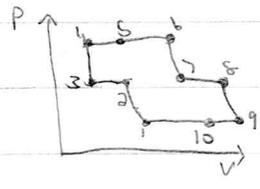
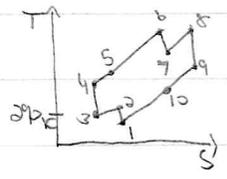


HW 1.5

123



$$T_2 = T_1 = T_1 r_p^{(\gamma-1)/\gamma} = (290)(4)^{0.4/1.4} = 430.9 \text{ K}$$

$$T_5 = T_4 + 20 = 430.9 + 20 = 450.9 \text{ K}$$

$$q_{in} = C_p(T_6 - T_5) \Rightarrow T_6 = T_5 + \frac{q_{in}}{C_p} = 450.9 + \frac{300}{1.005} = 749.4 \text{ K}$$

$$T_7 = T_6 \left(\frac{1}{r_p}\right)^{\frac{\gamma-1}{\gamma}} = 749.4 \left(\frac{1}{4}\right)^{0.4/1.4} = 504.3 \text{ K}$$

$$T_8 = T_7 + \frac{q_{in}}{C_p} = 504.3 + \frac{300}{1.005} = 802.8 \text{ K}$$

$$T_9 = T_8 \left(\frac{1}{r_p}\right)^{\frac{\gamma-1}{\gamma}} = (802.8) \left(\frac{1}{4}\right)^{0.4/1.4} = 540.2 \text{ K}$$

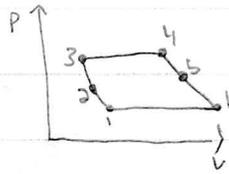
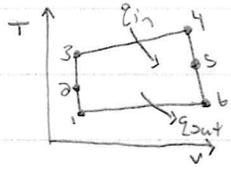
$$T_{10} = T_9 - 20 = 540.2 - 20 = 520.2 \text{ K}$$

$$q_{in} = 300 + 300 = 600 \text{ kJ/kg}$$

$$\begin{aligned} q_{out} &= C_p(T_{10} - T_1) + C_p(T_3 - T_2) \\ &= 1.005(520.2 - 290) + 1.005(430.9 - 290) \\ &= 373 \text{ kJ/kg} \end{aligned}$$

$$\eta_{th} = 1 - \frac{q_{out}}{q_{in}} = 1 - \frac{373}{600} = 0.378 \times 100 = \boxed{37.8\%}$$

129



$c_p = 0.24 \text{ Btu/lbm} \cdot \text{R}$        $k = 1.4$

a)  $T_2 = T_1 \frac{v_2^{\gamma} - v_1^{\gamma}}{\gamma c_p}$   
 $= 470 + \frac{(900)^2}{2(0.24)} \cdot \frac{1 \text{ Btu/lbm}}{25037 \text{ ft}^2/\text{s}^2}$

$T_2 = 537.4 \text{ R}$

$P_2 = P_1 \left( \frac{T_2}{T_1} \right)^{\frac{k}{k-1}}$   
 $= (7) \left( \frac{537.3}{470} \right)^{1.4/0.4}$

$P_2 = 11.19 \text{ psia}$

$P_3 = P_4 \Rightarrow (P_1)(P_2)$

$P_3 = 13(11.19)$

$P_3 = 145.5 \text{ psia}$

$T_3 = T_2 \left( r_p \right)^{\frac{k-1}{k}}$   
 $= 537.4 (13)^{0.4/1.4}$

$T_3 = 1118.3 \text{ R}$

$T_5 = T_4 - T_3 + T_2$   
 $= (2400 - 1118.3 + 537.4)$

$T_5 = 1819.1 \text{ R}$

$P_5 = P_4 \left( \frac{T_5}{T_4} \right)^{\frac{k}{k-1}}$   
 $= 145.5 \left( \frac{1819.1}{2400} \right)^{1.4/0.4}$

$P_5 = 52.2 \text{ psia}$

b)  $T_6 = T_5 \left( \frac{P_6}{P_5} \right)^{\frac{k-1}{k}}$   
 $= (1819.1) \left( \frac{7}{55.2} \right)^{0.4/1.4}$

$T_6 = 1008.4 \text{ R}$

$V_6 = \sqrt{2 c_p (T_5 - T_6)}$   
 $= \sqrt{2(0.24) (1819.1 - 1008.6) \left( \frac{25037 \text{ ft}^2/\text{s}^2}{1 \text{ Btu/lbm}} \right)}$

$V_6 = 3121 \text{ ft/s}$

c)  $w_p = (V_{exit} - V_{inlet}) V_{aircraft}$   
 $= (3121 - 900)(900) \left( \frac{1 \text{ Btu/lbm}}{25037 \text{ ft}^2/\text{s}^2} \right)$

$w_p = 79.8 \text{ Btu/lbm}$

$q_{in} = h_4 - h_3 = c_p (T_4 - T_3)$   
 $= (0.24) (2400 - 1118.3)$

$q_{in} = 307.6 \text{ Btu/lbm}$

$\eta_p = \frac{79.8}{307.6 + 100}$   
 $= 0.259$

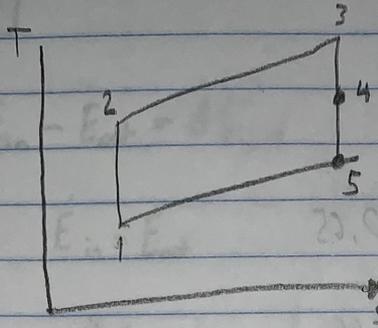
$\eta_p = 25.9\%$

MES50

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HW # 1.5

4-135)



$$T_1 = 300 \text{ K}$$

$$h_1 = 300.19 \text{ kJ/kg}$$

$$P_{r1} = 1.386$$

$$P_{r2} = \frac{P_2}{P_1} P_{r1} = (12)(1.386)$$

$$P_{r2} = 16.63$$

$$h_2 \Rightarrow 610.65 \text{ kJ/kg}$$

$$\dot{Q}_{in} = \dot{m}_c (h_2 - h_1)$$

$$= (0.2 \text{ kg/s})(41,700 \text{ kJ/kg})$$

$$= 8540 \text{ kJ/s}$$

$$q_{in} = \frac{\dot{Q}_{in}}{\dot{m}}$$

$$= \frac{8540 \text{ kJ/s}}{10 \text{ kg/s}} = 854 \text{ kJ/kg}$$

MET350  
Page 2 of 3

HW#15  
4-135 cont.

$$q_{in} = h_3 - h_2$$

$$854 = h_3 - 610.65$$

$$h_3 = 1464.65 \text{ kJ/kg}$$

$$\Rightarrow P_{r3} = 396.27$$

$$W_{comp,in} = W_{t,out}$$

$$\Rightarrow h_2 h_1 = h_3 - h_4$$

$$\Rightarrow h_4 = h_3 - h_2 + h_1$$

$$= 1464.65 - 610.65 + 300.19$$

$$h_4 = 741.17 \text{ kJ/kg}$$

$$P_{r5} = P_{r3} \left( \frac{P_5}{P_3} \right)$$

$$= (396.27) \left( \frac{1}{12} \right)$$

$$= 33.02$$

$$\Rightarrow h_5 = 741.79 \text{ kJ/kg}$$

MET350  
Page 3 of 3

HW 1.5  
4-135 cont.

$$\dot{E}_{in} - \dot{E}_{out} = \Delta E_{syst}$$

$$\dot{E}_{in} = \dot{E}_{out}$$

$$\Rightarrow h_4 + V_4^2/2 = h_5 + V_5^2/2$$

$$V_5 = \sqrt{2(h_4 - h_5)}$$

$$= \sqrt{(2)(1154.19 - 741) \left( \frac{1000 \text{ J}}{1 \text{ kJ/kg}} \right)}$$

$$= 908.9 \text{ m/s}$$

$$\text{Thrust} = \dot{m}(V_{exit} - V_{inlet}) = (10 \text{ kg/s})(908.9) \left( \frac{1 \text{ N}}{1 \text{ kg} \cdot \text{m/s}^2} \right)$$

$$= 9089 \text{ N}$$