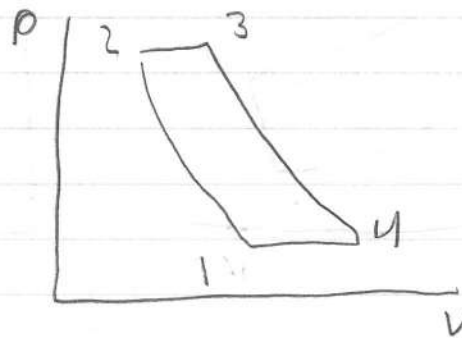
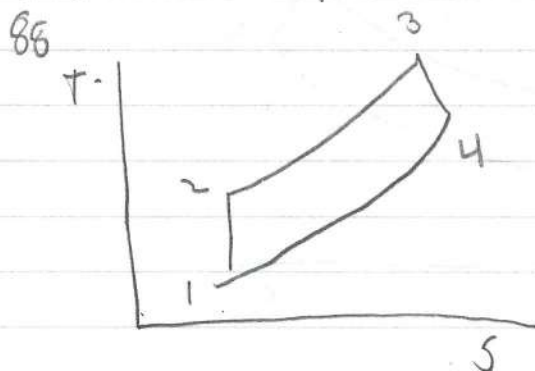


Thermal applications HW 1.5 Ben Smithson
88, 99, 107, 119, 121



① $T_1 = 273 \text{ K}$
 $P_1 = 10 \text{ kPa}$

② $T_2 = 527 \text{ K}$

③ $T_3 = 1025 \text{ K}$

④ $T_4 = 530.7 \text{ K}$

$$\left(\frac{T_2}{T_1}\right)_s = \left(\frac{P_2}{P_1}\right)^{(k-1)/k}$$

$$T_2 = (273)(10)^{0.4/1.4} = 527 \text{ K}$$

$$W_{2-1} = m c_p (T_1 - T_2) = (1)(1.005 \frac{\text{kJ}}{\text{kg} \cdot \text{K}})(273 - 527) = -255.3$$

$$T_3 = T_2 + \frac{2Q_3}{m c_p} \quad 2Q_3 = c_p (T_3 - T_2) = 500 \text{ given}$$

$$T_3 = 527 + \frac{500 \text{ kW}}{(1)(1.005)} \left(\frac{\text{KJ/s}}{\text{KW}} \right) = 1025 \text{ K}$$

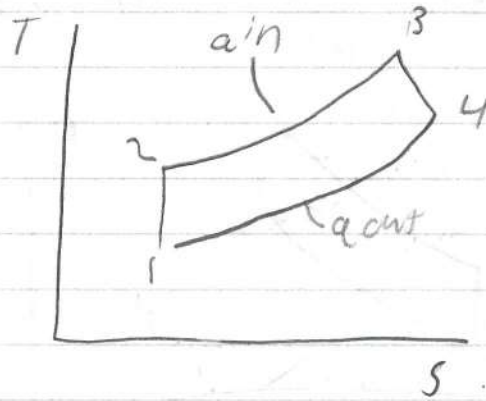
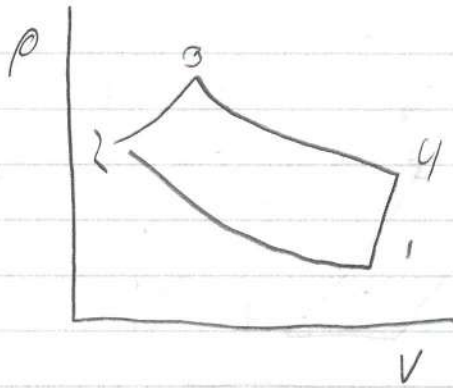
$$\left(\frac{T_4}{T_3}\right) = \left(\frac{P_4}{P_3}\right)^{(k-1)/k} = (1025) \left(\frac{1}{10}\right)^{(0.4/1.4)} = 530.7 \text{ K}$$

$$3W_{4-3} = m c_p (T_3 - T_4) = (1)(1.005)(1025 - 530.7) = 496$$

$$W_{\text{net}} = W_{2-1} + 3W_{4-3} = (-255.3) + (496) = 241 \frac{\text{KJ}}{\text{s}}$$

$$\eta_{th} = \frac{W_{\text{net}}}{Q_{in}} = 241 / 500 = 0.48 = 48\%$$

99



①

$$T_1 = 303 \text{ K}$$

$$P_1 = 100 \text{ kPa}$$

②

$$T_2 = 585$$

③

$$T_3 = 545.9$$

④

$$T_4 = 1073 \text{ K}$$

T₅

$$\frac{T_2}{T_1} = \frac{P_2}{P_1}^{\left(\frac{1.4-1}{1.4}\right)} = 10^{\left(\frac{0.4}{1.4}\right)}$$

$$303 \text{ K}$$

$$T_2 = 585 \text{ K}$$

$$\frac{T_4}{T_5} = \left(\frac{P_4}{P_5}\right)^{\left(\frac{1.4-1}{1.4}\right)}$$

$$T_5 = \frac{1073}{10^{(0.2857)}} = 545.9 \text{ K}$$

$$T_5 - T_3 = 10$$

$$T_3 = 10 - 545.9$$

$$m = \frac{115 \text{ kW}}{236.3}$$

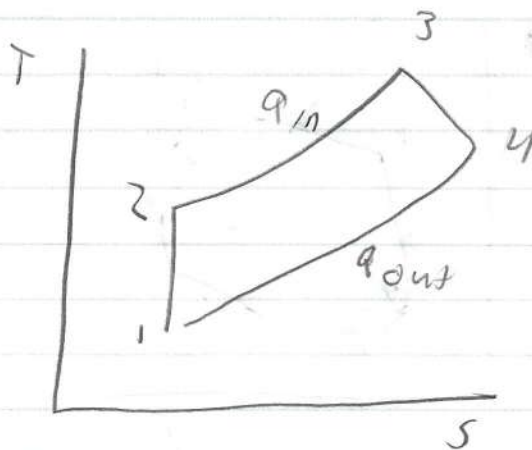
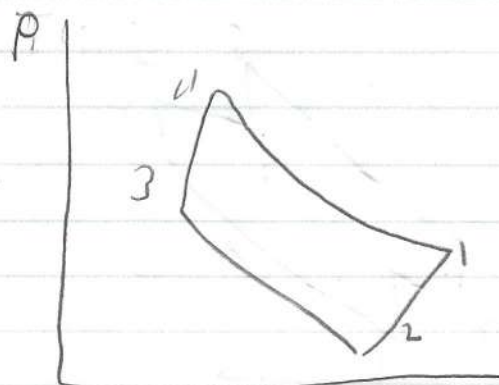
$$Q_{in} = m \cdot c_p \cdot (T_4 - T_3) = (0.48) (1.005) (1073 - 545.8) = 257 \text{ kW}$$

$$T_5 - T_6 = T_3 - T_2 = 245.8 - 585 - 545.9 = 595 \text{ K}$$

$$Q_{out} = 0.48 (1.005) \cdot (595 - 303) = 142 \text{ kW}$$

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1071



$$R_p = 55\%$$

$$\epsilon = 65\%$$

$$R_1 = 82\%$$

①

$$T_1 = 310K$$

②

$$T_2 = 617.3K$$

③

$$T_3 = 1150K$$

④

$$T_4 = 750K$$

$$T_2 = 310 \cdot 7^{\frac{1.4-1}{1.4}} = 540.3 =$$

$$\frac{T_2 - T_1}{T_2' - T_1} = \frac{540.3 - 310}{T_2' - 310} = 617.3$$

$$\frac{T_4}{T_3} = \left(\frac{P_4}{P_3}\right)^{\frac{\gamma-1}{\gamma}}$$

$$T_4 = \frac{T_3}{7^{\frac{1.4-1}{1.4}}} = \frac{1150}{7^{\frac{0.4}{1.4}}} = 659.5K$$

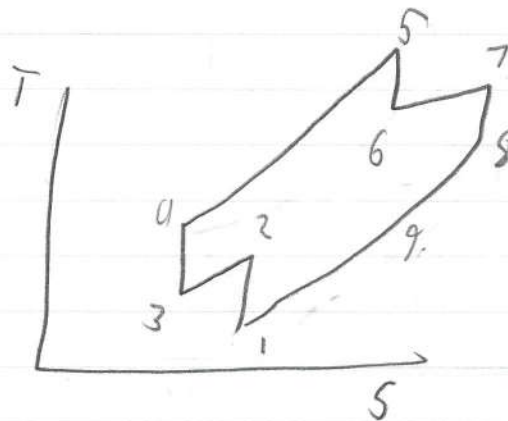
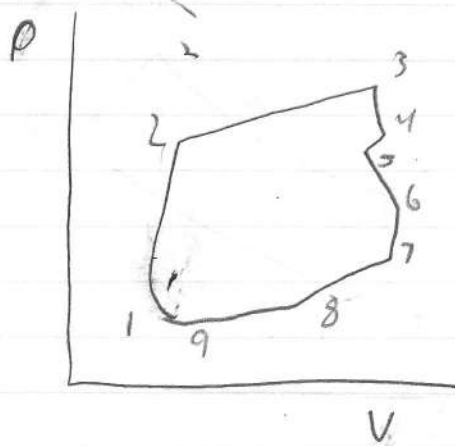
$$\frac{T_3 - T_4}{T_3 - T_4} = 0.82 = \frac{1150 - T_4}{1150 - 659.5} = \boxed{750K}$$

$$W_{net} = 1.005(1150 - 750)(617.3 - 310) = \boxed{981KJ/kg}$$

$$\epsilon = \frac{T_4 - T_2}{T_4' - T_2} = \frac{750 - 617.3}{750 - 617.3} = 700K$$

$$\eta_{th} = \frac{98}{1.005(1150 - 700K)} = \boxed{22\%}$$

119



① $T_1 = 300\text{K}$
 $h_1 = 300.19\text{ kJ/kg}$
 $P_{r1} = 1.38$

② $P_{r2} = 4.15$
 $h_2 = 411.25$

③ $P_{r3} = 4.92$
 $h_3 = 421.2$

④

⑤ $T_5 = 1200\text{K}$
 $h_5 = 1277.8\text{ kJ/kg}$
 $P_{r5} = 238$

⑥ $P_{r6} = 80$

⑦
 ⑧

Pressure ratio = 3

$$P_{r2} = \frac{P_2}{P_1} = 3 \cdot 1.38 = 4.15$$

$$\frac{h_2 - 411.12}{421.26 - 411.12} = \frac{4.15 - 4.19}{4.92 - 4.15} = 411.25\text{ kJ/kg}$$

$$P_{r6} = \frac{P_6}{P_5} P_{r5} = \frac{1}{3} \cdot 238 = 80$$

$$P_r = 75$$

$$n = 932$$

$$P_r = 82$$

$$n = 955$$

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$$\frac{h_6 - 932.9}{955.3 - 932.9} = \frac{79.3 - 75.3}{820 - 75.3} = h_6 - 932.9 = (955.3 - 932.9)$$

$$\frac{79.3 - 75.3}{820 - 75.3} = 946.35$$

$$w_{in} = 2(h_2 - h_1) = 2(411.25 - 300) = 222.13 \text{ kJ/kg}$$

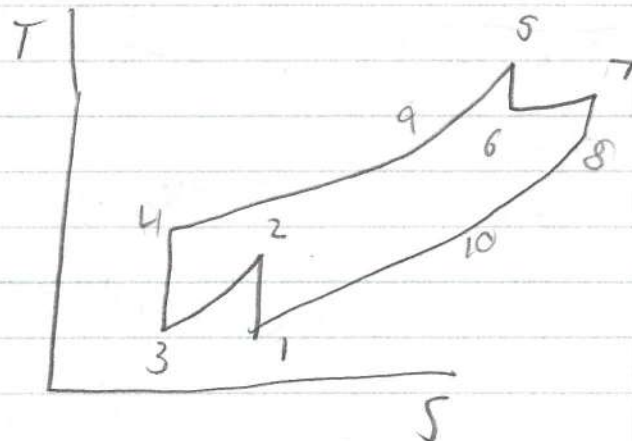
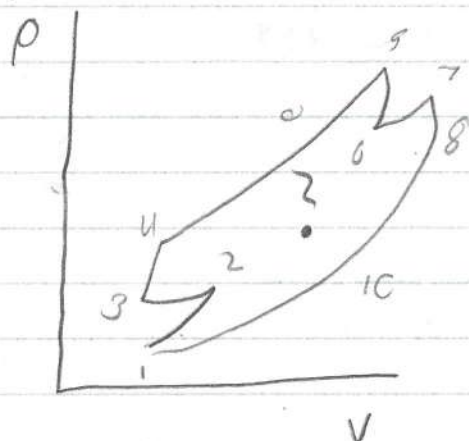
$$w_{out} = 2(h_5 - h_6) = 2(1277.8 - 946.3) = 662.86 \text{ kJ/kg}$$

$$w_{net} = w_{out} - w_{in} = 662.8 - 222.13 = 440.73$$

$$W = m w_{net} = (110 \times 10^3) = m(440.73) =$$

$$m = 250 \text{ kg/s}$$

121



① $h_1 = 300.19$ $P_{r1} = 1.38$ ② $P_{r2} = 4.15$ $h_2 = 411.26$ ③ $h_3 = 411.26$ ④ $h_4 = 411.26$ ⑤ $T_5 = 1200K$ $P_{r5} = 238$ $h_5 = 1277.8$ ⑥ $P_{r6} = 79.7$ $h_6 = 946$ ⑦ $T_7 = 1200K$ $h_7 = 1277.8$ ⑧ $h_8 = 946$

$$P_{r2} = \frac{P_2}{P_1} P_{r1} = 3(1.38) = 4.15$$

$$h_2 = h_4 = 411.26$$

$$T_5 = T_7 = 1200K \quad A-17$$

$$h_5 = h_7 = 1277.8 \text{ (K) / kg}$$

$$P_{r5} = 238$$

$$P_{r6} = \frac{P_6}{P_5} \quad P_{r5} = \frac{1}{3} 1238 = 79.7$$

$$h_6 = h_8 = 946.136$$

$$w_{in} = 2(h_2 - h_1) = 2(411.26 - 300.19) = 222.14 \text{ (K) / kg}$$

$$w_{out} = 2(h_5 - h_6) = 2(1277.8 - 944.3) = 662.8 \text{ (K) / kg}$$

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$$\frac{w_{in}}{w_{out}} = \frac{222.14}{662.8} = 0.335 = 33.5\%$$

$$q_{in} = (h_5 - h_4) + (h_7 - h_6) = (1277.79 - 411.2) + (1277.7 - 946.3) \\ = 1197 \text{ kJ/kg}$$

$$\eta_{th} = \frac{w_{net}}{q_{in}} = \frac{(662.86 - 222.14)}{1197} = \boxed{36.8\%}$$

$$\frac{w_{in}}{w_{out}} = 33.5\%$$

$$t(h_8 - h_4) = 0.75 (946.36 - 411.26) = 401.33 \text{ kJ/kg}$$

$$q_{in} = q_{in} - q_{out} = (1197 - 401.3) = 796 \text{ kJ/kg}$$

$$\eta_{th} = \frac{w_{net}}{q_{in}} = \frac{(662.8 - 222.14)}{796.6} = 0.553 = \boxed{55.3\%}$$