HOMEWORK MODULE 3 SOLUTIONS

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10.20 Sudden contraction: $h_L = K(v_2^2/2g)$ $\frac{D_1}{D_2} = \frac{122.3 \text{ mm}}{49.3 \text{ mm}} = 2.48$ $v_2 = \frac{Q}{A_2} = \frac{500 \text{ L/min}}{1.905 \times 10^{-3} \text{ m}^2} \times \frac{1 \text{ m}^3/\text{s}}{60000 \text{ L/min}} = 4.37 \text{ m/s}; K = 0.38 \text{ (Table 10.3)}$ $h_L = (0.38)(4.37)^2/2(9.81) = 0.371 \text{ m}$

10.37 Pt. 1 at inlet; Pt. 2 at outlet

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_{L_{pipe}} - h_{L_{bend}} = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}: \quad v_1 = v_2; \text{ assume } z_1 = z_2$$

$$p_1 - p_2 = \gamma \left(h_{L_{pipe}} + h_{L_{bend}} \right)$$

Close return bend:
$$L_e/D = 50$$
, $f_T = 0.027$ (Table 10.5)
 $v = \frac{Q}{A} = \frac{12.5 \text{ gal/min}}{0.00211 \text{ ft}^2} \times \frac{1 \text{ ft}^3/\text{s}}{449 \text{ gal/min}} = 13.19 \text{ ft/s}$
 $N_R = \frac{vD\rho}{\mu} = \frac{(13.19)(0.0518)(2.13)}{3.38 \times 10^{-4}} = 4.31 \times 10^3$
 $D/\varepsilon = 0.0518/1.5 \times 10^{-4} = 345$: $f = 0.041$
 $h_{L_{\text{bool}}} = f_T \frac{L_e}{D} \frac{v^2}{2g} = (0.027)(50) \frac{(13.19)^2}{2(32.2)} \text{ ft} = 3.65 \text{ ft}$
 $h_{L_{\text{tabe}}} = f_T \frac{L}{D} \frac{v^2}{2g} = (0.041) \left[\frac{8.00}{0.0518} \right] \frac{(13.19)^2}{2(32.2)} = 17.12 \text{ ft}$
 $p_1 - p_2 = (68.47)[17.12 + 3.65]/144 = 9.87 \text{ psi}$

10.39
$$v = \frac{Q}{A} = \frac{0.40 \text{ ft}^3/\text{s}}{0.05132 \text{ ft}^2} = 7.79 \text{ ft/s}$$
: **Tee-flow through run:** $\frac{L_e}{D} = 20$
 $f_T = 0.018 \text{ (Table 10.5)}$
 $h_L = f_T \frac{L_e}{D} \frac{v^2}{2g} = (0.018)(20) \frac{(7.79)^2}{2(32.2)} = 0.340 \text{ ft}$

10.43 **Proposal 1 - Pipe bend:**
$$\frac{r}{D} = \frac{750 \text{ mm}}{49.8 \text{ mm}} = 15.1; \frac{L_e}{D} = 40.5 \text{ (Fig. 10.23)}$$

 $v = \frac{Q}{A} = \frac{750 \text{ L/min}}{1.945 \times 10^{-3} \text{ m}^2} \times \frac{1 \text{ m}^3/\text{s}}{60000 \text{ L/min}} = 6.43 \text{ m/s}$
 $N_R = \frac{vD\rho}{\mu} = \frac{(6.43)(0.0498)(802)}{1.92 \times 10^{-3}} = 1.34 \times 10^5; \frac{D}{\varepsilon} = \frac{0.0498}{1.5 \times 10^{-6}} = 33200;$
 $f = 0.017; f_T = 0.010 \text{ in zone of complete turbulence}$
 $h_L = f_T \frac{L_e}{D} \frac{v^2}{2g} = (0.010)(40.5) \frac{(6.43)^2}{2(9.81)} = 0.85 \text{ m}$

Proposal 2 - Bend + tube:
$$\frac{r}{D} = \frac{150 \text{ mm}}{49.8 \text{ mm}} = 3.01: \frac{L_e}{D} = 11.8$$

 $h_{L_{\text{bend}}} = f_T \frac{L_e}{D} \frac{v^2}{2g} = (0.010)(11.8) \frac{(6.43)^2}{2(9.81)} = 0.248 \text{ m}$
 $h_{L_{\text{babe}}} = f \frac{L}{D} \frac{v^2}{2g} = (0.017) \frac{1.20}{0.0498} \frac{(6.43)^2}{2(9.81)} = 0.862 \text{ m}$
 $h_{L_{\text{babe}}} = 1.11 \text{ m}$

10.46
$$\frac{p_1}{\gamma_w} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma_w} + z_2 + \frac{v_2^2}{2g}$$

$$h_L = \frac{p_1 - p_2}{\gamma_w} + z_1 - z_2 + \frac{v_1^2 - v_2^2}{2g}$$

$$A_I = \frac{\pi D_1^2}{4} = \frac{\pi (0.050 \text{ m})^2}{4} = 0.001963 \text{ m}^2$$

$$A_2 = \frac{\pi D_2^2}{4} = \frac{\pi (0.10 \text{ m})^2}{4} = 0.007854 \text{ m}^2$$

$$\frac{z_1 - z_2 = -1.20 \text{ m}}{v_1} = \frac{Q}{A_1} = \frac{6.0 \times 10^{-3} \text{ m}^3/\text{s}}{0.001963 \text{ m}^2} = 3.056 \text{ m/s:} \quad \frac{v_1^2}{2g} = \frac{(3.056)^2}{2(9.81)} = 0.476 \text{ m}$$

$$v_2 = \frac{Q}{A_2} = \frac{6.0 \times 10^{-3}}{0.007854} = 0.764 \text{ m/s:} \quad \frac{v_2^2}{2g} = \frac{(0.764)^2}{2(9.81)} = 0.0297 \text{ m}$$

$$\frac{10.46}{Manometer:} \frac{p_1 + \gamma_w(0.25 \text{ m}) - \gamma_w(0.35 \text{ m}) - \gamma_w(1.10 \text{ m}) = p_2}{p_1 - p_2} = \gamma_m(0.35 \text{ m}) + \gamma_w(1.10 - 0.25)\text{ m}}$$

$$\frac{p_1 - p_2}{\gamma_w} = \frac{\gamma_m(0.35 \text{ m})}{\gamma_w} + \frac{\gamma_w(0.85 \text{ m})}{\gamma_w} = \frac{132.8(0.35 \text{ m})}{9.69} + 0.85 \text{ m}$$

$$\frac{p_1 - p_2}{\gamma_w} = 4.80 \text{ m} + 0.85 \text{ m} = 5.65 \text{ m}$$

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$$\frac{p_1 - p_2}{\gamma_w} = 4.80 \text{ m} + 0.476 \text{ m} = 10.3$$

10.48 90° Bend. Steel tube; 1 1/4 in OD × 0.083 in wall thickness. r = 3.25 in. D = 1.084 in = 0.09033 ft. $D/\varepsilon = 0.09033/1.5 \times 10^{-4} = 602$. Then $f_T = 0.023$ in fully turbulent zone. $A = 6.409 \times 10^{-3}$ ft². Q = 27.5 gal/min = 0.0612 ft³/s. $v = Q/A = (0.0612 \text{ ft}^3/\text{s})/(0.006409 \text{ ft}^2) = 9.556 \text{ ft/s}$ $(v^2/2g) = (9.556 \text{ ft/s})^2/[2(32.2 \text{ ft/s}^2)] = 1.418 \text{ ft. } r/D = 3.25 \text{ in}/1.084 \text{ in } = 3.00.$ $L_e/D = 12.5$ (Fig.10.27), $K = f_T/(L_e/D) = 0.023(12.5) = 0.288.$ $h_L = K(v^2/2g) = 0.288(1.418 \text{ ft}) = 0.408 \text{ ft} = h_L$

11.5 **Class I;**
$$\frac{p_{A}}{\gamma} + z_{A} + \frac{v_{A}^{2}}{2g} - h_{L} = \frac{p_{B}}{\gamma} + z_{B} + \frac{v_{B}^{2}}{2g}$$
,
Then $p_{A} = p_{B} + \gamma_{o} \left[(z_{A} - z_{B}) + \frac{v_{B}^{2} - v_{A}^{2}}{2g} + h_{L} \right]$
 $v_{A} = \frac{Q}{A_{A}} = \frac{0.015 \text{ m}^{3}/\text{s}}{1.682 \times 10^{-2} \text{ m}^{2}} = 0.892 \text{ m/s}; \frac{v_{A}^{2}}{2g} = \frac{0.892^{2}}{2(9.81)} \text{ m} = 0.0405 \text{ m}$
 $v_{B} = \frac{Q}{A_{B}} = \frac{0.015}{1.905 \times 10^{-3}} = 7.87 \text{ m/s}; \frac{v_{B}^{2}}{2g} = \frac{(7.87)^{2}}{2(9.81)} \text{ m} = 3.16 \text{ m}$
 $N_{R_{A}} = \frac{v_{A}D_{A}}{v} = \frac{(0.892)(0.1463)}{2.12 \times 10^{-5}} = 6.15 \times 10^{3}; D/\varepsilon = \frac{0.1463}{4.6 \times 10^{-5}} = 3180; f_{A} = 0.035$
 $N_{R_{B}} = \frac{v_{B}D_{B}}{v} = \frac{(7.87)(0.0493)}{2.12 \times 10^{-5}} = 1.83 \times 10^{4}; D/\varepsilon = \frac{0.0493}{4.6 \times 10^{-5}} = 1072; f_{B} = 0.028$
 $f_{TB} = 0.019$
 $h_{L} = f_{A} \frac{180}{0.1463} (0.0405) + 0.37(3.16) + 2(20)(f_{TB})(3.16) + f_{B} \frac{8}{0.0493}}{(3.16)}$
Friction 6-in Contr. Elbows Friction 2-in
Where $D_{1}/D_{2} = 0.1463/0.0493 = 2.97; K = 0.37, \text{ Table 10.3}$
 $h_{L} = 19.68 \text{ m}$
 $p_{A} = 12.5 \text{ MPa} + \frac{8.80 \text{ kN}}{\text{m}^{2}} [4.5 + 3.16 - 0.0405 + 19.68]\text{m} = 12.5 \text{ MPa} + 240 \text{ kPa}$

11.5 **Class I;**
$$\frac{p_A}{\gamma} + z_A + \frac{v_A^2}{2g} - h_L = \frac{p_B}{\gamma} + z_B + \frac{v_B^2}{2g}$$
,
Then $p_A = p_B + \gamma_o \left[(z_A - z_B) + \frac{v_B^2 - v_A^2}{2g} + h_L \right]$
 $v_A = \frac{Q}{A_A} = \frac{0.015 \text{ m}^3/\text{s}}{1.682 \times 10^{-2} \text{ m}^2} = 0.892 \text{ m/s}; \frac{v_A^2}{2g} = \frac{0.892^2}{2(9.81)} \text{ m} = 0.0405 \text{ m}$
 $v_B = \frac{Q}{A_B} = \frac{0.015}{1.905 \times 10^{-3}} = 7.87 \text{ m/s}; \frac{v_B^2}{2g} = \frac{(7.87)^2}{2(9.81)} \text{ m} = 3.16 \text{ m}$
 $N_{R_A} = \frac{v_A D_A}{v} = \frac{(0.892)(0.1463)}{2.12 \times 10^{-5}} = 6.15 \times 10^3; D/\varepsilon = \frac{0.1463}{4.6 \times 10^{-5}} = 3180; f_A = 0.035$
 $N_{R_B} = \frac{v_B D_B}{v} = \frac{(7.87)(0.0493)}{2.12 \times 10^{-5}} = 1.83 \times 10^4; D/\varepsilon = \frac{0.0493}{4.6 \times 10^{-5}} = 1072; f_B = 0.028$
 $f_{TB} = 0.019$
 $h_L = f_A \frac{180}{0.1463} (0.0405) + 0.37(3.16) + 2(20)(f_{TB})(3.16) + f_B \frac{8}{0.0493} (3.16)$
Friction 6-in Contr. Elbows Friction 2-in
Where $D_1/D_2 = 0.1463/0.0493 = 2.97; K = 0.37$, Table 10.3
 $h_L = 19.68 \text{ m}$
 $p_A = 12.5 \text{ MPa} + \frac{8.80 \text{ kN}}{\text{m}^2} [4.5 + 3.16 - 0.0405 + 19.68]\text{m} = 12.5 \text{ MPa} + 240 \text{ kPa}$

11.6 Class I

Pts. 1 and 2 at reservoir surfaces: $p_1 = p_2 = 0$; $v_1 = v_2 = 0$ $\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}$; $z_1 - z_2 = h_L$ = sum of 8 losses Water at 10 C; $v = 1.30 \times 10^{-6} \text{ m}^2/\text{s}$ **3-in pipe:** $v_3 = \frac{Q}{A_3} = 5.37 \text{ m/s}$: $\frac{v_3^2}{2g} = 1.47 \text{ m}$: $N_{R_3} = \frac{v_3 D_3}{v} = 3.48 \times 10^5$ $D_3/\varepsilon = 0.0843/1.2 \times 10^{-4} = 703; f_3 = 0.022; F_{T3} = 0.0215$ **6-in pipe:** $v_6 = \frac{Q}{A_6} = 1.57 \text{ m/s}$: $\frac{v_6^2}{2g} = 0.126 \text{ m}; N_{R_6} = \frac{v_6 D_6}{v} = 1.88 \times 10^5$ $D_6/\varepsilon = 0.1560/1.2 \times 10^{-4} = 1300; f_6 = 0.0205; f_{T6} = 0.0185$ $h_L = 1.0 \frac{v_3^2}{2g} + f_3 \frac{100}{0.0843} \frac{v_3^2}{2g} + 2(30) f_{T3} \frac{v_3^2}{2g} + 160 f_{T3} \frac{v_3^2}{2g} + 0.43 \frac{v_3^2}{2g} + f_6 \frac{300}{0.1560} \frac{v_6^2}{2g}$ Entr. Friction 3-in Elbows 3-in Gate valve Enl. Friction 6-in $+ 2(30) f_{T6} \frac{v_6^2}{2g} + 1.0 \frac{v_6^2}{2g}$ Elbows 6-in Exit $z_1 - z_2 = \sum h_L = 1.47 + 38.4 + 1.90 + 5.06 + 0.63 + 4.97 + 0.140 + 0.126$ $z_1 - z_2 = 52.7 \text{ m}$

APPLIED FLUID MECHANICS		II-A & II-B US: CLASS II SERIES SYSTEMS		
Objective: Volume flow rate	e Met	hod II-A: No minor losses		
Problem 11.13 (a)	Use	es Equation 11-3 to find maximum allowable volume flow rate		
Figure 11.18	to n	aintain desired pressure at point 2 for a given pressure at point 1		
System Data: US	Customary	Units		
Pressure at point 1 =	<i>20</i> psig	g Elevation at point 1 = 0 ft		
Pressure at point 2 =	0 psig	g Elevation at point 2 = 18 ft		
Energy loss: <i>h_L</i> =	<i>28.45</i> Ft			
<i>Fluid Properties:</i> Tu	rpentine at 77	7F May need to compute: $v = \eta/\rho$		
Specific weight =	62.00 lb/f	ť ³ Kinematic viscosity = 7.37E-06 fť ² /s		
Pipe data: Smooth alumine	um tube			
Diameter: D =	0.417 ft			
Wall roughness: ε =	1.00E-08 ft			
Length: L =	20 ft	Results: Maximum values		
Area: A =	<i>0.00137</i> ft ²	Volume flow rate: Q = 0.0194 ft ³ /s Using Eq. 11-3		
<i>D/</i> ε =	4170000	Velocity: v = 14.23 ft/s		

CLASS II SERIES SYSTEMS			Volume flow rate: Q =	0.01107 ft ³ /s
Method II-B: Use results of Method IIA;			Given: Pressure p_1 =	20 psig
Include minor losses;			Pressure p_2 =	0.00 psig
then pressure at Point 2 is	computed		NOTE: Should be >	0 psig
Additional Pipe Data:			Adjust estimate for Q un	p_2
L/D =	480		is equal or greater than	desired.
Flow Velocity =	8.11 f	ˈt/s	Velocity at point 1 =	8.11 ft/s > If velocity is in pipe:
Velocity head =	1.020 f	ťt	Velocity at point 2 =	32.42 ft/s > Enter "=B24"
Reynolds No. =	4.59E+04		Vel. head at point 1 =	1.02 ft
Friction factor: f =	0.0212		Vel. head at point 2 =	16.32 ft
Energy losses in Pipe:	K	Qty.		
Pipe: $K_1 = f(L/D) =$	10.15	1	Energy loss $h_{L1} =$	10.36 ft Friction
Bend: K ₂ =	0.34	1	Energy loss $h_{L2} =$	0.35 ft $f_T = 0.01$ Assumed
*Nozzle: K ₃ =	2.40	1	Energy loss $h_{L3} =$	2.45 ft
Element 4: K ₄ =	0.00	1	Energy loss $h_{L4} =$	0.00 ft
Element 5: K ₅ =	0.00	1	Energy loss $h_{L5} =$	0.00 ft
Element 6: K_6 =	0.00	1	Energy loss $h_{L6} =$	0.00 ft
Element 7: K_7 =	0.00	1	Energy loss $h_{L7} =$	0.00 ft
Element 8: K ₈ =	0.00	1	Energy loss h _{L8} =	0.00 ft
	L		Total energy loss $h_{Ltot} =$	13.15 ft

*Nozzle K₃ restated in terms of velocity head in pipe rather than outlet velocity head. *K₃ = 0.15(v_2/v_1)² = 0.15(4)² = 2.40

Nozzle Velocity: $v_N = v_p(A_p/A_N) = v_p(D_p/D_N)^2 = 4.0v_p = 4.0(8.11 \text{ ft/s}) = 32.44 \text{ ft/s}$

APPLIED FLUID MECHANIC	S	II-A & II-B US: CLASS II SERIES SYSTEMS		
Objective: Volume flow rate	Me	ethod II-A: No minor losses		
Problem 11.13 (b)	Us	es Equation 11-3 to find maximum allowable volume flow rate		
Figure 11.18	to	naintain desired pressure at point 2 for a given pressure at point 1		
System Data: US	Customary	/ Units		
Pressure at point 1 =	<i>80</i> ps	ig Elevation at point 1 = 0 ft		
Pressure at point 2 =	<i>0</i> ps	ig Elevation at point 2 = 18 ft		
Energy loss: $h_L =$	<i>167.81</i> ft			
Fluid Properties: Tur	pentine at 7	77F May need to compute: $v = \eta/\rho$		
Specific weight =	62.00 lb/	/ft ³ Kinematic viscosity = 7.37E-06 ft^2/s		
Pipe data: Smooth aluminu	m tube			
Diameter: D =	0.417 ft			
Wall roughness: $\varepsilon = 1$.00E-08 ft			
Length: L =	20 ft	Results: Maximum values		
Area: A =	0.00137 ft ²	Volume flow rate: Q = 0.0522 ft ³ /s Using Eq. 11-3		
D/ε = 4	4170000	Velocity: v = 38.20 ft/s		

CLASS II SERIES SYSTEMS			Volume flow rate: Q =	0.02781 ft ³ /s
Method II-B: Use results of Method IIA;			Given: Pressure p_1 =	80 psig
Include minor losses;			Pressure p_2 =	0.01 psig
then pressure at Point 2 is	computed		NOTE: Should be >	0 psig
Additional Pipe Data:			Adjust estimate for Q un	p_2
L/D =	480		is equal or greater than	desired.
Flow Velocity =	20.36 f	ˈt/s	Velocity at point 1 =	20.36 ft/s > If velocity is in pipe:
Velocity head =	6.439 f	ťt	Velocity at point 2 =	81.45 ft/s > Enter "=B24"
Reynolds No. =	1.15E+05		Vel. head at point 1 =	6.44 ft
Friction factor: f =	0.0173		Vel. head at point 2 =	103.02 ft
Energy losses in Pipe:	K	Qty.		
Pipe: $K_1 = f(L/D) =$	8.32	1	Energy loss $h_{L1} =$	53.57 ft Friction
Bend: K ₂ =	0.34	1	Energy loss $h_{L2} =$	2.19 ft $f_T = 0.01$ Assumed
*Nozzle: K ₃ =	2.40	1	Energy loss $h_{L3} =$	15.45 ft
Element 4: K ₄ =	0.00	1	Energy loss $h_{L4} =$	0.00 ft
Element 5: K ₅ =	0.00	1	Energy loss $h_{L5} =$	0.00 ft
Element 6: K_6 =	0.00	1	Energy loss $h_{L6} =$	0.00 ft
Element 7: K_7 =	0.00	1	Energy loss $h_{L7} =$	0.00 ft
Element 8: K ₈ =	0.00	1	Energy loss $h_{L8} =$	0.00 ft
			Total energy loss $h_{Ltot} =$	71.21 ft

*Nozzle K_3 restated in terms of velocity head in pipe rather than outlet velocity head. * $K_3 = 0.15(v_2/v_1)^2 = 0.15(4)^2 = 2.40$

Nozzle Velocity: $v_N = v_p(A_p/A_N) = v_p(D_p/D_N)^2 = 4.0v_p = 4.0(20.36 \text{ ft/s}) = 32.44 \text{ ft/s}$

11.14 **Class II** Pt. 1 at surface of tank A; Pt. 2 in stream outside pipe. $v_1 = 0, p_2 = 0$ $\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}; \frac{p_1}{\gamma} + (z_1 - z_2) = \frac{v_2^2}{2g} + h_L$ $\frac{150 \text{ kN/m}^2}{8.07 \text{ kN/m}^3} - 5 \text{ m} = \boxed{13.59 \text{ m} = \frac{v_2^2}{2g} + h_L} \qquad \bigcirc \qquad \text{Method IIC}$ $h_L = 0.50 \frac{v_2^2}{2g} + 160 f_T \frac{v_2^2}{2g} + 2(18) f_T \frac{v_2^2}{2g} + f \frac{30 \text{ mm}}{0.0498 \text{ m}} \frac{v_2^2}{2g} = (2.46 + 602f) \frac{v_2^2}{2g}$ Entrance Valve Bends Friction $\downarrow r/D = \frac{300 \text{ mm}}{49.8 \text{ mm}} = 6.02 \rightarrow \frac{L_e}{D} = 18 \text{ (Fig. 10.23)}$ $D/\varepsilon = \frac{0.0498 \text{ m}}{1.5 \times 10^{-6} \text{ m}} = 33200$ $f_T = 0.010 \text{ (Approx.)}$

In Eq. I:

13.59 m =
$$\frac{v_2^2}{2g}$$
 + (2.46 + 602 f) $\frac{v_2^2}{2g}$ = (3.46 + 602 f) $\frac{v_2^2}{2g}$
 $v = \sqrt{\frac{2g(13.59 \text{ m})}{3.46 + 602 f}} = \sqrt{\frac{2(9.81)(13.59)}{3.46 + 602 f}} = \sqrt{\frac{266.6}{3.46 + 602 f}}$

Try
$$f = 0.02$$

 $v = \sqrt{\frac{266.6}{3.46 + 602(0.02)}} = 4.15 \text{ m/s}; N_R = \frac{vD\rho}{\eta} = \frac{(4.15)(0.0498)(823)}{1.64 \times 10^{-3}} = 1.04 \times 10^5$
New $f = 0.018; v = 4.32 \text{ m/s}; N_R = 1.08 \times 10^5; \text{New } f = 0.018 \text{ No change}$
 $Q = Av = (1.945 \times 10^{-3} \text{ m}^2)(4.32 \text{ m/s}) = 8.40 \times 10^{-3} \text{ m}^3/\text{s}$

11.15 **Class II with 2 pipes:** Pts. A and B at tank surfaces. **Method IIC**

$$\frac{p_{A}}{\gamma} + z_{A} + \frac{v_{A}^{2}}{2g} - h_{L} = \frac{p_{B}}{\gamma} + z_{B} + \frac{v_{B}^{2}}{2g} : z_{A} - z_{B} = h_{L} = 10 \text{ m}: \begin{array}{l} p_{A} = p_{B} = 0 \\ v_{A} = v_{B} = 0 \end{array}$$

$$h_{L} = 1.0 \frac{v_{3}^{2}}{2g} + 2(30) f_{3T} \frac{v_{3}^{2}}{2g} + f_{3} \frac{55}{0.08432} \frac{v_{3}^{2}}{2g} + 0.45 \frac{v_{3}^{2}}{2g} \end{array}$$
Based on 3-in pipe; $f_{3T} = 0.022$
Entrance Elbows Friction Enlarge. $\frac{D_{2}}{D_{1}} = \frac{0.156}{0.08433} = 1.85$

$$+ f_{6} \frac{30}{0.156} \frac{v_{6}^{2}}{2g} + 30 f_{6T} \frac{v_{6}^{2}}{2g} + 45 f_{6T} \frac{v_{6}^{2}}{2g} + 1.0 \frac{v_{6}^{2}}{2g} \end{aligned}$$
Based on 6-in pipe; $f_{6T} = 0.019$
Friction Elbow Valve Exit
$$h_{L} = (2.77 + 652f_{3})\frac{v_{3}^{2}}{2g} + (2.43 + 192f_{6})\frac{v_{6}^{2}}{2g}$$

But
$$v_3 = v_6 \frac{A_6}{A_3} = v_6 \left(\frac{D_6}{D_3}\right)^2 = v_6 \left(\frac{0.156}{0.0843}\right)^2 = 3.42 v_6; v_3^2 = 11.73 v_6^2$$

SERIES PIPE LINE SYSTEMS

$$h_L = (2.77 + 652f_3)\frac{11.73v_6^2}{2g} + (2.43 + 192f_6)\frac{v_6^2}{2g} = (34.9 + 7646f_3 + 192f_6)\frac{v_6^2}{2g}$$

Solve for v_6

$$\begin{split} \upsilon_6 &= \sqrt{\frac{2gh_L}{(34.9+7646f_3+192f_6)}} = \sqrt{\frac{2(9.81)(10)}{34.9+7646f_3+192f_6}} \\ &= \sqrt{\frac{196.2}{34.6+7646f_3+192f_6}} \end{split}$$

Iterate for both f_3 and f_6 : D = 0.0843 m

_

$$\frac{D_3}{\varepsilon} = \frac{0.0843 \text{ m}}{1.2 \times 10^{-4} \text{ m}} = 703: N_{R_3} = \frac{v_3 D_3}{v} = \frac{v_3 (0.0843)}{6.56 \times 10^{-7}} = 1.29 \times 10^5 (v_3)$$
$$\frac{D_6}{\varepsilon} = \frac{0.1560}{1.2 \times 10^{-4}} = 1300: N_{R_6} = \frac{v_6 D_6}{v} = \frac{v_6 (0.156)}{6.56 \times 10^{-7}} = 2.38 \times 10^5 (v_6)$$

Try
$$f_3 = f_6 = 0.02$$

 $v_6 = \sqrt{\frac{196.2}{34.9 + 7646(0.02) + 192(0.02)}} = 1.012 \text{ m/s}$

$$v_3 = 3.42 v_6 = 3.46 \text{ m/s}$$

 $N_{R_3} = 1.29 \times 10^5 (3.46) = 4.46 \times 10^5 \rightarrow \text{New} f_3 = 0.0195$
 $N_{R_6} = 2.38 \times 10^5 (1.012) = 2.41 \times 10^5 \rightarrow \text{New} f_6 = 0.020$

$$\nu_6 = \sqrt{\frac{196.2}{34.9 + 7646(0.0195) + 192(0.02)}} = 1.022 \text{ m/s}$$

$$\nu_3 = 3.42 \nu_6 = 3.50 \text{ m/s}$$

$$N_{R_3} = 1.29 \times 10^5 (3.50) = 4.20 \times 10^5 \rightarrow f_3 = 0.0195 \text{ No change}$$

$$N_{R_6} = 2.38 \times 10^5 (1.02) = 2.43 \times 10^5 \rightarrow f_6 = 0.020 \text{ No change}$$

$$Q = A_6 v_6 = \frac{\pi (0.156 \text{ m})^2}{4} \times 1.02 \text{ m/s} = 1.95 \times 10^{-2} \text{ m}^3/\text{s}$$

Practice problems for any class

11.21 **Class I** Pt. 1 at tank surface, Pt. 2 in stream outside pipe:
$$p_1 = p_2 = 0; v_1 = 0$$

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}; \quad \boxed{z_1 - z_2 = \frac{v_2^2}{2g} + h_L} \quad \textcircled{O}$$

$$v_2 = \frac{Q}{A_2} = \frac{1500 \text{ L/min}}{6.38 \times 10^{-3} \text{m}^2} \frac{1 \text{ m}^3/\text{s}}{60000 \text{ L/min}} = 3.92 \text{ m/s}; \quad \frac{v_2^2}{2g} = \frac{(3.92)^2}{2(9.81)} = 0.782 \text{ m}$$

$$f_T = 0.018$$

$$h_L = 0.5 \frac{v_2^2}{2g} + f_T (160) \frac{v_2^2}{2g} + f_T (30) \frac{v_2^2}{2g} = \frac{v_2^2}{2g} [0.5 + 190 f_T] = 0.782 [0.5 + 190(0.018)]$$

$$= 3.07 \text{ m}$$
In Eq. \textcircled{O}

$$z_1 - z_2 = \frac{v_2^2}{2g} + h_L = 0.782 + 3.07 = 3.85 \text{ m}$$
11.22 **Class I** Pt. 1 at collector tank surface. Pt. 2 at pump inlet. $p_1 = 0, v_1 = 0$

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}; \quad \boxed{p_2 = \gamma \left[(z_1 - z_2) - h_L - \frac{v_2^2}{2g}\right]} \end{gathered}$$

22 **Class I** Pt. 1 at collector tank surface. Pt. 2 at pump inlet.
$$p_1 = 0, v_1 = 0$$

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L = \frac{p_2}{\gamma} + z_2 + \frac{v_2^2}{2g}; \qquad p_2 = \gamma \left[(z_1 - z_2) - h_L - \frac{v_2^2}{2g} \right] \bigcirc$$

$$Q = 30 \text{ gal/min} \times \frac{1 \text{ ft}^3/\text{s}}{449 \text{ gal/min}} 1 = 0.0668 \text{ ft}^3/\text{s} \qquad f_T = 0.019 \text{ for } 2\text{-in pipe}$$

$$v_2 = \frac{Q}{A_2} = \frac{0.0668 \text{ ft}^3/\text{s}}{0.02333 \text{ ft}^2} = 2.86 \text{ ft/s}; \frac{v_2^2}{2g} = \frac{(2.86)^2}{2(32.2)} = 0.127 \text{ ft}$$

$$h_L = 0.5 \frac{v_2^2}{2g} + 1.85 \frac{v_2^2}{2g} + f \frac{10.0 \text{ ft}}{0.1723 \text{ ft}} \frac{v_2^2}{2g} + f_T(8) \frac{v_2^2}{2g} = \frac{v_2^2}{2g} (2.50 + 58.0 f)$$
Entrance Filter Friction Valve
$$N_R = \frac{vD\rho}{\eta} = \frac{(2.86)(0.1723)(0.92)(1.94)}{3.6 \times 10^{-5}} = 2.45 \times 10^4 : \frac{D}{\varepsilon} = \frac{0.1723}{1.5 \times 10^{-4}} = 1149$$

$$f = 0.0265$$

$$h_L = (0.127 \text{ ft})[2.50 + 58.0(0.0265)] = 0.513 \text{ ft}$$
In Eq. \bigcirc :
$$p_2 = (0.92) \frac{62.4 \text{ lb}}{\text{ft}^3} [3.0 - 0.513 - 0.127] \frac{\text{ft ft}^2}{144 \text{ in}^2} = 0.94 \text{ psig}$$

11.23 **Class I** Pt. 1 at collector tank surface; Pt. 3 at upper tank surface.
$$p_1 = p_3 = 0$$
, $v_1 = v_3 = 0$

$$\frac{p_1}{\gamma} + z_1 + \frac{v_1^2}{2g} - h_L + h_A = \frac{p_3}{\gamma} + z_3 + \frac{v_3^2}{2g}$$
 $h_A = (z_3 - z_1) + h_L = 19.0 \text{ ft} + h_L$
 $h_L = h_{L_{stact.}} + h_{L_{stach.}} = 0.513 \text{ ft} + f_{dT} (100) \frac{v_d^2}{2g} + f_d \frac{18 \text{ ft}}{0.115 \text{ ft}} \frac{v_2^2}{2g} + 1.0 \frac{v_d^2}{2g}$

$$\overline{\text{From Prob. 11.22}} \quad \text{Ch. valve} \quad \text{Friction} \quad \text{Exit}$$
 $v_d = \frac{Q}{A_d} = \frac{0.0668 \text{ ft}^3/s}{0.01039 \text{ ft}^2} = 6.43 \text{ ft/s:} \quad \frac{v_d^3}{2g} = \frac{(6.43)^2}{2(32.2)} = 0.642 \text{ ft}$
 $N_{R_d} = \frac{v_d D\rho}{\eta} = \frac{(6.43)(0.115)(0.92)(1.94)}{3.6 \times 10^{-5}} = 3.67 \times 10^4$:
$$\frac{D}{\varepsilon} = \frac{0.115}{1.5 \times 10^{-4}} = 767 \rightarrow f = 0.0265; \ f_{dT} = 0.022$$
 $h_L = 0.513 \text{ ft} + (0.022)(100)(0.642) + (0.0265)(157)(0.642) + 1.0(0.642) = 5.24 \text{ ft}$
 $h_A = 19.0 \text{ ft} + h_L = 19.0 + 5.24 = 24.24 \text{ ft}$
Power $= P_A = h_A \gamma Q = (24.24 \text{ ft})(0.92) \left(\frac{62.4 \text{ }lb}{\text{ ft}^3}\right) \left(\frac{0.0668 \text{ ft}^3}{\text{ s}}\right) \frac{1 \text{ hp}}{550 \text{ ft-lb/s}} 2 = 0.169 \text{ hp}$

APPLIED FLUID MECHANICS		III-A & III-B US: CLASS III SEF	RIES SYSTEMS	
Objective: Minimum pipe dia	meter	Method III-A: Uses Equation 11-8	to compute the	
Problem 11.24		minimum size of pipe of a given length		
Figure 11.24 – Return System	from upper tank	that will flow a given volume flow rate of fluid		
System Data: SI Met	ric Units	with a limited pressure drop. (No minor losses)		
Pressure at point 1 =	0 psig	Fluid Properties: Coolant – Gl	iven properties	
Pressure at point 2 =	<i>0</i> psig	Specific weight =	<i>57.41</i> lb/ft ³	
Elevation at point 1 =	<i>9</i> ft	Kinematic Viscosity =	<i>2.02E-05</i> ft ² /s	
Elevation at point 2 =	<i>O</i> ft	Intermediate Results in	Eq. 11-8:	
Allowable Energy Loss: $h_{L=}$	12.00 ft	$L/gh_L =$	0.134576	
Volume flow rate: Q =	<i>06682</i> ft ³ /s	Argument in bracket:	1.37E-09	
Length of pipe: L = 39 ft		Final Minimum Diam	eter:	
Pipe wall roughness: $\varepsilon = 1.50E-04$ ft		Minimum diameter: D =	0.1059ft	

CLASS III SERIES SYSTEMS			Specified pipe diameter: D =	0.115 ft-min std sz	
Method III-B: Use results of Method III-A;			5-in Sch 40 steel pipe		
Specify actual diameter; Include minor losses;			If velocity is in the pipe, enter "=B23" for value		
then pressure at Point 2 is computed.			Velocity at point 1 =	<i>0.00</i> ft/s	
Additional Pipe Data:			Velocity at point 2 =	<i>6.43</i> ft/s	
Flow area: A =	0.01039	ft ²	Vel. head at point 1 =	0.000 ft	
Relative roughness: D/ϵ =	767		Vel. head at point 2 =	0.643 ft	
L/D =	339		Results:		
Flow Velocity =	6.43	ft/s	Given pressure at point 1 =	0 psig	
Velocity head =	0.643	ft	Desired pressure at point 2 =	0 psig	
Reynolds No. =	Reynolds No. = 3.67E+04		Actual pressure at point 2 =	0.49 psig	
Friction factor: $f = 0.0261$		(Compare actual with desired	pressure at point 2)		
Energy losses in Pipe:	K	Qty.			
Pipe Friction: $K_1 = f(L/D) =$	8.84	1	Energy loss $h_{L1} =$	5.68 ft	
Entrance-Square edge: K_2 =	0.50	1	Energy loss h_{L2} =	0.32 ft	
Elbows: K ₃ =	0.66	2	Energy loss $h_{L3} =$	0.85 ft $f_T = 0.022$	
Tee-flow thru run: $K_4 =$	0.44	1	Energy loss $h_{L4} =$	0.28 ft $f_T = 0.022$	
Element 5: K ₅ =	0.00	1	Energy loss $h_{L5} =$	0.00 ft	
Element 6: K ₆ =	0.00	1	Energy loss $h_{L6} =$	0.00 ft	
Element 7: K ₇ =	0.00	1	Energy loss $h_{L7} =$	0.00 ft	
Element 8: K ₈ = 0.00 1		Energy loss <i>h_{L8}</i> =	0.00 ft		
			Total energy loss $h_{Ltot} =$	7.13 ft	

16.6
$$Q = A v = (2.95 \text{ in}^{2})(22.0 \text{ ft/s})(1 \text{ ft}^{2}/144 \text{ in}^{2})$$

$$= 0.451 \text{ ft}^{3}/\text{s}$$

$$R_{x} = \rho Q \left(v_{2_{x}} - v_{1_{x}} \right) = \rho Q \left[v_{2} \cos 50^{\circ} - (-v_{1}) \right]$$

$$R_{x} = \rho Q \left[v_{2} \cos 50^{\circ} + v_{1} \right]; \text{ but } v_{2} = v_{1}$$

$$R_{x} = \rho Q v_{1} \left[\cos 50^{\circ} + 1 \right]$$

$$R_{x} = \frac{1.88 \text{ lb} \cdot \text{s}^{2}}{\text{ft}^{4}} \times \frac{0.451 \text{ ft}^{3}}{\text{s}} \times \frac{22.0 \text{ ft}}{\text{s}} \times 1.643$$

$$= 30.6 \text{ lb}$$

$$R_{y} = \rho Q \left(v_{2_{y}} - v_{1_{y}} \right) = \rho Q \left[v_{2} \sin 50^{\circ} - 0 \right] = (1.88)(0.451)(22 \sin 50^{\circ}) = 14.3 \text{ lb}$$

16.11
$$Q = 100 \text{ gal/min} \times \frac{1 \text{ ft}^3/\text{s}}{449 \text{ gal/min}} = 0.223 \text{ ft}^3/\text{s}: \quad v_1 = \frac{Q}{A} = \frac{0.223 \text{ ft}^3/\text{s}}{0.0060 \text{ ft}^2} = 37.1 \text{ ft/s}$$
Assume all fluid strikes vane and is deflected perpendicular to incoming stream.

$$R_x = \rho Q \left(v_{2_x} - v_{1_x} \right) = \rho Q [0 - (-v_1)] = \rho Q v_1$$

$$R_x = \frac{1.94 \text{ lb} \cdot \text{s}^2}{\text{ft}^4} \times \frac{0.223 \text{ ft}^3}{\text{s}} \times \frac{37.1 \text{ ft}}{\text{s}} = 16.0 \text{ lb}$$

$$R_x \text{ is force exerted by vane on water}$$

$$R_x' \text{ is force exerted by water on vane}$$

$$\Sigma M_A = 0 = F_S(0.5 \text{ in}) - R_x'(1.0 \text{ in})$$

$$F_S = R_x' \frac{1.0}{0.5} = 2R_x' = 2(16.0 \text{ lb}) = 32.0 \text{ lb}$$

16.20
$$Q = Av = (3.142 \times 10^{-2} \text{ m}^2)(30 \text{ m/s}) = 0.943 \text{ m}^3/\text{s}$$

a. **x-direction:**
 $R_x = \rho Q \left(v_{2_x} - v_{1_x} \right) = \rho Q (v_2 - (-v_1 \cos 15^\circ))$
 $R_x = \rho Q v (1 + \cos 15^\circ) = 1.966\rho Q v$
 $R_x = (1.966) \left(\frac{1000 \text{ kg}}{\text{m}^3} \right) \left(\frac{0.943 \text{ m}^3}{\text{s}} \right) \left(\frac{30 \text{ m}}{\text{s}} \right)$



 $R_x = 55.6 \times 10^3 \text{ kg·m/s}^2 = 55.6 \text{ kN} = \text{Force of car on water.} \leftarrow \text{Force on car} = 55.6 \text{ kN} \rightarrow$

y-direction:

$$R_{y} = \rho Q \left(v_{2y} - v_{1y} \right) = \rho Q (0 - (-v_{1} \sin 15^{\circ})) = \rho Q v \sin 15^{\circ}$$

$$R_{y} = (1000)(0.943)(30)(0.259) = 7.32 \times 10^{3} \text{ kg·m/s}^{2} = 7.32 \text{ kN} = \text{Force on water } \downarrow$$

Force on car = 7.32 kN \uparrow

b. Because the inlet jet acts at an angle to the *x*-*y* directions, we compute its components: $v_{1x} = v_1 \cos (15^\circ) = (30 \text{ m/s})(0.966) = 28.98 \text{ m/s}$: $v_{1y} = v_1 \sin (15^\circ) = 30 \text{ m/s})(0.259) = 7.76 \text{ m/s}$

Only v_{lx} is affected by the moving vane. Then $v_{elx} = v_{lx} - 12 \text{ m/s} = 16.98 \text{ m/s}.$ $v_{ely} = v_{ly} = 7.76 \text{ m/s}.$ The magnitude of the resultant effective velocity is: $|v_{ely}| = \sqrt{(16.98)^2 + (7.76)^2} = 18.67 \text{ m/s}$

The total effective mass flow rate into the vane, M_c , is,

 $M_e = \rho Q_e = \rho A v_{e1} = (1000 \text{ kg/m}^3)(3.142 \times 10^{-2} \text{ m}^2)(18.67 \text{ m/s}) = 586.6 \text{ kg/s}$ The velocity, v_{e1} , acts at an angle α , with respect to the horizontal, where $\alpha = \text{Tan}^{-1}(7.76)/16.98) = 24.58^{\circ}$

Only the component of v_{e1} acting parallel to the vane is maintained as the jet travels around the vane.

This component is computed using β , the difference between α and the angle of the vane inlet.

 $\beta = 24.58^{\circ} - 15^{\circ} = 9.58^{\circ}$

Then, $v_{e1(par)} = (v_{e1})\cos(9.58^\circ) = (18.67 \text{ m/s})(0.986) = 18.41 \text{ m/s}$ This velocity remains undiminished as the jet travels around the vane. Then $v_{e2} = 18.41$ m/s to the left.

Force in x-direction: $R_x = M_e(\Delta v_{ex}) = M_e(v_{e2x} - v_{e1x}) = (586.6 \text{ kg/s})[18.41 - (-16.98)]\text{m/s} = 20.76 \text{ kN}$

Force in y-direction: $R_y = M_e(\Delta v_{ey}) = M_e(v_{e2y} - v_{e1y}) = (586.6 \text{ kg/s})[0 - (-7.76)]\text{m/s} = 4.55 \text{ kN}$





Force in the *x*-direction: $R_x = M(\Delta v_x) = M(v_{2x} - v_{1x})$ = (1.105 kg/s)[12.5 - (-24.62)]m/s = **41.0** N Force in the *y*-direction: $R_y = M(\Delta v_y) = M(v_{2y} - v_{1y})$ = (1.105 kg/s)[21.65 - 4.34]m/s = **19.1** N

CHAPTER THIRTEEN

PUMP SELECTION AND APPLICATION

- 13.1 to 13.14: Answers to questions in text.
- 13.15 Affinity laws relate the manner in which capacity, head and power vary with either speed or impeller diameter.

13.16
$$Q_2 = Q_1 \frac{N_2}{N_1} = Q_1 \frac{0.5N_1}{N_1} = 0.5Q_1$$
: Capacity cut in half.

13.17
$$h_{a_2} = h_{a_1} \left(\frac{N_2}{N_1}\right)^2 = h_{a_1} \left(\frac{0.5N_1}{N_1}\right)^2 = 0.25h_{a_1} \colon h_a \text{ divided by 4.}$$

13.18
$$P_2 = P_1 \left(\frac{N_2}{N_1}\right)^3 = P_1 \left(\frac{0.5N_1}{N_1}\right)^3 = 0.125P_1$$
: *P* divided by 8.

13.19
$$Q_2 = Q_1 \frac{D_2}{D_1} = Q_1 \frac{0.75D_1}{D_1} = 0.75Q_1$$
: 25% reduction.

13.20
$$h_{a_2} = h_{a_1} \left(\frac{D_2}{D_1}\right)^2 = h_{a_1} \left(\frac{0.75D_1}{D_1}\right)^2 = 0.5625h_{a_1}$$
: 44% reduction.

13.21
$$P_2 = P_1 \left(\frac{D_2}{D_1}\right)^3 = P_1 \left(\frac{0.75D_1}{D_1}\right)^3 = 0.422P_1$$
: 58% reduction.

13.22 $1\frac{1}{2} \times 3$ 6 $\begin{bmatrix} & & & \\$

13.23
$$1\frac{1}{2} \times 3$$
 10

13.24
$$1\frac{1}{2} \times 3$$
 6

13.25 Q = 230 gal/min; P = 22 hp; e = 53%; $NPSH_R = 10.1$ ft

PUMP SELECTION AND APPLICATION

- 13.26 At $h_a = 248$ ft, $e_{max} = 57\%$: Q = 165 gal/min; P = 17.0 hp; $NPSH_R = 7.5$ ft
- 13.27 From Problem 13.26, $h_{a_1} = 248$ ft: Let $h_{a_2} = 1.15 h_{a_1} = 285$ ft Then $Q_2 = 65$ gal/min; $P_2 = 8.5$ hp; $e_2 = 44\%$; $NPSH_R = 5.5$ ft (approximate values)

	6 in	7 in	8 in	9 in	10 in
h_a	120 ft	195 ft	248 ft	320 ft	390 ft
Q	90 gal/min	130 gal/min	165 gal/min	210 gal/min	245 gal/min
$e_{\rm max}$	52%	55%	57%	58%	58.7%(Est)

13.29 $NPSH_R$ increases.

13.28

- 13.30 Throttling valves dissipate energy from fluid that was delivered by pump. When a lower speed is used to obtain a lower capacity, power required to drive pump decreases as the cube of the speed. Variable speed control is often more precise and it can be automatically controlled.
- 13.31 As fluid viscosity increases, capacity and efficiency decrease, power required increases.
- 13.32 Total capacity doubles.
- 13.33 The same capacity is delivered but the head capability increases to the sum of the ratings of the two pumps.
- 13.34 a. Rotary or 3500 rpm centrifugal
 - b. Rotary
 - c. Rotary
 - d. Reciprocating
 - e. Rotary or high speed centrifugal
 - f. 1750 rpm centrifugal
 - g. 1750 rpm centrifugal or mixed flow
 - h. Axial flow

13.35
$$Q = 350 \text{ gal/min}; H = 550 \text{ ft}; D = 12 \text{ in}; N = 3560 \text{ rpm}$$

 $N_s = \frac{N\sqrt{Q}}{H^{3/4}} = \frac{3560\sqrt{350}}{(550)^{0.75}} = 586; D_s = \frac{DH^{1/4}}{\sqrt{Q}} = \frac{(12)(550)^{0.25}}{\sqrt{350}} = 3.1$

Point in Fig. 13.53 lies in radial flow centrifugal region.

13.36
$$Q = 2525$$
 gal/min; $H = 200$ ft; $D = 15$ in; $N = 1780$ rpm
 $N_s = \frac{N\sqrt{Q}}{H^{3/4}} = \frac{1780\sqrt{2525}}{(200)^{0.75}} = 1682; D_s = \frac{DH^{1/4}}{\sqrt{Q}} = \frac{15(200)^{0.25}}{\sqrt{2525}} = 1.12$

Point in Figure 13.34 lies in radial flow centrifugal region.

13.37
$$N_s = \frac{N\sqrt{Q}}{H^{3/4}}$$
: $N = \frac{N_s H^{3/4}}{\sqrt{Q}} = \frac{(5000)(40)^{0.75}}{\sqrt{10000}} = 795 \text{ rpm}$