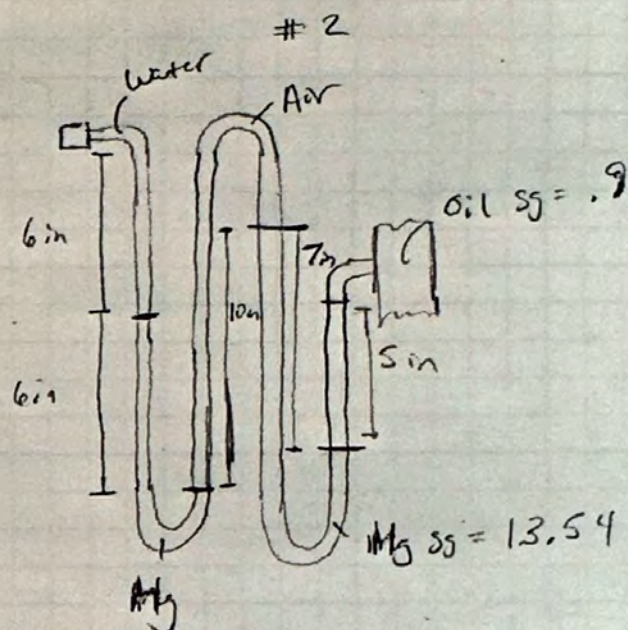
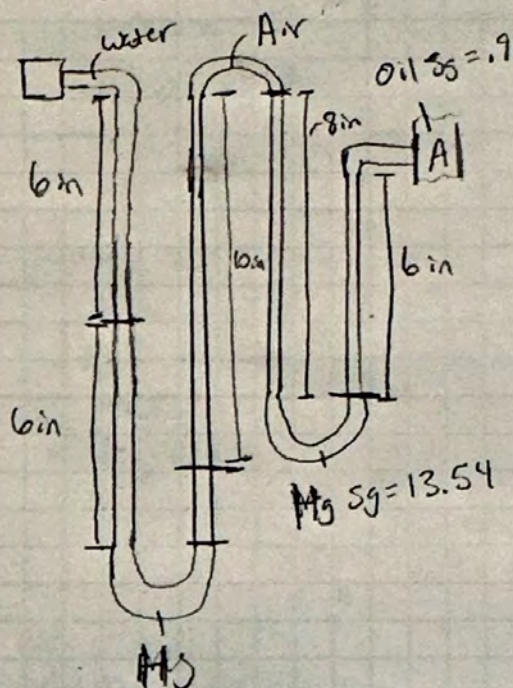


1. Purpose Determine press diff $P_A - P_B$ @ 6 in
+ @ 5 in height of oil

Diagram: #1



Assumptions

1. incompressible fluids
2. steady state
3. Isothermal @ 70°F
4. water/mercury don't mix

Data & variables

$$\gamma_{\text{water}} = 62.3 \text{ lb/ft}^3$$

$$\gamma_{\text{oil}} = 62.3 \cdot 0.9 = 56.07 \text{ lb/ft}^3$$

$$\gamma_{\text{Hg}} = 62.3 \cdot 13.54 = 843.54 \text{ lb/ft}^3 \quad \gamma_{\text{air}} = 0$$

Materials

Water, oil, mercury, Air

Procedure for @ 6in

Use increment of height equation $\Delta p = \gamma \cdot h$

to find pressure @ $P_B \rightarrow P_A$

Moving down is positive, up is negative.

Calculations

$$6\text{in} \cdot \frac{1\text{ft}}{12\text{in}} = .5\text{ft} \quad 10\text{in} \cdot \frac{1\text{ft}}{12\text{in}} = .833\text{ft} \quad 8\text{in} \cdot \frac{1\text{ft}}{12\text{in}} = .666\text{ft}$$

Start @ point A

$$P_A + \gamma_{oil} \cdot .5\text{ft} - \gamma_{Hg} \cdot .666\text{ft} + \gamma_{air} \cdot .833\text{ft} - \gamma_{Hg} \cdot .5\text{ft} - \gamma_w \cdot .5\text{ft} = P_B$$

$$P_A - P_B = -56.07 \frac{\text{lb}}{\text{ft}^3} \cdot .5\text{ft} + 884.54 \frac{\text{lb}}{\text{ft}^3} \cdot .666\text{ft} + 884.51 \frac{\text{lb}}{\text{ft}^3} \cdot .5\text{ft} + 64.3 \frac{\text{lb}}{\text{ft}^3} \cdot .5\text{ft}$$

$$P_A - P_B = \boxed{987.68 \text{ lb/ft}^2}$$

Summary

the differential pressure between $P_A \rightarrow P_B$ is 987.68 lb/ft^2

Analysis: The pressure of a certain point only depends on height of the fluid column & the specific weight of the fluid.

Procedure for @ 5in

Point A reduces to 5in $\rightarrow$ causes Hg to raise up 1in, Changing the total distance from 8in to 7in.

The Air pocket expands to compensate for the changes & doesn't affect the other measurements

Calculations

$$5 \text{ in} \cdot \frac{1 \text{ ft}}{12 \text{ in}} = .416 \text{ ft}$$

$$7 \text{ in} \cdot \frac{1 \text{ ft}}{12 \text{ in}} = .583 \text{ ft}$$

$$P_A + \gamma_{\text{oil}} \cdot .416 \text{ ft} - \gamma_{\text{Hg}} \cdot .583 \text{ ft} + \gamma_{\text{air}} \cdot .0036 \text{ ft} - \gamma_{\text{Hg}} \cdot .5 \text{ ft} - \gamma_{\text{w}} \cdot .5 \text{ ft} = P_B$$

$$P_A - P_B = -56.07 \frac{\text{lb}}{\text{ft}^3} \cdot .416 \text{ ft} + 884.54 \frac{\text{lb}}{\text{ft}^3} \cdot .583 \text{ ft} + 884.5 \frac{\text{lb}}{\text{ft}^3} \cdot .5 \text{ ft} + 64.3 \frac{\text{lb}}{\text{ft}^3} \cdot .5 \text{ ft}$$

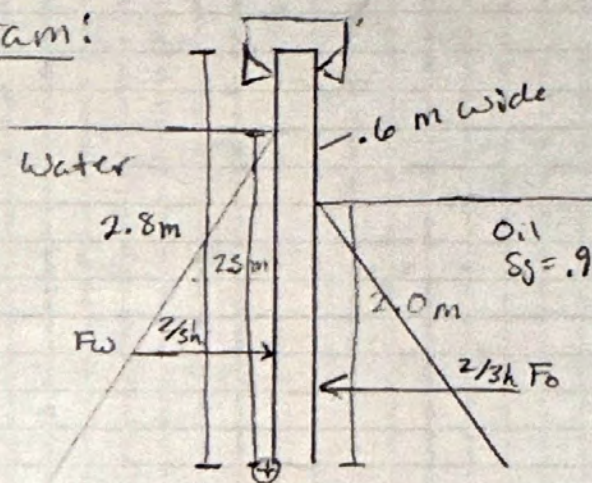
$$P_A - P_B = 972.12 \frac{\text{lb}}{\text{ft}^2}$$

Summary: Pressure diff between P_A & P_B is $972.12 \frac{\text{lb}}{\text{ft}^2}$

Problem # 2

Purpose: find net forces on the gate, hinge + support

Diagram:



Assumptions

1. incompressible fluid
2. Iso thermal process + constant properties

Data/Variables

$$\gamma_w = 9.81 \text{ KN/m}^3$$

$$h_{\text{gate}} = 2.8 \text{ m} \quad h_{\text{water}} = 2.5 \text{ m} \quad h_{\text{oil}} = 2.0 \text{ m}$$

$$W_{\text{gate}} = .6 \text{ m}$$

Materials

Water + Oil

Procedure

Compute force on both sides of door,

$$\text{With } F = \gamma h_c \cdot A$$

Center of pressure can be found at $\frac{2}{3}$ height from the surface of liquid

With forces + pressure centers, summation of moment can be used to find forces @ Support + hinge

Calculations:

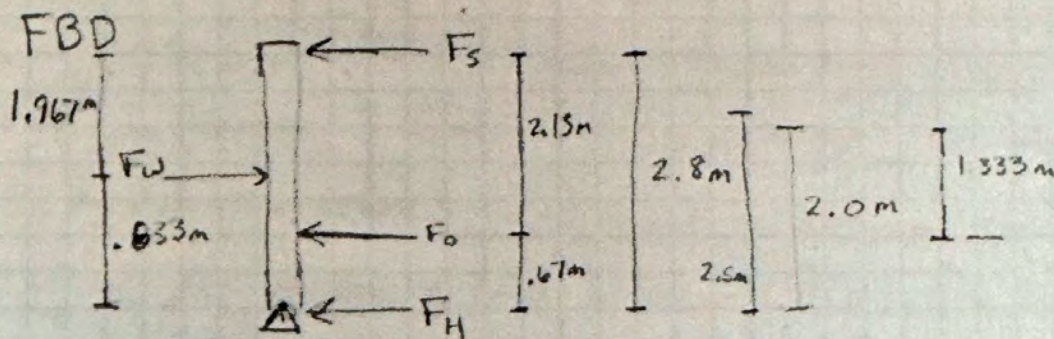
$$F_{\text{water}} = 9.81 \frac{\text{KN}}{\text{m}^3} \cdot \frac{2.5\text{m}}{2} \cdot (2.5\text{m} \cdot 6\text{m}) = 18.39 \text{ KN} \rightarrow$$

$$LP_1 = 2.5\text{m} \cdot \frac{2}{3} = 1.667\text{m}$$

$$F_{\text{oil}} = (9.81 \frac{\text{KN}}{\text{m}^3} \cdot 9) \frac{2\text{m}}{2} (2\text{m} \cdot 6\text{m}) = 10.59 \text{ KN} \leftarrow$$

$$LP_2 = 2\text{m} \cdot \frac{2}{3} = 1.333\text{m}$$

$$\text{Gate Net Force} = 18.39 \text{ KN} - 10.59 \text{ KN} = \boxed{7.79 \text{ KN} \rightarrow}$$



$$\sum M_H: 10.59 \text{ KN} \cdot 0.67\text{m} - 18.39 \text{ KN} \cdot 0.833\text{m} + F_s \cdot 2.8\text{m} = 0$$

$$\boxed{F_s = \frac{8.22 \text{ KN} \cdot \text{m}}{2.8\text{m}} = 2.94 \text{ KN} \leftarrow}$$

$$\sum M_s: 18.39 \text{ KN} \cdot 1.967\text{m} - 10.59 \text{ KN} \cdot 2.13\text{m} - F_H \cdot 2.8\text{m} = 0$$

$$\boxed{F_H = \frac{13.61 \text{ KN} \cdot \text{m}}{2.8\text{m}} = 4.863 \text{ KN} \leftarrow}$$

Summary: Net force on gate is $7.79 \text{ KN} \rightarrow$

Net force on support is $2.94 \text{ KN} \leftarrow$

Net force on hinge is $4.863 \text{ KN} \leftarrow$

All of these forces are in equilibrium since the gate is stationary + balance out due to their differing locations.

Excel spreadsheet

→
Positive forces are left to right
Negative forces are right to left
←

$$F_w = \gamma_w \cdot h_c \cdot (\text{water height} \cdot .6)$$

$\frac{1}{2}$
water height

$$F_{oil} = \gamma_w \cdot S_{oil} \cdot \frac{\text{oil height}}{2} \cdot (\text{oil height} \cdot .6)$$

$$\text{Gate Net Force} = F_{water} - F_{oil}$$

$$COP_{water} = \text{Water height} \cdot \frac{2}{3}$$

$$COP_{oil} = \text{oil height} \cdot \frac{2}{3}$$

$$COP_{water, \text{ from top}} = COP_{water} + (\text{Gate height} - \text{Water height})$$

$$COP_{oil, \text{ from top}} = COP_{oil} + (\text{Gate height} - \text{oil height})$$

$$COP_{water, \text{ from bottom}} = \text{Gate height} - COP_{water, \text{ from top}}$$

$$COP_{oil, \text{ from bottom}} = \text{Gate height} - COP_{oil, \text{ from top}}$$

$$\text{Force on Support} = \frac{(F_{oil} \cdot COP_{oil, \text{ from bottom}}) - (F_{water} \cdot COP_{water, \text{ from bottom}})}{- \text{gate height}}$$

$$\text{Force on hinge} = \frac{(F_{water} \cdot COP_{water, \text{ top}}) - (F_{oil} \cdot COP_{oil, \text{ top}})}{\text{gate height}}$$

Analysis

As oil height increases hinge force moves towards zero & eventually the other direction. This is due to the oil eventually putting more force at the base as its height is greater than water's

Problem # 3

Excel spreadsheet

$$CoG = Length/2$$

$$Volume, cylinder = \frac{\pi}{4} d^2 \cdot l$$

$$Weight, cylinder = Vol_{cylinder} \cdot \gamma_{cylinder}$$

$$Fluid Volume = \frac{\pi}{4} \cdot d^2 \cdot \text{floating position}$$

$$W_f = V_f \cdot \gamma_f$$

$$\text{Floating position} = \frac{W_c}{\frac{\pi}{4} \cdot d^2 \cdot \gamma_f}$$

$$\text{Center of Buoyancy} = \frac{\text{Floating position}}{2}$$

$$Volume displaced = \frac{\pi}{4} d^2 \cdot \text{Floating position}$$

$$\text{Moment of inertia} = \frac{\pi \cdot d^4}{64}$$

$$MB = \frac{\text{Moment of Inertia}}{\text{Volume displaced}}$$

$$\text{Meta center} = \text{Center of buoyancy} + MB$$

$$\text{Comparison} = \text{If meta center} > CoG = \text{Stable}$$

$$\text{metacenter} < CoG = \text{unstable}$$

Analysis: As diameter increases, stability increases
if all other variables stay the same