac{V_1^2}{2g} - h_L = \frac{P_2}{\gamma} + z_2 + \frac{V_2^2}{2g}$$

$$P_2 = \gamma(z_1 - z_2) - h_L - \frac{V_2^2}{2g}$$

- h_L for this part is just $h_1 - h_4$ because of Ref. Points.

- h_L from previous part a and b

$$h_1 = 12.55 \text{ ft}$$

$$h_2 = .295 \text{ ft}$$

friction

$$h_3 = .464 \text{ ft}$$

$$h_4 = .038 \text{ ft}$$

open
pipe
valve

$$h_L = .1255 + .295 + .464 + .038$$

$$h_L = .9205 \text{ ft}$$

$$P_2 = .92 \left(\frac{62.4 \text{ lb}}{\text{ft}^3} \right) [3 \text{ ft} - .9205 \text{ ft} - .251 \text{ ft}] \left(\frac{4 \text{ ft}^2}{144 \text{ in}^2} \right)$$

$$P_2 = .729 \text{ psig}$$

Summary:

- d) The new pipe size $2\frac{1}{2}$ " Schedule 40 before and after the pump is larger than the original one which was 2" before the pump and $1\frac{1}{4}$ " after the pump.
- b) The total head on the pump is 21.25 ft and the power delivered by the pump to the coolant is .296 hp. After we put the new $2\frac{1}{2}$ " Schedule 40 pipe on the
- c) The pressure at inlet of the pump is now .729 psig after the new $2\frac{1}{2}$ " Schedule 40 pipe.

Analysis

- Since our flow is now larger the piping has to be larger as well to keep up with flow.
- Not that much energy loss in pipes.
- Changing flow rate to 30 gpm in each machine affects our system.

② Purpose:

- 1) Determine the size of the pipe (Steel pipe schedule 40), for the gravity driven system to deliver a flow rate of 30 gpm in each machine

Sources:

- Moti, R. Untenur, J.A "Applied Fluid Mechanics". 7th edition, Pearson Education, Inc (2015)

- Blackboard notes

Design Consideration

- Constant properties
- Constant temp
- Incompressible fluid

- Steady state

- Pipe friction

Materials

- Schedule 40 steel pipe
- Coolant
- pipe

Data and Variables

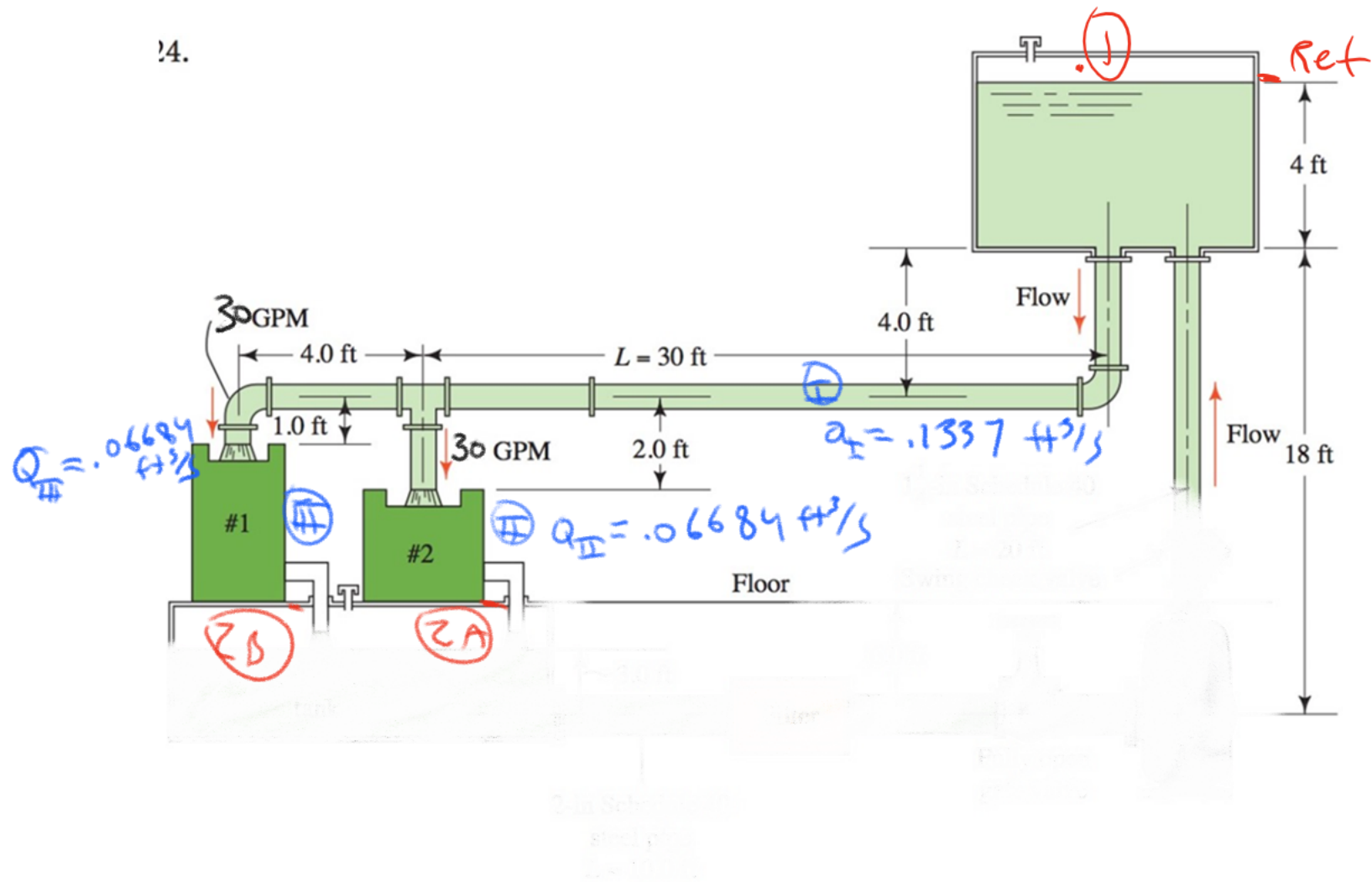
$$Q_I = 60 \text{ gpm} = .1337 \text{ ft}^3/\text{s}$$

$$Q_{II} = 30 \text{ gpm} = .06684 \text{ ft}^3/\text{s}$$

$$Q_{III} = 30 \text{ gpm} = .06684 \text{ ft}^3/\text{s}$$

$$m = 3.6 \times 10^{-5}$$

14.



Procedure and Calculations

- manipulate bernoulli equation between point 1 and 2A

$$\frac{P_1}{\rho} + Z_1 + \frac{V_1^2}{2g} = h_L + \frac{P_2}{\rho} + Z_2 + \frac{V_2^2}{2g}$$

$$Z_1 = \frac{V_{2A}^2}{2g} + Z_{2A} + h_{L1-2A}$$

$$Z_1 - Z_{2A} = \frac{V_{2A}^2}{2g} + h_{L1-2A}$$

- h_{L1-2A} : energy loss

$$h_{L1-2A} = h_{ent} + h_{elbow} + h_{tee} + h_{L1} + h_{LII}$$

- Let's calculate energy losses h_m

$$h_m = K \frac{V^2}{2g} \Rightarrow h_m = \frac{8K}{g\pi^2 D^5} Q^2$$

- Pipe energy losses $= h_L = f \frac{L}{D} \frac{V^2}{2g}$

$$h_L = \frac{8fL}{g\pi^2 D^5} Q^2$$

$$\frac{V^2}{2g} = \frac{8}{g\pi^2 D^4} Q^2$$

- Plug in Substitutions.

$$Z_1 - Z_{2A} = \frac{8}{g\pi^2 D_{II}^4} Q_{II}^2 + \frac{8K_{ent}}{g\pi^2 D_I^4} Q_I^2 + \frac{8K_{elbow}}{g\pi^2 D_I^4} Q_I^2 + \frac{8K_{tee}}{g\pi^2 D_I^4} Q_I^2 + \frac{8f_1 L_1}{\pi^2 g D_I^5} Q_I^2 + \frac{8f_2 L_2}{g\pi^2 D_{II}^5} Q_{II}^2$$

- Plug in numbers

$$10 \text{ ft} = \frac{8}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_{II}^4} (0.0664 \text{ ft}^3/s)^2 + \frac{8(1.5)}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_I^4} (1.337 \text{ ft}^3/s)^2 + \frac{8 \cdot 30 \text{ ft}}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_I^4} (1.337 \text{ ft}^3/s)^2$$

$$+ \frac{8 \cdot 60 \text{ ft}}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_I^4} (1.337 \text{ ft}^3/s)^2 + \frac{8f_2(34 \text{ ft})}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_I^4} (1.337 \text{ ft}^3/s)^2 + \frac{8f_1(2 \text{ ft})}{\left(\frac{32.2 \text{ ft}}{s^2}\right) \pi^2 D_{II}^5} (0.0664 \text{ ft}^3/s)^2$$

$$10 = \frac{1.125 \times 10^{-4}}{D_{II}^4} + \frac{2.249 \times 10^{-4}}{D_I^4} + \frac{1.349 \times 10^{-2} (f_{II})}{D_I^4} + \frac{2.699 \times 10^{-2} (f_{II})}{D_I^4} + \frac{1.529 \times 10^{-2} (f_I)}{D_I^5} + \frac{2.249 \times 10^{-4} (f_{II})}{D_{II}^5}$$

$$A: 1 \times 10^5 = (2.249 + 1.349 f_{II} + 2.699 f_{II}) \frac{1}{D_I^4} + \frac{1.529 f_I}{D_I^5} + \frac{1.125}{D_{II}^4} + \frac{2.249 f_{II}}{D_{II}^5}$$

- Manipulate Bernoulli's equation between points 1 and 2

$$z_1 = \frac{V_1^2}{2g} + z_{2b} + h_{ent} + h_{elb} + h_{f_{12}} + h_{f_{23}} + h_{clw_{23}} + h_{f_{23}}$$

$$\frac{V_1^2}{2g} = \frac{8}{9\pi^2 D_1^5} Q_{III}^2 = \frac{8}{32.2\pi^2 D_1^5} \left(\frac{0.6684 \text{ ft}^3}{s} \right)^2 = \frac{1.125 \times 10^{-4}}{D_1^5}$$

$$\frac{8.999 \times 10^{-3} \text{ ft}^3}{D_1^5}$$

$$h_{clw_{23}} = \frac{8 K_{clw}}{9\pi^2 D_1^5} Q_{III}^2 = \frac{8(30 f_{III})}{32.2\pi^2 D_1^5} \left(\frac{0.6684 \text{ ft}^3}{s} \right)^2 = \frac{3.374 \times 10^{-3} f_{III}}{D_1^5}$$

$$h_{f_{23}} = \frac{8 f_{III} L_{23}}{9\pi^2 D_1^5} Q_{III}^2 = \frac{8 f_{III} \cdot 1}{32.2\pi^2 D_1^5} \left(\frac{0.6684 \text{ ft}^3}{s} \right)^2 = \frac{1.125 \times 10^{-4} f_{III}}{D_1^5}$$

$$B: 9 \times 10^4 = (2.249 + 134.1 f_{12} + 899.9 f_{12}) \frac{1}{D_1^5} + \frac{152.9 f_{12}}{D_1^5} + (425 + 33.74 f_{12}) \frac{1}{D_1^5} + \frac{1.125 f_{12}}{D_1^5}$$

- Let's use $V_{max} = 3 \text{ m/s}$ (9.843 ft/s) because it's the V we use for this (10)

$$V_1 = \frac{4 Q_F}{\pi D_1^2} = \frac{4(1337 \text{ ft}^3/s)}{\pi D_1^2}$$

$$V_1 = .170 \frac{1}{D_1^2} \rightarrow D_1 = \sqrt{\frac{1.170 \text{ ft}^3/s}{9.843 \text{ ft/s}}}$$

$$D_1 = .131 \text{ ft} \text{ or } 1.57 \text{ in}$$

- From table F.1, it should use $1\frac{1}{2}$ inch nominal size

$$D_1 = 1\frac{1}{2} \text{ in nominal size Schedule 40}$$

$$D_{2i} = .1342 \text{ ft} \quad A_i = .01414 \text{ ft}^2$$

- Now solve for D_{II} .

$$A: 1 \times 10^5 = (2.249 + 134.9 f_{12} + 269.9 f_{12}) \frac{1}{D_1^5} + \frac{152.9 f_{12}}{D_1^5} + \frac{1.125}{D_{II}^5}$$

$$\frac{\epsilon}{D_1} = \frac{1.5 \times 10^{-4} \text{ ft}}{.1342 \text{ ft}} \text{ (for steel)}$$

$$\frac{\epsilon}{D_1} = 1.117 \times 10^{-3} \quad \text{or} \quad \frac{D_1}{\epsilon} = 894.67 \text{ ft}$$

$$f_{12} = .021$$

- Now find f_z

$$Re = \frac{V_z D_z}{\nu} = \frac{.170}{\nu} \cdot \frac{D_z}{D} = \frac{.170}{D \cdot \nu} = \frac{.170}{(.0394)(6.27 \times 10^{-7})} = 2.02 \times 10^6$$

- from Moody's $f_z = .022$

- Now plug in numbers

$$1 \times 10^5 = [2.249 + 134.7(.021) + 269.7(.022)] \frac{1}{.13924} + \frac{152.9(.022)}{.13425} + \frac{1175}{D_{II}^2} + \frac{2.249 f_{II}}{D_{II}^5}$$

$$1 \times 10^5 = (11.0197 + 3093.1 + 77280.1 + \dots)$$

$$1 \times 10^5 = 3093 + 77280.1 + \dots$$

$$19626.9 = \frac{1125 f_{II}}{D_{II}^4} + \frac{2.249 f_{II}}{D_{II}^5}$$

- To solve equation we have to use trial and error. First guess is $.041$ ft

$$\frac{D_{II}}{\epsilon} = \frac{.041}{1.5 \times 10^{-4}} = 273.3$$

$$Re = \frac{V_z D_{II}}{\nu} = \frac{40 \pi}{\pi D_{II}^2} \cdot \frac{D_{II}}{D} = \frac{40 \pi}{\pi D_{II}} = \frac{4(.06684)}{\pi(.041)(6.27 \times 10^{-7})}$$

$$Re = 3.31 \times 10^6$$

from Moody's $f_{II} = .0277$

$$D_{II} : 19626.9 = \frac{1}{D_{II}^4} \left(1.125 + \frac{2.249 f_{II}}{D_{II}} \right)$$

$$D_{II} = \sqrt[4]{5.732 \times 10^{-4} \frac{1.146 \times 10^{-4} f_{II}}{D_{II}}}$$

- Now trial and error until $D_{II} = D_{II}$

$D_{a, nom}$	$D_{a/2}$	R_c	f_{II}	$D_{II} = \sqrt[4]{5.732 \times 10^{-9} \frac{1.146 \times 10^{-4} f_{II}}{CDR \cdot C_{II}}}$	
.1723	1148.6	788159.288	.02	.156 ft	X
.161	1113.3	813172.6	.02	.1556 ft	X
<u>.159</u>	1060	854087	.02	.1551 ft	✓

$D_{II} = .159$ ft, now we go to table F and pick a diameter

$D_{II} = 2$ in nominal size Schedule 40 steel

$D_{II} = .1723$ ft $A_i = .02333$ ft²

- Plug in numbers and find D_{III} :

$$D_{III} =$$

$$9 \times 10^4 = \left[2.249 + 134.9(.021) + 699(.01) \right] \frac{1}{.1342^4} + \frac{152.9(.022)}{.1342^5} + (1.125 + 33.74 f_{III}) \frac{1.125}{D_{III}^4} + \frac{1.125 f_{III}}{D_{III}^5}$$

$$9 \times 10^4 = 773932.5 + 77280.1 + (1.125 + 33.74 f_{III}) \frac{1}{D_{III}^4} + \frac{1.125 f_{III}}{D_{III}^5}$$

OR,

$$761212.6 = (1.125 + 33.74 f_{III}) \frac{1}{D_{III}^4} + \frac{1.125 f_{III}}{D_{III}^5}$$

$$761212.6 = \frac{1}{D_{III}^4} \left[1.125 + 33.74 f_{III} + \frac{1.125 f_{III}}{D_{III}} \right]$$

$$D_{III} = \sqrt[4]{1.478 \times 10^{-6} + 4.432 \times 10^{-5} f_{III} + \frac{1.478 \times 10^{-6} f_{III}}{D_{III}}}$$

- Now trial and error just like before.

$D_{III} \text{ mm}$	$D_{III}/2$	R_c	F_{III}	f_{III}	$D_{III} \leq 1.476 \times 10^{-5} + 4.477 \times 10^{-5}$	
.159	106	854087	.02	.02	.04625	X
.04625	308.3	213017.6	.0256	.0256	.04304	X
.04304	286.9	315520	.0257	.0257	.04325	✓

$$D_{III} = .04304 \text{ ft}$$

- Look up in table F.

$$D_{III} = \frac{1}{2} \text{ in normal size, Schedule 40 Steel}$$

$$D_{III} = .0518 \text{ ft}$$

$$A_i = .00211 \text{ ft}^2$$

- Summary

- Schedule 40 Steel

$D_I = 1\frac{1}{2} \text{ in}$	$D_I = .1342 \text{ ft}$ $A_I = .0144 \text{ ft}^2$
$D_{II} = 2 \text{ in}$	$D_{II} = .1723 \text{ ft}$ $A_{II} = .0233 \text{ ft}^2$
$D_{III} = \frac{1}{2} \text{ in}$	$D_{III} = .0518 \text{ ft}$ $A_{III} = .00211 \text{ ft}^2$

- Values are from table F.1

Analysis

To double check we want a flow rate of 30 gpm or .06684 ft³/s in machine 1 and 2. Let's plug in the values of pipe sizes and check.

$$V = \frac{Q}{A} \Rightarrow Q = V \cdot A$$

$$Q_{II} = Q_{III} = .06684 \text{ ft}^3/\text{s}$$

- for the #1 machine.

$$V = \frac{.06684 \text{ ft}^3/\text{s}}{.00211 \text{ ft}^2} \quad (a)$$

$$V = 31.67 \text{ ft/s}$$

$$Q_{III} = (31.67 \text{ ft/s})(.00211 \text{ ft}^2)$$

$$Q_{III} = .06684 \text{ ft}^3/\text{s} \quad \checkmark$$

- for the #2 machine

$$V = \frac{.06684 \text{ ft}^3/\text{s}}{.02333 \text{ ft}^2}$$

$$V = 2.864 \text{ ft/s}$$

$$Q_{II} = (2.864 \text{ ft/s})(.02333 \text{ ft}^2)$$

$$Q_{II} = .06684 \text{ ft}^3/\text{s} \quad \checkmark$$

- This means the pipe size for the system needs to be 2 in for machine #2 and $\frac{1}{2}$ inch for machine #1. To get a 30 gpm flow rate, we do not want to always increase pipe diameter because of energy losses.