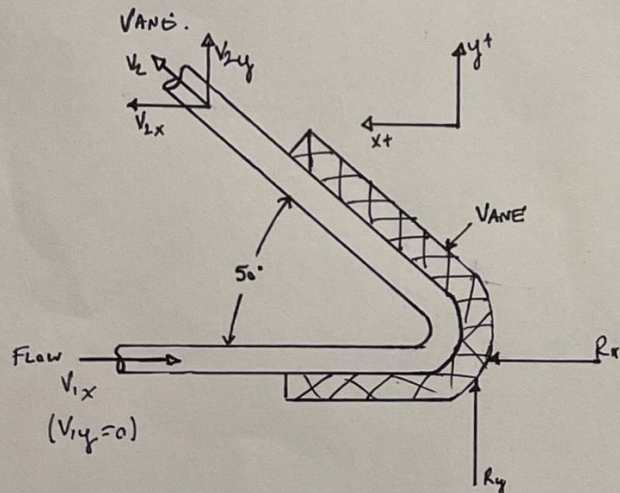


16.6) THE FIGURE SHOWS A FREE STREAM OF WATER AT 180°F BEING DEFLECTED BY A STATIONARY VANE THROUGH A 130° ANGLE. THE ENTERING STREAM HAS A VELOCITY OF $22 \frac{\text{ft}}{\text{s}}$. THE CROSS-SECTIONAL AREA OF THE STREAM IS CONSTANT AT 2.95 in^2 THROUGHOUT THE SYSTEM. COMPUTE THE FORCES IN THE HORIZONTAL AND VERTICAL DIRECTIONS EXERTED ON THE WATER BY THE VANE.



GIVEN: $V_{1x} = 22 \frac{\text{ft}}{\text{s}}$

$$A_s = 2.95 \text{ in}^2 \cdot \frac{1 \text{ ft}^2}{144 \text{ in}^2} = 0.020486 \text{ ft}^2$$

* STATIONARY VANE *

$$\rho_w = 1.88 \frac{\text{slugs}}{\text{ft}^3}$$

$$\theta = 130^\circ, \quad 180^\circ - 130^\circ = 50^\circ$$

SOLUTION:

$$Q = A_s \cdot V_1 = (0.020486 \text{ ft}^2) \left(22 \frac{\text{ft}}{\text{s}} \right)$$

$$Q = 0.450692 \frac{\text{ft}^3}{\text{s}}$$

$$V_{2x} = V_1 \cos(50^\circ) = \left(22 \frac{\text{ft}}{\text{s}} \right) \cos(50^\circ) = 14.1413 \frac{\text{ft}}{\text{s}}$$

$$V_{2y} = V_1 \sin(50^\circ) = \left(22 \frac{\text{ft}}{\text{s}} \right) \sin(50^\circ) = 16.853 \frac{\text{ft}}{\text{s}}$$

$$\sum R_x = \rho_w \cdot Q \cdot (V_{2x} - V_{1x}) = 0$$

$$= \left(1.88 \frac{\text{slugs}}{\text{ft}^3} \right) \left(0.450692 \frac{\text{ft}^3}{\text{s}} \right) \left(14.1413 \frac{\text{ft}}{\text{s}} - 22 \frac{\text{ft}}{\text{s}} \right) = 0$$

$$= -6.659 \text{ lb}$$

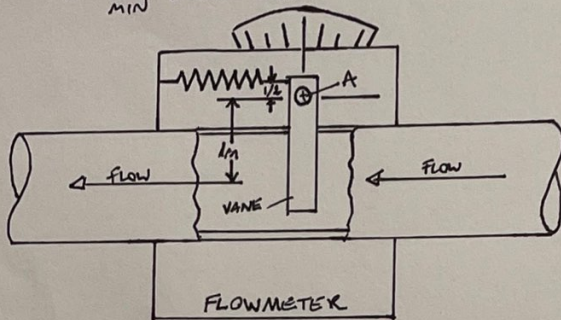
$$R_x = 6.659 \text{ lb} \leftarrow +$$

$$\sum R_y = \rho_w \cdot Q \cdot (V_{2y} - V_{1y}) = 0$$

$$= \left(1.88 \frac{\text{slugs}}{\text{ft}^3} \right) \left(0.450692 \frac{\text{ft}^3}{\text{s}} \right) \left(16.853 \frac{\text{ft}}{\text{s}} - 0 \frac{\text{ft}}{\text{s}} \right)$$

$$R_y = 14.2796 \text{ lb} \uparrow +$$

16.11) THE FIGURE REPRESENTS A TYPE OF FLOWMETER IN WHICH THE FLAT VANE IS ROTATED ON A PIVOT AS IT DEFLECTS THE FLUID STREAM. THE FLUID FORCE IS COUNTERBALANCED BY A SPRING. CALCULATE SPRING FORCE REQUIRED TO HOLD THE VANE IN A VERTICAL POSITION WHEN WATER AT 100 $\frac{\text{GAL}}{\text{MIN}}$ FLOWS FROM THE 1 in SCH. 40 PIPE TO WHICH THE METER IS ATTACHED.



$$\text{GIVEN: } Q = 100 \frac{\text{GAL}}{\text{MIN}} \cdot \frac{1 \text{ ft}^3/\text{s}}{449 \frac{\text{GAL}}{\text{MIN}}} = 0.222717 \frac{\text{ft}^3}{\text{s}}$$

$$1 \text{ in SCH. 40} \rightarrow A = 0.006 \text{ ft}^2 \\ D = 0.0874 \text{ ft}$$

$$P_w = 1.94 \frac{\text{SLUGS}}{\text{ft}^3} \cdot \frac{32.174 \text{ lb}}{1 \text{ SLUG}} = 62.4 \frac{\text{lb}}{\text{ft}^3}$$

$$\text{SOLUTION: } V = \frac{Q}{A} = \frac{0.222717 \frac{\text{ft}^3}{\text{s}}}{0.006 \text{ ft}^2} = 37.1195 \frac{\text{ft}}{\text{s}}$$

$$F_w = P_w \cdot Q \cdot V = \left(1.94 \frac{\text{SLUGS}}{\text{ft}^3} \right) \left(0.222717 \frac{\text{ft}^3}{\text{s}} \right) \left(37.1195 \frac{\text{ft}}{\text{s}} \right)$$

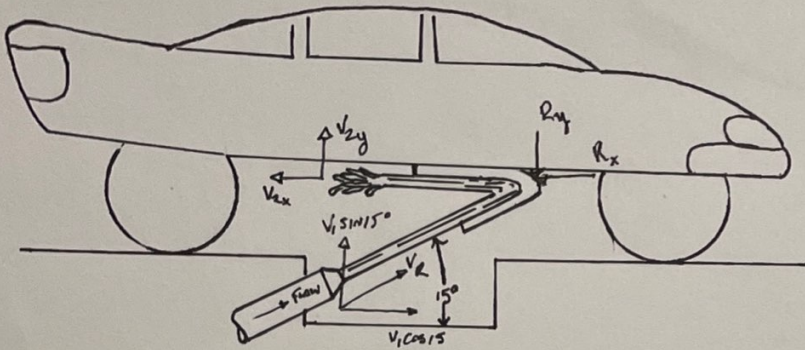
$$F_w = 515.87 \text{ lb}$$

$$\Sigma M_A = F_w(1 \text{ in}) - F_s(0.5 \text{ in}) = 0$$

$$F_s = \frac{F_w(1 \text{ in})}{0.5 \text{ in}} = \frac{515.87 \text{ lb}(1 \text{ in})}{0.5 \text{ in}}$$

$$F_s = 1031.74 \text{ lb}$$

- 16.20) A vehicle is to be propelled by a jet of water impinging on a vane as shown. The jet has a velocity of $30 \frac{m}{s}$ and issues from a nozzle with a diameter of 200 mm. Calculate the force of the vehicle (a) if it is stationary and (b) if moving at $12 \frac{m}{s}$.



Given: $\rho_w = 1000 \frac{kg}{m^3}$

$V_1 = 30 \frac{m}{s}$

$D = 200 \text{ mm} = 0.2 \text{ m}$

$V_c = 12 \frac{m}{s}$

Solution: $A = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.2 \text{ m})^2 = 0.031416 \text{ m}^2$

$Q = A \cdot V_1 = (0.031416 \text{ m}^2) (30 \frac{m}{s}) = 0.94248 \frac{m^3}{s}$

$V_2 = V_1$

(a) $(F_x) \sum R_x = \rho_w \cdot Q (V_2 + V_1 \cos 15^\circ) \quad -(-) \rightarrow +$

$= (1000 \frac{kg}{m^3}) (0.94248 \frac{m^3}{s}) (30 \frac{m}{s} + 30 \frac{m}{s} \cos 15^\circ) \quad \frac{kg \cdot m}{s^2} = N *$
 $= 55585.4 \text{ N}$

$(F_y) \sum R_y = \rho_w \cdot Q (V_2 + V_1 \sin 15^\circ)$

$= (1000 \frac{kg}{m^3}) (0.94248 \frac{m^3}{s}) (0 \frac{m}{s} + 30 \frac{m}{s} \sin 15^\circ)$
 $= 7317.95 \text{ N}$

(b) Solve for new velocities, $V_{x1} = V_1 \cos 15^\circ - V_c = 30 \frac{m}{s} \cos 15^\circ - 12 \frac{m}{s}$
 $V_{x1} = 16.978 \frac{m}{s}$

$M = \rho \cdot A \cdot V_R$
 $= (1000 \frac{kg}{m^3}) (0.031416 \text{ m}^2) (18.669 \frac{m}{s})$
 $= 586.505 \frac{kg}{s}$

$\theta = \tan^{-1} (\frac{7.765}{16.978}) = 24.577^\circ$
 $\beta = \theta - 15^\circ = 24.577^\circ - 15^\circ$
 $= 9.577^\circ$

$V_{y1} = V_1 \sin 15^\circ - 0 = 30 \sin 15^\circ = 7.765 \frac{m}{s}$
 $V_{y1} = 7.765 \frac{m}{s}$

$V_R = \sqrt{(V_{x1})^2 + (V_{y1})^2}$
 $= \sqrt{(16.978 \frac{m}{s})^2 + (7.765 \frac{m}{s})^2} = 18.669 \frac{m}{s}$

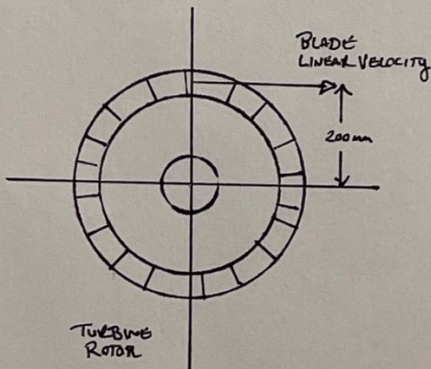
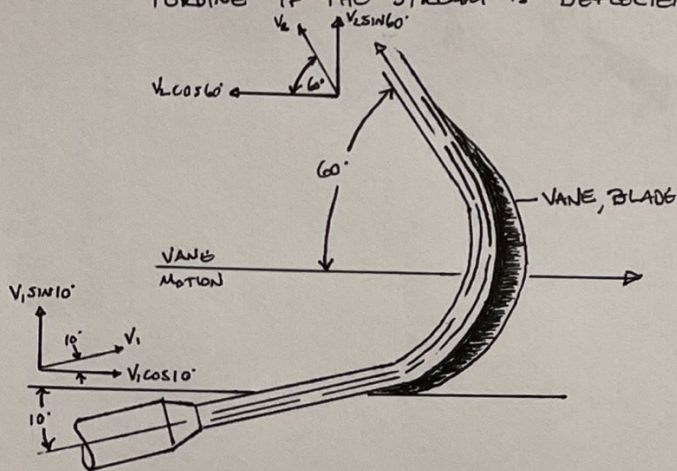
$\sum F_x = 0, R_x = M (V_{effx} + V_{x1})$
 $= (586.505 \frac{kg}{s}) (18.409 \frac{m}{s} + 16.978 \frac{m}{s})$
 $= 20754.7 \text{ N}$

$V_{effx} = V_R \cos \beta$
 $= 18.669 \frac{m}{s} \cos 9.577^\circ$
 $= 18.409 \frac{m}{s}$

$\sum F_y = 0, R_y = M (V_{effy} + V_{y1})$
 $= (586.505 \frac{kg}{s}) (0 + 7.765 \frac{m}{s})$
 $= 4554.21 \text{ N}$

$V_{effy} = 0$

16.29) TURBINE IN WHICH THE INCOMING STREAM OF WATER AT 15°C HAS A DIAMETER OF 7.5 mm AND IS MOVING WITH A VELOCITY OF $25 \frac{\text{m}}{\text{s}}$. COMPUTE THE FORCE ON ONE BLADE OF THE TURBINE IF THE STREAM IS DEFLECTED THROUGH THE ANGLE SHOWN AND THE BLADE IS STATIONARY.



GIVEN: $D = 7.5 \text{ mm} = 0.0075 \text{ m}$

$V_1 = 25 \frac{\text{m}}{\text{s}} = V_2$

BLADE IS STATIONARY

$\rho_w = 1000 \frac{\text{kg}}{\text{m}^3}$

SOLUTION: $A = \frac{\pi}{4} D^2 = \frac{\pi}{4} (0.0075 \text{ m})^2 = 0.0004418$
 $= 4.418 \times 10^{-5} \text{ m}^2$

$Q = A \cdot V = (4.418 \times 10^{-5} \text{ m}^2) (25 \frac{\text{m}}{\text{s}}) = 0.0011045$
 $= 1.1045 \times 10^{-3} \frac{\text{m}^3}{\text{s}}$

$\Sigma F_x = 0, R_x = \rho_w \cdot Q \cdot (V_1 \cos 10^\circ - (-V_2 \cos 60^\circ))$
 $= (1000 \frac{\text{kg}}{\text{m}^3}) (1.1045 \times 10^{-3} \frac{\text{m}^3}{\text{s}}) (25 \frac{\text{m}}{\text{s}} \cos 10^\circ + 25 \frac{\text{m}}{\text{s}} \cos 60^\circ)$
 $= 40.9993 = 41 \text{ N}$
 $R_x = 41 \text{ N}$

$\Sigma F_y = 0, R_y = \rho_w \cdot Q \cdot (V_1 \sin 10^\circ - V_2 \sin 60^\circ)$
 $= (1000 \frac{\text{kg}}{\text{m}^3}) (1.1045 \times 10^{-3} \frac{\text{m}^3}{\text{s}}) (25 \frac{\text{m}}{\text{s}} \sin 10^\circ - 25 \frac{\text{m}}{\text{s}} \sin 60^\circ)$
 $R_y = -19.1183 \text{ N}$