

## Homework #1

Ch 1: Nature of Fluids & Ch 2: Viscosity of Fluids and  
Pressure

MET 330 Virginia Beach Distance Learning WC2 and  
Campus

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CH 2 48, 88, 43, 76, 92, 107

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Problem 48

The coin press requires a force of 18000 lb.

Hydraulic cylinder has as a diameter of 2.50 in

Compute oil pressure.

Given  $F = 18000 \text{ lb}$   $D = 2.50 \text{ in}$   $1 \text{ psi} = 1 \text{ lb/in}^2$

use pressure formula

$$P = \frac{F}{A} \quad \text{Find } A$$

cylinder

$$A = \frac{\pi D^2}{4} \quad A = \frac{\pi (2.50 \text{ in})^2}{4} \quad A \approx 4.909 \text{ in}^2$$

$$P = \frac{F}{A} = \frac{18000 \text{ lb}}{4.909 \text{ in}^2} = 3666.734569 \text{ psi}$$

$$P = 3666.7 \text{ psi}$$

Problem 58

Compute the pressure change required to cause  
a decrease in the volume of mercury by 1.00%.

Express the result in both psi and MPa

Given  $E$  mercury based on the bulk modulus

Mercury  $68^\circ\text{F}/20^\circ\text{C}$  is  $3.59 \text{ Mpsi}/24750 \text{ MPa}$

$$E = 3.59 \text{ Mpsi}$$

$$\text{Formula for bulk} = E = \frac{-\Delta P}{(\Delta V)/V}$$

$$\frac{(\Delta V)/V}{1.00\%} = 0.01 \quad (\text{decrease in volume})$$

$$\frac{\Delta V}{V} = -0.01$$

Mercury

Problem 58 cont.

$$E = \frac{-\Delta p}{(\Delta V)/V}$$

Find  $\Delta p$

$$\Delta p = -E(\Delta V/V)$$

For PSI

$$\Delta p = -(3.59 \text{ Mpsi} \times -0.01) \\ = \boxed{35900 \text{ psi}}$$

MPa

$$\Delta p = -(24750 \text{ MPa} \times -0.01) \\ = \boxed{247.5 \text{ MPa}}$$

Problem 63



### Problem 63

A measure of the stiffness of a linear actuator system is the amount of force required to cause a certain linear deflection.

For an actuator that has an inside diameter of 0.50 in and a length of 42.0 in and that is filled with machine oil, compute the stiffness in lb/in.

Given  $D = 0.50 \text{ in}$

$L = 42.0$

Bulk modulus  $E = -\frac{p}{(\Delta V/V)}$

Stiffness - Actuator

$$k_A = \frac{F}{\Delta L}$$



$$E = 189000 \text{ lb/in}^2$$

This problem requires equation plugged into other equation but first

Area of actuator

$$A = \frac{1}{4} \pi d^2 \Rightarrow \frac{1}{4} \pi (0.5 \text{ in})^2$$

$$= 0.1963 \text{ in}^2$$

Break down bulk modulus equation to match up

$$\epsilon = \frac{F}{\Delta L}$$

$$\text{Pressure } p = \frac{F}{A}$$

$$\text{Volume} = A \times L$$

$$\Delta \text{Volume} = -A \times \Delta L$$

Place in formula

Stiffness

$$E = -\left(\frac{F}{A}\right) \times \frac{\Delta L}{-A \times \Delta L} = \frac{F}{\Delta L} = \frac{EA}{L}$$

$$= \frac{EA}{L} = \frac{189000 \text{ lb/in}^2 \times 0.1963 \text{ in}^2}{42.0 \text{ in}}$$

$$\text{Stiffness} = 883.35 \text{ lb/in}$$

## Problem 76

In the US, hamburger and other meats are sold by the pound. Assuming that this is 1.00 lb force, compute the mass in slugs, the mass in kg, and the weight

Given: mass of man  $m = \frac{W}{g}$

Slugs  $W = 1.0 \text{ lbf}$

$g = 32.2 \text{ ft/s}^2$   $m = \frac{1.0 \text{ lbf}}{32.2 \text{ ft/s}^2}$

$m = 0.031 \text{ lbf} \cdot \text{s}^2/\text{ft}$  (mass of man)

$= 0.031 \text{ slugs}$

kg Find mass of mass  $1 \text{ lbf} \rightarrow \text{N}$

Given weight of man  $\Rightarrow 1 \text{ lbf} = 4.448 \text{ N}$

$g = 9.81 \text{ m/s}^2$

$m = \frac{W}{g} = \frac{(4.448 \text{ N})}{9.81 \text{ m/s}^2} = 0.4534 \text{ N} \cdot \frac{\text{s}^2}{\text{m}}$

$= \boxed{0.4534 \text{ kg}}$

Weight of the meat

meat = 1 lbf

$= \boxed{4.448 \text{ N}}$



problem 92

A cylindrical container is 150 mm in diameter and weighs 2.25 N when empty. When filled to a depth of 200 mm with a certain oil, it weighs 35.4 N.

Calculate the specific gravity of the oil

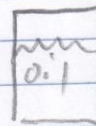
Given

$D = 150 \text{ mm}$  of cylindrical container

Empty weight of container = 2.25 N

Depth of oil = 200 mm

Weight + oil = 35.4 N



← Container

$$\begin{aligned}\text{The weight of the oil} &= 35.4 - 2.25 \\ &= 35.4 \text{ N} - 2.25 \text{ N} = 33.15 \text{ N}\end{aligned}$$

Vol of cylinder  $V = \pi r^2 h$

$$r = 150 \text{ mm} = 75 \text{ mm} = 0.075 \text{ m} \quad h = 200 \text{ mm} = 0.200 \text{ m}$$

$$= (\pi)(0.075 \text{ m})^2 (0.200 \text{ m})$$

$$V = 3.534 \times 10^{-3} \text{ m}^3$$

Specific weight

$$\gamma = \frac{w}{V} = \frac{\text{weight of oil}}{\text{Volume}} = \frac{33.15 \text{ N}}{3.534 \times 10^{-3} \text{ m}^3}$$

$$\gamma = 9380.3056$$

$$= 9380.31 \frac{\text{N}}{\text{m}^3}$$

match units  
to  $\text{KN/m}^3$

$$\text{Specific gravity} = \frac{\gamma_{\text{oil}}}{\gamma_{\text{water @ } 4^\circ\text{C}}} = \frac{9380.31 \frac{\text{N}}{\text{m}^3} \times 10^3}{9.81 \text{ KN/m}^3}$$

$$= \frac{9.380 \text{ KN/m}^3}{9.810 \text{ KN/m}^3} =$$

$$sg = 0.956167$$

$$\boxed{sg = 0.956}$$

### Problem 107

Alcohol has a specific gravity of 0.79.

Calculate its density both in  $\text{slugs/ft}^3 \rightarrow \text{g/cm}^3$

Given:

$$\text{Specific gravity} = sg = 0.79$$

Density

$$\rho = (sg)(\rho_{\text{water}} @ 4^\circ\text{C})$$

$$= 0.79 \times 1.94 \text{ slugs/ft}^3$$

$$= \boxed{1.53 \text{ slugs/ft}^3}$$

$\text{g/cm}^3$

$$1 \text{ slugs/ft}^3 = 0.5155 \text{ g/cm}^3$$

$$\rho = (1.53 \text{ slugs/ft}^3) \left( \frac{0.5155 \text{ g/cm}^3}{1 \text{ slugs/ft}^3} \right)$$

$$\rho = 0.78795$$

$$\boxed{\rho = 0.79 \text{ g/cm}^3}$$



CH2 17, 18, 27, 35, 40

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12/3/17

### Problem 17

Give examples of the

Non-Newtonian fluids

- Thixotropic fluids like blood
- Solid particles that turn into liquid. These are electrorheological fluids.
- Toothpaste is another example. These are Bingham fluids.
- Dilatant fluids like cornstarch

### Problem 18

Appendix D gives dynamic viscosity for a variety of fluids as a function of temperature. Using this appendix give the value of the viscosity for the following fluids: Water at 40°C

$$\text{Viscosity @ } 40^\circ\text{C} = \boxed{6.5 \times 10^{-4} \text{ Pa}\cdot\text{s}}$$

(Based on Appendix D)

### Problem 27

Use Appendix D to find Hydrogen at 40°F

$$\text{Viscosity @ } 40^\circ\text{F} = \boxed{1.7 \times 10^{-7} \text{ lb}\cdot\text{s}/\text{ft}^2}$$



Problem 35

SAE 30 oil at  $210^{\circ}\text{F}$  Based on Appendix D

The viscosity @  $210^{\circ}\text{F}$   
 $= 2.2 \times 10^{-4} \text{ lb.s/ft}^2$

# Problem 61

In a falling ball viscometer, a steel ball 1.66 mm in diameter is allowed to fall freely in a heavy fuel oil having a specific gravity of 0.94. Steel weighs 77 kN/m<sup>3</sup>. If the ball is observed to fall 250 mm in 10.4 s, calculate the viscosity of the oil.

FBD of the ball

Given

$$D = 1.6 \text{ mm} = 1.6 \times 10^{-3} \text{ m}$$

$$S_g = 0.94$$

$$(\text{steel ball}) \gamma_s = \gamma = 77 \text{ kN/m}^3$$

$$\text{The ball travel } 250 \text{ mm } t = 10.4 \text{ s}$$

$$\eta = \text{viscosity of oil}$$

kinematic

viscosity

$$\eta = \frac{F_d}{3\pi\eta V}$$

$$W - F_b - F_d = 0$$

$$S_g = \frac{\text{specific weight of oil}}{\text{specific weight of water}} = 0.94 = \frac{\gamma}{9.81 \text{ kN/m}^3}$$

Find oil

$$\gamma_s = 0.94 [9.81 \text{ kN/m}^3]$$

$$= 9.2214 \text{ kN/m}^3$$

oil x volume of ball

$$F_b = \gamma_s \left( \frac{\pi D^3}{6} \right) = 9.2214 \text{ kN/m}^3 \left( \frac{\pi (1.6 \times 10^{-3})^3}{6} \right)$$

$$F_b = 1.978 \times 10^{-8} \text{ kN}$$

Find weight of ball

$$W = \gamma V = 77 \text{ kN/m}^3 \left( \frac{\pi (1.6 \times 10^{-3})^3}{6} \right) = 7.651 \times 10^{-7} \text{ kN}$$



Go back to equation

$$W - F_b - F_d = 0$$
$$(1.651 \times 10^{-7} \text{ kN}) - (1.978 \times 10^{-8}) - F_d = 0$$

$$F_d = (1.651 \times 10^{-7} \text{ kN}) - (1.978 \times 10^{-8} \text{ kN})$$

$$F_d = 1.453 \times 10^{-7} \text{ kN}$$

What is the velocity

$$V = \frac{\text{Distance}}{\text{time}} = \frac{0.25 \text{ m}}{10.9 \text{ s}} = 0.024 \text{ m/s}$$

now use

$$\gamma = \frac{F_d}{3\pi\eta l} = \frac{1.453 \times 10^{-7} \text{ kN}}{3\pi (0.024 \text{ m/s})(1.6 \times 10^{-3} \text{ m})}$$

$$\gamma = 4.01479 \times 10^{-4} \frac{\text{kN}\cdot\text{s}}{\text{m}^2}$$
$$= 4.015 \times 10^{-4} \frac{\text{kN}\cdot\text{s}}{\text{m}^2}$$

$$\gamma = 4.015 \times 10^{-4} \text{ kPa}\cdot\text{s} \text{ or } 0.4015 \text{ Pa}\cdot\text{s}$$

Homework 1 - ch 1: 48, 56, 63, 76, 92, 107  
ch 2: 17, 18, 21, 35, 61

chapter 1

1.48  $P = \frac{F}{A}$



$$P = \frac{15000 \text{ lb}}{4.90625 \text{ in}^2} = 3061.79 \text{ lb/in}^2$$

$$\frac{\pi d^2}{4} = A$$

$$\frac{3.14 \cdot (2.5 \text{ in})^2}{4} = 4.90625 \text{ in}^2$$

1.58  $E = \frac{-\Delta p}{(\Delta V)/V}$

$$\Delta p = -E \left[ \frac{\Delta V}{V} \right] = [-3,590,000 \text{ psi}] [-0.012] = 35900 \text{ psi}$$

or 247,502 N/m<sup>2</sup>

1.63 Stiffness =  $\frac{F}{\Delta L}$

$$V = A \cdot L$$

$$\Delta V = A \cdot \Delta L$$

$$882 \text{ lb/in}$$

F = Force

$\Delta L$  = Displacement

$$E = \frac{F}{A}$$

$$\frac{F}{A} = \frac{A \cdot L}{A \cdot \Delta L}$$

$$\frac{F}{\Delta L} = \frac{EA}{L}$$

$$E = \frac{P}{\Delta V/V}$$

$$\frac{A \cdot \Delta L}{A \cdot L}$$

F1

$$P = \frac{F}{A}$$

$$A = \frac{\pi d^2}{4}$$

$$\frac{\pi (0.502)^2}{4}$$

$$A = 0.196 \text{ in}^2$$

$$\frac{489000 \text{ lb}}{42}$$



$$1.76 \quad W = mg \quad m = \frac{16 \cdot 5}{1} = 80 \text{ g} \quad g = 32.2 \text{ ft/s}^2$$

$$\frac{m \cdot W}{g} = \frac{1.16 \text{ F}}{32.2 \text{ ft/s}^2}$$

$$m = 0.031 \text{ 16F} \cdot \text{s}^2 / \text{Ft} \text{ or } 80 \text{ g}$$

$$16 \text{ F} = 4.448 \text{ N} \quad 1 \text{ N} = \text{kg} \cdot \text{m/s}^2$$

$$\frac{1.16 \text{ F} \cdot 4.448 \text{ N}}{1.16 \text{ F}} = 4.448 \text{ N}$$

$$m = \frac{4.448 \text{ N}}{9.81 \text{ m/s}^2} = 0.453 \text{ N} \cdot \text{s}^2 / \text{m}$$

$$m = 0.453 \text{ kg}$$

$$1.92 \quad S_g = \frac{\gamma_o}{\gamma_w @ 4^\circ \text{C}}$$

$$\gamma_o = W/V$$

$$D = 150 \text{ mm} = 0.15 \text{ m}$$

$$r = 75 \text{ mm} = 0.075 \text{ m}$$

$$2.25$$

$$V = \pi r^2 h$$

$$200 \text{ mm} = 0.2 \text{ m}$$

$$\frac{35.40 \text{ N} - 2.25 \text{ N}}{33.15 \text{ N}}$$

$$V = \pi (0.075)^2 (0.2)$$

$$V = 0.00353 \text{ m}^3$$

$$\gamma'_{oi} = W_{oi} / V_{oi}$$

$$= 33.15 / 0.00353 \quad \gamma'_{oi} = 9390.934 \text{ N/m}^3$$

$$\frac{9390.934 \text{ N-m}^3}{1000} = 9390.934 \text{ N/m}^3$$

1.10)  $S_g = 0.79$   
 $P = 29.4 \text{ mm Hg}$

$S_g = \frac{P_v}{P_{\text{atm}}}$   
 $P_{\text{atm}} = 101.325 \text{ kPa}$

$S_g \cdot P_{\text{atm}} \cdot \rho_v = P_v$

$0.79 \cdot 101.325 \text{ kPa} = P_v$

$P_v = 10.525 \text{ kPa}$

$10.525 \text{ kPa} \cdot \frac{1 \text{ kg/m}^3}{1 \text{ kPa}} = 10.525 \text{ kg/m}^3$

## Chapter 2

2.17 Pseudoplastic, Dilatant Fluids, Bingham Fluids, Thixotropic

2.18  $W @ 40^\circ\text{C}$

Viscosity =  $4.3 \times 10^{-4} \text{ Pa}\cdot\text{s}$

2.27 Hydrogen @  $40^\circ\text{F}$

Viscosity =  $1.6 \times 10^{-7} \text{ lb}\cdot\text{s/ft}^2$

2.35 SAE 30 oil @  $210^\circ\text{F}$

Viscosity =  $2.2 \times 10^{-4} \text{ lb}\cdot\text{s/ft}^2$



$$2.6 \quad D = 1.6 \text{ mm} = 1.6 \times 10^{-3} \text{ m} \quad \gamma = 77 \text{ kN/m}^3$$

$$\gamma = \frac{F_d}{3\pi v D}$$

$$\gamma = 10.94 \cdot 9.91 \text{ kN/m}^3 = 9.22 \text{ kN/m}^3$$

$$F_{ball} = \frac{9.22 \pi D^3}{6} = \frac{9.22 \pi \times 1.6 \times 10^3}{6} = 1.97 \times 10^{-4} \text{ kN}$$

$$\text{Velocity} = \frac{D}{T} = \frac{0.25 \text{ m}}{10.45} = 0.024 \text{ m/s}$$

$$W = \gamma V = 77 \text{ kN/m}^3 \cdot 2.14 \times 10^{-9} = 1.6478 \times 10^{-7} \text{ kN}$$

$$W - F_b - F_d = 0 \quad 1.6478 \times 10^{-7} \text{ kN} - 1.97 \times 10^{-4} \text{ kN} - F_d = 0$$

$$F_d = 1.45 \times 10^{-7} \text{ kN}$$

$$\gamma = \frac{1.45 \times 10^{-7} \text{ kN}}{3\pi (0.024 \text{ m/s}) (1.6 \times 10^{-3} \text{ m})} = 4.0065 \times 10^{-4} \text{ kN} \cdot \text{s/m}^2$$

$$\gamma = 0.4006 \text{ Pa} \cdot \text{s}$$

## Homework 1.1

Chapter 1: 48, 58, 63, 76, 92, 107

Chapter 2: 17, 18, 27, 35, 61

- 1-48 A coining press is used to produce commemorative coins with the likenesses of all the U.S. presidents. The coining process requires a force of 18000 lb. The hydraulic cylinder has a diameter of 2.50 in. Compute the required oil pressure.

$$P = \frac{F}{A} \quad F = 18000 \text{ lb} \quad A = ? \quad A = \frac{\pi}{4} (d)^2 \rightarrow A = \frac{\pi}{4} (2.5)^2$$

$$A = 4.9087 \text{ in}^2$$

$$P = \frac{18000 \text{ lb}}{4.9087 \text{ in}^2} = 3666.96 \text{ lb/in}^2 \text{ or psi}$$

- 1-58 Compute the pressure change required to cause a decrease in the volume of mercury by 1.00 percent. Express the result in Psi and MPa

$$E = \frac{\Delta P}{\Delta V / V} \quad \text{change in pressure } \Delta P = -E \left( \frac{\Delta V}{V} \right)$$

mercury atm 80° 3.59 x 10<sup>5</sup> psi 24,750 MPa

$$\Delta P = -(3.59 \times 10^5 \text{ psi}) \left( -\frac{1.00}{100} \right) = 35,900 \text{ psi}$$

$$\Delta P = -(24,750 \text{ MPa}) \left( -\frac{1.00}{100} \right) = 247.5 \text{ MPa}$$

- 1-63 A measure of the stiffness of a linear actuator system is the amount of force required to cause a certain linear deflection. For an actuator that has an inside diameter of 0.50 in and a length of 42.0 in and that is filled with machine oil compute the stiffness in lb/in

$$\text{stiffness} = \frac{F}{\Delta L} \quad E = \frac{F}{\Delta V / V} \quad P = \frac{F}{A} \quad V = A \times L$$

$$\Delta V = -A(\Delta L) \quad E = \frac{\left( \frac{F}{A} \right)}{\frac{-A(\Delta L)}{A \times L}} \rightarrow -\frac{F}{A} \times \frac{A \times L}{-A(\Delta L)} = \frac{FL}{A(\Delta L)} \rightarrow \frac{F}{\Delta L} = \frac{EA}{L}$$

$$A = \frac{\pi}{4} (d)^2 \rightarrow \frac{\pi}{4} (0.50)^2 = 0.196 \text{ in}^2 \quad \text{machine oil} = 189,000 \text{ psi}$$

$$\frac{F}{\Delta L} = \frac{E \times A}{L} = \frac{(189,000 \text{ lb/in}^2)(0.196 \text{ in}^2)}{42 \text{ in}} = 882 \text{ lb/in}$$



- 1-7b In the United States, hamburger and other meats are sold by the pound. Assuming that this is 1.00-lb force, compute the mass in slugs, in kg and the weight in N.

$$m = \frac{W}{g} \quad g = 32.2 \text{ ft/s}^2$$

$$m = \frac{1 \text{ lbF}}{32.2 \text{ ft/s}^2} = 0.031 \text{ lbF} \cdot \text{s}^2/\text{ft} \quad m = 0.031 \text{ slugs}$$

$$1 \text{ lbF} = 4.448 \text{ N} \quad W = 1 \text{ lbF} \left( \frac{4.448 \text{ N}}{1 \text{ lbF}} \right) = 4.448 \text{ N}$$

$$m = \frac{4.448 \text{ N}}{9.81 \text{ m/s}^2} = 0.453 \text{ N} \cdot \text{s}^2/\text{m} \quad m = 0.453 \text{ kg}$$

$$W = 4.448 \text{ N}$$

- 1-9a A cylindrical container is 150 mm in diameter and weighs 2.25 N when empty. When filled to a depth of 200 mm with a certain oil, it weighs 35.4 N. Calculate the specific gravity of the oil.

$$D = 150 \text{ mm} \quad r = \frac{150}{2} = 75 \text{ mm} \left( \frac{1 \text{ m}}{1000 \text{ mm}} \right) = 0.075 \text{ m} \quad \text{Empty } W = 2.25 \text{ N}$$

$$\text{Oil depth} = 200 \text{ mm} \left( \frac{1 \text{ m}}{1000 \text{ mm}} \right) = 0.2 \text{ m} \quad W_{\text{container with oil}} = 35.4 \text{ N}$$

$$\text{Weight of oil} = (35.4 - 2.25 \text{ N}) = 33.15 \text{ N} \left( \frac{1 \text{ kN}}{1000 \text{ N}} \right) = 0.03315 \text{ kN}$$

$$V = \pi r^2 h \rightarrow (\pi)(0.075^2)(0.2) = 3.534 \times 10^{-3} \text{ m}^3 \quad \text{Specific weight oil } \gamma_{\text{oil}} = \frac{W_{\text{oil}}}{V}$$

$$\gamma_{\text{oil}} = \frac{0.03315 \text{ kN}}{3.534 \times 10^{-3} \text{ m}^3} = 9.38 \text{ kN/m}^3 \quad \text{Specific Gravity} = \frac{\gamma_{\text{oil}}}{\gamma_{\text{water @ 4}^\circ\text{C}}}$$

$$\gamma_{\text{water @ 4}^\circ\text{C}} = 9.81 \text{ kN/m}^3 \quad Sg = \frac{9.38 \text{ kN/m}^3}{9.81 \text{ kN/m}^3} \quad Sg = 0.956 \text{ kN/m}^3$$

- 1-107 Alcohol has a specific gravity of 0.79. Calculate its density both in slug/ft<sup>3</sup> and g/cm<sup>3</sup>.

$$Sg = 0.79 \quad P = Sg \times P_{\text{water @ 4}^\circ\text{C}}$$

$$P = 0.79 \times 1.94 \text{ slugs/ft}^3 \quad P = 1.53 \text{ slug/ft}^3$$

$$1 \text{ slug/ft}^3 = 0.515 \text{ g/cm}^3$$

$$P = 1.53 \text{ slug/ft}^3 \times \frac{0.515 \text{ g/cm}^3}{1 \text{ slug/ft}^3} \quad P = 0.79 \text{ g/cm}^3$$

2-17 Give four examples of the types of Fluids that are non-Newtonian.

- Pseudoplastic - Dilatant Fluids - Bingham Fluids - Thixotropic

2-18 Give the value of the viscosity  
Water at 40°C

$$\text{viscosity} = 6.3 \times 10^{-4} \text{ Pa}\cdot\text{s}$$

2-27 Hydrogen at 40°F

$$\text{viscosity} = 1.6 \times 10^{-7} \text{ lb}\cdot\text{s}/\text{ft}^2$$

2-35 SAE 30 oil at 80°F

$$\text{viscosity} = 2.9 \times 10^{-4} \text{ lb}\cdot\text{s}/\text{ft}^2$$

2-61 In a falling-ball viscometer, a steel ball 1.6mm in diameter is allowed to fall freely in a heavy fuel oil having a specific gravity of 0.94. Steel weighs 77 kN/m<sup>3</sup>. If the ball is observed to fall 250 mm in 10.45s. Calculate oil viscosity

$$D = 1.6 \text{ mm} = 1.6 \times 10^{-3} \text{ m} \quad \text{sg} = 0.94 \quad \gamma = 77 \text{ kN/m}^3$$

$$\gamma = \frac{\rho}{\rho_w} \gamma_w = (0.94)(9.81) \text{ kN/m}^3 = 9.22 \text{ kN/m}^3$$

$$F_{\text{ball}} = 9.22 \left( \frac{\pi D^3}{6} \right) = 9.22 \left( \frac{\pi \times 1.6 \times 10^{-3}}{6} \right) = 1.97 \times 10^{-7} \text{ kN}$$

$$\text{Velocity } v = \frac{D}{t} = \frac{0.25 \text{ m}}{10.45} = 0.024 \text{ m/s}$$

$$W = \gamma V \rightarrow (77 \text{ kN/m}^3) \left( \frac{\pi D^3}{6} \right) = 1.6478 \times 10^{-7} \text{ kN}$$

$$W - F_b - F_d = 0 \rightarrow (1.6478 \times 10^{-7} \text{ kN}) - (1.97 \times 10^{-7} \text{ kN}) - F_d = 0$$

$$F_d = 1.45 \times 10^{-7} \text{ kN}$$

$$\eta = \frac{1.45 \times 10^{-7} \text{ kN}}{3\pi (0.024 \text{ m/s}) (1.6 \times 10^{-3} \text{ m})} = 4.0065 \times 10^{-4} \text{ kN}\cdot\text{s}/\text{m}^2$$

$$\eta = 0.4006 \text{ Pa}\cdot\text{s}$$