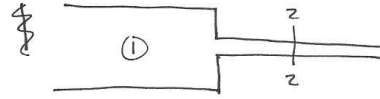


HW 2.1: CH10 - (20, 37, 39, 43, 46, 48) CH11 - 5, 13, 20

10 #20 Determine the energy loss for a sudden contraction from a DN 125 schedule 80 steel pipe to a DN 50 schedule 80 pipe for a flow rate of 500 L/min. = $0.5 \text{ m}^3/\text{min} = 0.008 \text{ m}^3/\text{s}$

→ sudden contraction $h_L = K \frac{V_2^2}{2g}$



→ cont. eqn.: $Q = v \cdot A$ $V_1 = \frac{Q}{A_1}$ $V_2 = \frac{Q}{A_2}$

→ Bernoulli's: $\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + h_L$

→ $Q = 500 \text{ L/min} = 30 \text{ m}^3/\text{s}$

→ diameter of DN 125: 141.3 mm ϕ

→ diameter of DN 50: 60.3 mm ϕ

$\frac{D_2}{D_1} = 0.43$

→ ~~$K = 0.5$~~

→ $V_2 = \frac{Q}{A_2} = \frac{0.008 \text{ m}^3/\text{s}}{\left(\frac{(0.0603 \text{ m})^2 \pi}{4}\right)} = V_2 = 2.8 \text{ m/s}$

→ K is found from Figure 10.8:

$K = 0.45$

→ $h_L = K \frac{V_2^2}{2g} = (0.45) \frac{(2.8 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)}$

$h_L = 0.18 \text{ m}$

10.57) Bernoulli equation

$$\frac{P_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_f - h_L = \frac{P_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$$

energy in pipe

$$P_1 - P_2 = \gamma (h_L + h_f)$$

energy loss because of bend

$$h_L = K \left(\frac{v^2}{2g} \right)$$

Given

$$\text{temperature} = 77^\circ\text{F}$$

$$Q (\text{flow rate}) = 12.5 \text{ gal/min}$$

USE $Q = Av$ to get discharge of flow

A = area

v = velocity of flow

$$\text{Switch formula around to } v = \frac{Q}{A} \quad \frac{12.5 \text{ change to ft}^3/\text{s} = 0.275}{(.0021)}$$

google says

$$.0022 \times 12.5 = .0275 \text{ ft}^3/\text{s}$$

$$v = 13.033 \text{ ft/s}$$

resistance coefficient closed bend

$$\begin{aligned} \text{Moody's diagram } K &= f_r (L/D) & L_e/D &= 50 \\ \text{given } f_r &= .26 & K &= (.26)(50) & E &= 1.5 \times 10^{-4} \\ & & &= 1.3 \end{aligned}$$

not use energy loss formula

$$h_L = 1.3 \left(\frac{(13.033)^2}{2(32.2)} \right) = 3.43 \text{ ft}$$

not use h_L due to friction (guess what our f_r so we can get f from Moody's diagram)

$$\begin{aligned} h_f &= f \times \frac{8}{.0518} \times \frac{(13.033)^2}{2(32.2)} \\ &= .04 \times \frac{8}{.0518} \times \frac{(13.033)^2}{2(32.2)} = 16.31 \text{ ft} \end{aligned}$$

fill in the $P_1 - P_2$ values

$$P_1 - P_2 = (68.5) (3.43 + 16.31) = \boxed{P_1 - P_2 = 1,552.19 \text{ lb/ft}^2}$$

10.8

$$Q = .40 \text{ ft}^3/\text{s}$$

$$A = .05132 \text{ ft}^2 \text{ (schedule 40 3" pipe)}$$

$$T = 50^\circ$$

$$h_L = f \frac{L_c}{D} \frac{V^2}{2g}$$

$$V = \frac{Q}{A} = \frac{.4 \text{ ft}^3/\text{s}}{.05132 \text{ ft}^2}$$

~~7.794 ft/s~~

$$V = 7.794 \text{ ft/s}$$

Table 10.4 = Tee with flow through tee (run)

$$= L_c/D = 20$$

Table 10.5 = New schedule 40 pipe

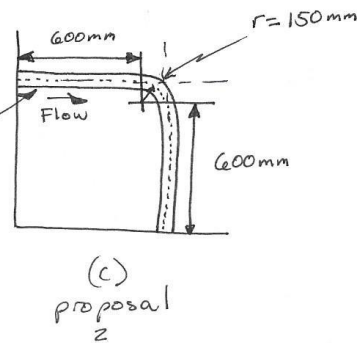
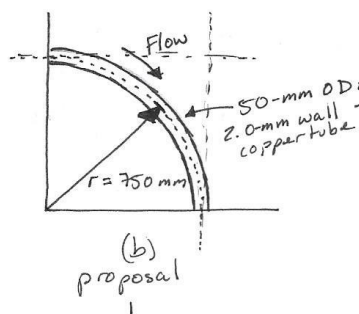
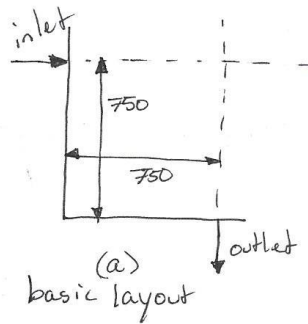
~~0.017~~ $f = .017$

$$h_L = (.017) \cdot (20) \cdot \left(\frac{(7.794 \text{ ft/s})^2}{2(32.2 \text{ ft/s}^2)} \right) = h_L = .32$$

$$h_L = .32$$

10 #43

The inlet & outlet shown ^{in (a)} are to be connected w/ a 50mm OD x 2.0mm wall copper tube to carry 750 L/min of propyl alcohol @ 25°C. Evaluate the two schemes shown in parts (b) & (c) w/ regard to the energy loss. Include the losses due to both the bend and the friction in the straight tube.



→ (b) $Q = 750 \text{ L/min} = 0.75 \text{ m}^3/\text{min} = 0.0125 \text{ m}^3/\text{s}$

→ $h_L = K \frac{V^2}{2g}$

→ $K = f_T \left(\frac{L_e}{D} \right)$ (for a pipe bend (figure 10.28))

→ $\frac{D}{\epsilon} = \frac{0.046 \text{ m}}{1.5 \times 10^{-6} \text{ m}} = 30,666.7$

→ $V = Q/A$

→ $D = 50 \text{ mm} - 2(2.0 \text{ mm}) = 46 \text{ mm} = 0.046 \text{ m}$

→ $\epsilon = (\text{table 8.2}) = 1.5 \times 10^{-6} \text{ m}$

→ $\frac{L_e}{D}$ (according to figure 10.28) ⇒ 43

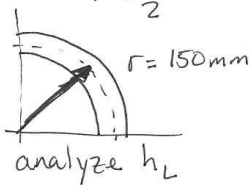
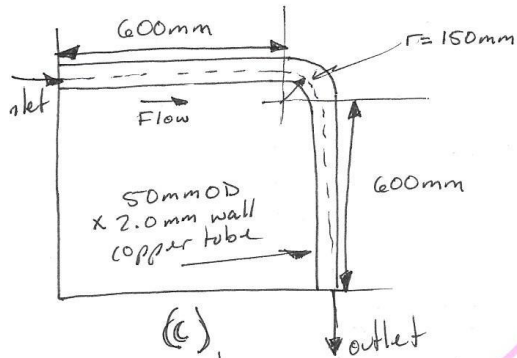
→ $\frac{r}{\text{inner } D} = \frac{750 \text{ mm}}{0.046 \text{ m}} = 16.3$ (now look @ figure 10.28)

→ $V = \frac{0.0125 \text{ m}^3/\text{s}}{\frac{\pi (0.046 \text{ m})^2}{4}} = 7.5 \text{ m/s} = V$

→ $f_T = 0.0095$ (according to moody's diagram on figure 8.7)

→ $K = f_T \left(\frac{L_e}{D} \right) = 0.0095(43) = 0.4085 = K$

→ $h_L = K \left(\frac{V^2}{2g} \right) = 0.4085 \left(\frac{(7.5 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} \right) = 1.17 = h_L$



$$\rightarrow h_L = K \frac{V^2}{2g}$$

$$\rightarrow K = f_T \left(\frac{L_e}{D} \right)$$

$$\rightarrow V = Q/A = \frac{0.0125 \text{ m}^3/\text{s}}{\frac{\pi (0.046 \text{ m})^2}{4}} = \boxed{7.5 \text{ m/s} = V}$$

$$\rightarrow \epsilon = 1.5 \times 10^{-6} \text{ m}$$

$$\rightarrow D = 0.046 \text{ m}$$

$$\rightarrow \frac{D}{\epsilon} = \frac{0.046 \text{ m}}{1.5 \times 10^{-6} \text{ m}} = 30,666.7 \therefore f_T = 0.0095$$

$$\rightarrow \frac{L_e}{D} \Rightarrow \frac{r}{D} = \frac{150 \text{ mm}}{0.046 \text{ m}} = 3.26 \therefore \left[\frac{L_e}{D} = 12 \text{ (according to figure 10.28)} \right]$$

$$\rightarrow K = f_T \left(\frac{L_e}{D} \right) = 0.0095 (12) = \boxed{0.114 = K}$$

$$\rightarrow h_L = (0.114) \left(\frac{(7.5 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} \right) = \boxed{0.327 \text{ m} = h_{L1}}$$

energy loss in 90° bend.
add this to the loss in
the straightened pipe
lengths.

→ to get h_L for a straight pipe; $h_L = f \times \frac{L}{D} \times \frac{V^2}{2g}$

→ to find Friction factor f calculate Reynold's number and divide into f ; use in turbulent eqn

$$\rightarrow Re = \frac{\rho \cdot V \cdot D}{\mu} = \frac{(802 \text{ kg/m}^3)(7.5 \text{ m/s})(0.046 \text{ m})}{1.92 \times 10^{-3} \frac{\text{kg} \cdot \text{m}}{\text{s}^2}} = 144109$$

$$\rightarrow Re = 144109$$

$$\rightarrow f = \text{Done in Excel calculator} = 0.0168$$

$$\rightarrow h_L = (0.0168)(0.6 \text{ m}) \frac{(7.5 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} = 0.028 \text{ m}$$

$$\text{Total } h_L = h_{L1} + h_{L2} + h_{L3} = 0.327 + (0.028)2$$

$$h_L = 1.58 \text{ m}$$

10#46 | The figure shows a test setup for determining the energy loss due to a heat exchanger. Water @ 50°C is flowing vertically upward @ $6.0 \times 10^{-3} \text{ m}^3/\text{s}$. Calculate the energy loss between points 1 & 2. Determine the resistance coefficient for the heat exchanger based on the velocity in the inlet tube.

Step 1: write continuity & Bernoulli's

$$Q = V \cdot A \quad V_1 \cdot A_1 = V_2 \cdot A_2$$

$$\rightarrow \frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + h_L$$

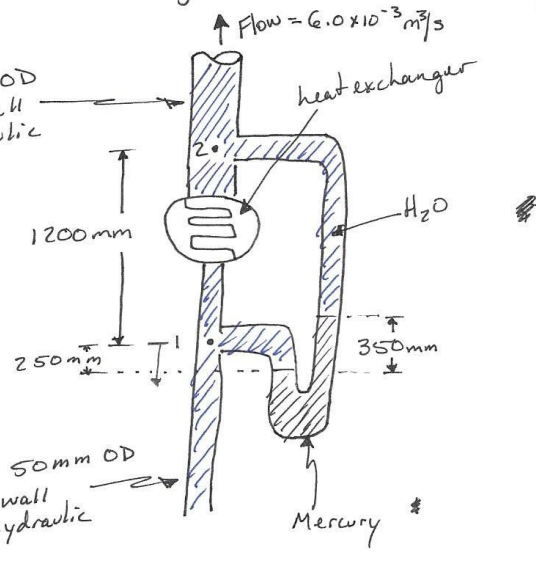
solve for

Step 2: minor loss using resistance coefficient

$$\rightarrow h_L = K \left(\frac{V^2}{2g} \right)$$

velocity of flow in pipe
BEFORE heat exchanger
(so, it's V_1)

100mm OD
x 3.5mm wall
steel hydraulic
tube



Step 3: solve for K using the whole of Bernoulli's Eqn

$$\rightarrow \frac{P_1}{\gamma} + \frac{V_1^2}{2g} + z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + z_2 + K \left(\frac{V_1^2}{2g} \right)$$

* Analysis *

→ we know everything right off the bat, except pressures 1 & 2. solving them will have to do with the manometer on the side.

We know $P_1 > P_2$

$$\rightarrow P_1 + (\gamma_{H_2O})(0.25\text{m}) - (\gamma_{\text{mercury}})(0.35\text{m}) - (\gamma_{H_2O})(1.1\text{m}) = P_2$$

$$P_1 + (9.69\text{ kN/m}^3)(0.25\text{m}) - (132.8\text{ kN/m}^3)(0.35\text{m}) - (9.69\text{ kN/m}^3)(1.1\text{m}) = P_2$$

$$P_1 + 2.42\text{ kPa} - 46.48\text{ kPa} - 10.659\text{ kPa} = P_2$$

$$\boxed{P_1 - 54.72\text{ kPa} = P_2} \quad (\text{solved for } P_2 \text{ in terms of } P_1)$$

$$\rightarrow V_1 = \frac{Q}{A_1} = \frac{6.0 \times 10^{-3} \text{ m}^3/\text{s}}{0.001662 \text{ m}^2} \Rightarrow V_1 = 3.61 \text{ m/s} = V_1$$

$$\rightarrow V_2 = \frac{Q}{A_2} = \frac{6.0 \times 10^{-3} \text{ m}^3/\text{s}}{6.793 \times 10^{-3} \text{ m}^2} \Rightarrow V_2 = 0.88 \text{ m/s}$$

→ Rewrite the stars and Bernoulli's Eqn

$$\rightarrow \frac{P_1}{\gamma_{H_2O}} + \frac{V_1^2}{2g} + \cancel{z_1}^0 = \frac{P_2}{\gamma_{H_2O}} + \frac{V_2^2}{2g} + \check{z_2} + K(V_1^2/2g)$$

$$\frac{P_1}{9.69 \text{ kN/m}^3} + \frac{(3.61 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} = \frac{P_1 - 54.72 \text{ kPa}}{9.69 \text{ kN/m}^3} + \frac{(0.88 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} + 1.2 \text{ m} + K \left(\frac{3.61^2}{2(9.81)} \right)$$

$$\cancel{\frac{P_1}{9.69 \text{ kN/m}^3}} - \cancel{\frac{P_1}{9.69 \text{ kN/m}^3}} + 0.664 \text{ m} + 5.647 \text{ m} - 0.0395 \text{ m} - 1.2 \text{ m} = K(0.661 \text{ m})$$

$$5.072 \text{ m} = K(0.661 \text{ m})$$

$$[K = 7.67]$$

$$\rightarrow h_L = K(V_1^2/2g) = (7.67) \left(\frac{3.61 \text{ m/s}^2}{2(9.81 \text{ m/s}^2)} \right) = (7.67)(0.661 \text{ m})$$

$$h_L = 5.07 \text{ m}$$

10 #48] Compute the energy loss in a 90° bend in a steel tube used for a fluid power system. The tube has a 1 1/4-in OD and a wall thickness of 0.083 in. The mean bend radius is 3.25 in. The flow rate of hydraulic oil is 27.5 gal/min.

→ $Q = 27.5 \text{ gal/min}$

→ compute h_L :

→ $h_L = K \frac{v^2}{2g}$

→ $K = f_T \left(\frac{L_e}{D} \right)$ (for a pipe bend)
(Figure 10.28)

→ $\frac{D}{\epsilon} = \text{---}$ (use to help find f_T from Moody diagram (8.7))

→ $V = Q/A$

→ $D = 1.25 - 2(0.083) = [1.084 \text{ in}] = 0.0903 \text{ ft}$

→ $V = \frac{27.5 \text{ gal}}{\text{min}} \cdot \frac{1}{4} \frac{1}{(1.084 \text{ in})^2}$

$\frac{27.5 \text{ gal}}{\text{min}} = 0.062 \text{ ft}^3/\text{s}$

$V = \frac{0.062 \text{ ft}^3/\text{s}}{0.00409 \text{ ft}^2} = [9.67 \text{ ft/s} = V] = [116.04 \text{ in/s}]$

→ $\epsilon = (\text{table 8.2}) = 1.5 \times 10^{-4} \text{ ft}$

→ $\frac{D}{\epsilon} = \frac{0.0903 \text{ ft}}{1.5 \times 10^{-4} \text{ ft}} = 602 \therefore f_T = 0.022$

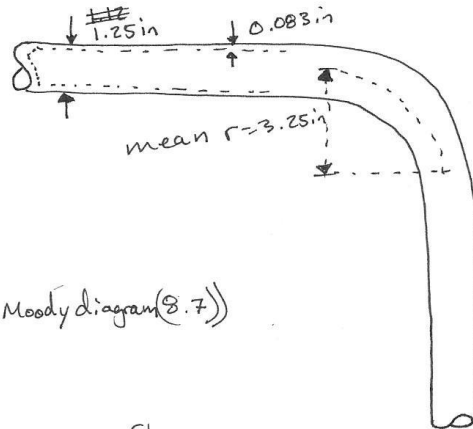
→ ~~---~~

→ $\frac{L_e}{D} = (\text{according to Figure 10.28}) =$

→ $\left[\frac{r}{D} = \frac{3.25 \text{ in}}{1.084 \text{ in}} = 3.00 \right] \cdot \left[\frac{L_e}{D} = 12 \right]$

→ $K = f_T \left(\frac{L_e}{D} \right) = (0.022)(12) = 0.264$

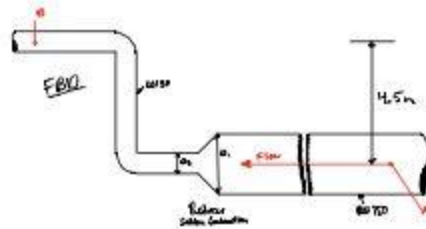
→ $h_L = 0.264 \left(\frac{(9.67 \text{ ft/s})^2}{2(32.2 \text{ ft/s}^2)} \right) \Rightarrow h_L = 0.38$



Homework 2.1

11-5) Given:

- $Q_{tot} = 0.015 \frac{m^3}{s}$
- $V_a = 9.80 \frac{m}{s}$
- $V_b = 2.12 \times 10^{-2} \frac{m}{s}$
- Length of 60/100 pipe = 150m
- Length of 100/50 pipe = 3m
- Both pipes are Schedule 80 steel
- $D_{60/100} = 146.3mm = 0.1463m$
- $D_{100/50} = 41.3mm = 0.0413m$



- Considering all pipe friction and minor losses, calculate the pressure at A.

Step 1) Determine velocities with $Q = VA$

$$Q = V_a A_a \quad V_a = \frac{Q}{A_a} = \frac{0.015}{\frac{\pi (0.1463)^2}{4}} = 9.80 \frac{m}{s}$$

$$Q = V_b A_b \quad V_b = \frac{Q}{A_b} = \frac{0.015}{\frac{\pi (0.0413)^2}{4}} = 2.12 \frac{m}{s}$$

Step 2) Determine Friction Factors

- $N_{Re} = \frac{V_a D_a}{\nu} = \frac{(9.80)(0.1463)}{(1.12 \times 10^{-6})} = 6129$
 $\rightarrow N_{Re} = 6.13 \times 10^3$
- D/e with Schedule 80 STEEL pipe, $E = 4.6 \times 10^{-5} m$
 Using $D_a = 0.1463m$, $\frac{D_a}{E} = \frac{0.1463}{4.6 \times 10^{-5}} \rightarrow \frac{D_a}{E} = 3174$
- Now with $N_{Re} = 6.13 \times 10^3$ and $\frac{D_a}{E} = 3174$, using Moody's diagram

$$f_{sa} = 0.015 \quad f_{sb} = 0.055$$

- $N_{Re} = \frac{V_b D_b}{\nu} = \frac{(2.12)(0.0413)}{(1.12 \times 10^{-6})} = 18190$
 $\rightarrow N_{Re} = 1.82 \times 10^4$
- $\frac{D_b}{E}$, $E = 4.6 \times 10^{-5} m$ and using $D_b = 0.0413m$
 $\frac{D_b}{E} = \frac{0.0413}{4.6 \times 10^{-5}} \rightarrow \frac{D_b}{E} = 1045$
- Now with $N_{Re} = 1.82 \times 10^4$ and $\frac{D_b}{E} = 1045$, using Moody's diagram

$$f_{sa} = 0.019 \quad f_{sb} = 0.028$$

Step 3) Determine minor losses in pipes

$$h_{L1} = f_{L1} \cdot \left(\frac{L}{D}\right) \cdot \left(\frac{V^2}{2g}\right) = 0.035 \cdot \left(\frac{1.20 \text{ m}}{0.104 \text{ m}}\right) \cdot \left(\frac{(2.09 \text{ m/s})^2}{2 \cdot 9.81 \text{ m/s}^2}\right) \approx 0$$

$$\hookrightarrow h_{L1} = 1.74 \text{ m}$$

$$h_{L2} = f_{L2} \cdot \left(\frac{L}{D}\right) \cdot \left(\frac{V^2}{2g}\right) = 0.028 \cdot \left(\frac{2.0 \text{ m}}{0.104 \text{ m}}\right) \cdot \left(\frac{(2.09 \text{ m/s})^2}{2 \cdot 9.81 \text{ m/s}^2}\right) \approx 0$$

$$\hookrightarrow h_{L2} = 14.43 \text{ m}$$

$$h_{L3} = K_{\text{elbow}} \cdot \left(\frac{V^2}{2g}\right) = (2) \cdot 2.0 \cdot 0.04 \cdot \left(\frac{(2.09 \text{ m/s})^2}{2 \cdot 9.81 \text{ m/s}^2}\right) \approx 0$$

$$\hookrightarrow h_{L3} = 2.74 \text{ m}$$

$$h_{L4} = K \left(\frac{V^2}{2g}\right), \text{ with } K = 0.5 \text{ and } V = 2.09 \text{ m/s} \rightarrow K = 0.57$$

$$\downarrow$$

$$= 0.57 \cdot \left(\frac{(2.09 \text{ m/s})^2}{2 \cdot 9.81 \text{ m/s}^2}\right) \approx 0$$

$$\hookrightarrow h_{L4} = 1.17 \text{ m}$$

$$\text{Sum all energy losses: } \Sigma h_L = h_{L1} + h_{L2} + h_{L3} + h_{L4} = 1.74 + 14.43 + 2.74 + 1.17 \approx 20$$

$$\hookrightarrow \Sigma h_L = 18.74 \text{ m}$$

Step 4) Use Bernoulli's Equation and plug in values to find P_A

$$\frac{P_A}{\gamma} + z_A + \frac{V_A^2}{2g} - h_L = \frac{P_B}{\gamma} + z_B + \frac{V_B^2}{2g}$$

$$\frac{P_A}{\gamma} + 0 + \frac{(0.919 \text{ m/s})^2}{2 \cdot (9.81 \text{ m/s}^2)} = \frac{P_B}{\gamma} + (4.5 \text{ m}) + \frac{(2.09 \text{ m/s})^2}{2 \cdot (9.81 \text{ m/s}^2)} + h_L$$

$$\frac{P_A}{9.81 \text{ kN/m}^3} = \frac{12.5 \text{ MPa}}{9.81 \text{ kN/m}^3} + (4.5 \text{ m}) + \left(\frac{(2.09 \text{ m/s})^2}{2 \cdot (9.81 \text{ m/s}^2)}\right) + 18.74 \text{ m}$$

$$\frac{P_A - (12.5 \text{ MPa})}{9.81 \text{ kN/m}^3} = 27.35 \text{ m} \cdot 9.81 \text{ kN/m}^3$$

$$P_A = 12.5 \text{ MPa} + 270.7 \text{ kPa}$$

$$P_A = 270.7 \text{ kPa} + 12.5 \text{ MPa} \approx [12.5 + 0.27 \text{ MPa}]$$

$$P_A = 12.74 \text{ MPa}$$

$$\therefore P_A = 12.74 \text{ MPa}$$

- 11-11) Water at 15°C is flowing downward in a vertical tube 2.5 m long. The pressure is 550 kPa at the top and 98.5 kPa at the bottom. A ball-type check valve is installed near the bottom. The hydraulic tube is drawn steel, with a 32 mm OD and a 2.0 mm wall thickness. Compute the volume flow rate of water.

• Given (Top-bottom = A-B respectively):

$$\begin{aligned} T &= 15^\circ\text{C} : \gamma = 9.81 \frac{\text{N}}{\text{m}^3} \\ P_A &= 550 \text{ kPa} \quad P = 1000 \frac{\text{kg}}{\text{m}^3} \\ P_B &= 98.5 \text{ kPa} \quad \eta = 1.15 \times 10^{-3} \text{ Pa}\cdot\text{s} \\ L &= 2.5 \text{ m} \quad \nu = 1.15 \times 10^{-6} \frac{\text{m}^2}{\text{s}} \\ 32 \text{ mm OD} \\ t &= 2 \text{ mm} \end{aligned}$$

• Step 1) Determine cross-sectional area of pipe.

$$\begin{aligned} D &= \text{OD} - 2t = 32 - 2(2) \text{ mm} \\ &\rightarrow D = 28 \text{ mm} = 0.028 \text{ m} \end{aligned}$$

$$\begin{aligned} A &= \frac{\pi D^2}{4} = \frac{\pi (0.028)^2}{4} \\ &\rightarrow A = 6.16 \times 10^{-5} \text{ m}^2 \end{aligned}$$

• Step 2) Determine ρ_e ratio with $D = 0.028$

$$\begin{aligned} \text{Drawn Steel } \epsilon &= 1.5 \times 10^{-4} \text{ m} \\ \rho_e &= \frac{1.5 \times 10^{-4}}{0.028} \\ &\rightarrow \rho_e = 1.866 \end{aligned}$$

• Step 3) Apply and rearrange Bernoulli's

$$\frac{P_A}{\rho} + z_A + \frac{V_A^2}{2g} = \frac{P_B}{\rho} + z_B + \frac{V_B^2}{2g} \quad \text{put everything in m (Bernoulli)}$$

$$\begin{aligned} \left(\frac{P_A - P_B}{\rho} \right) + (z_A - z_B) + \left(\frac{V_A^2 - V_B^2}{2g} \right) &= h_{L_e} \quad [V = 0 \text{ everywhere}] \\ h_{L_e} &= \left(\frac{550 - 98.5}{9.81} \right) + (2.5 - 0) + \frac{V^2 - 0}{2g} = 0 \\ &\rightarrow h_{L_e} = 5.15 \text{ m} \end{aligned}$$

• Step 4) Determine Velocity using Darcy's

$$\begin{aligned} h_{L_e} &= f \cdot \left(\frac{L}{D} \right) \cdot \left(\frac{V^2}{2g} \right) \\ 5.15 \text{ m} &= f \cdot \left(\frac{2.5}{0.028} \right) \cdot \left(\frac{V^2}{2 \cdot 9.81} \right) \\ \frac{5.15 \text{ m}}{2.5} &= f \cdot \frac{V^2}{0.028} \\ 2.06 \text{ m} &= f \cdot \frac{V^2}{0.028} \\ \frac{0.028}{2.06} &= \frac{f \cdot V^2}{0.028} \\ V &= \sqrt{\frac{0.028^2}{2.06}} \quad \text{Eq. 1} \\ V &= \sqrt{\frac{0.028^2}{2.06}} \quad \text{Eq. 2} \\ V &= \sqrt{\frac{0.028^2}{2.06}} \quad \text{Eq. 3} \\ &\rightarrow V = 4 \text{ m/s} \end{aligned}$$

• Step 5) Determine friction factor for velocity

$$\begin{aligned} N_{Re} &= \frac{\rho V D}{\mu} = \frac{(1000 \frac{\text{kg}}{\text{m}^3})(4 \text{ m/s})(0.028 \text{ m})}{1.15 \times 10^{-3} \text{ Pa}\cdot\text{s}} \\ &\rightarrow N_{Re} = 24342.02 \approx V \end{aligned}$$

• Make assumption for f to see if it gives us a value and again [Start set up using Excel for trials]

$$\begin{aligned} \text{for } f = 0.018, \quad V &= \sqrt{\frac{0.028^2}{2.06}} = 4 \text{ m/s} \rightarrow N_{Re} = 24342.02 \approx V \\ &\rightarrow \text{best accepted assumption } f = 0.018 \quad (\text{solve for } V) \end{aligned}$$

• Step 6) Determine flow rate, Q

$$\begin{aligned} Q &= V \cdot A = (4 \text{ m/s}) \cdot (6.16 \times 10^{-5} \text{ m}^2) \\ &\rightarrow Q = 0.000246 \text{ m}^3/\text{s} \end{aligned}$$

$$\therefore Q = 0.00246 \frac{\text{m}^3}{\text{s}}$$

11.20)

Bernoulli equation

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} + z_1 = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + h_L$$

$$\frac{P_5}{\rho g} (H-y) + y = \frac{0}{\rho g} + 0 + h_L$$

$$H - y + y = h_L$$

$$H = h_L$$

Known : Temperature = 80°F

length = 75 ft

flow rate = 400 gal/min

steel pipes roughness $\epsilon = 1.5 \times 10^{-5}$ ft

Kinetic viscosity of water at 80°F = 9.15×10^{-6} ft²/s

Size of pipe dia

$$D = .66 \left[(1.5 \times 10^{-5})^{1.25} \left(\frac{75 \times (400 \times \frac{1}{6.24})^2}{32.2 \times H} \right)^{0.75} + 9.15 \times 10^{-6} \left(\frac{400 \times 1}{5.2 \times H} \right)^{2.4} \right]^{0.04}$$

$$D = .66 \times \left[1.66 \times 10^{-5} \left(\frac{16.48}{(H)^{4.85}} + \frac{1.57 \times 10^{-9}}{(H)^{5.2}} \right)^{0.04} \right]$$

$$D = .66 \left[\frac{24.031}{(H)^{4.85}} + \frac{1.57 \times 10^{-9}}{(H)^{5.2}} \right]^{0.04}$$

Assume or guess your value of H

$$H = (12 \text{ ft})$$

$$= .66 \left[\frac{24.031}{(12)^{4.85}} + \frac{1.57 \times 10^{-9}}{(12)^{5.2}} \right]^{0.04}$$

$$\boxed{D = .485 \text{ ft}}$$