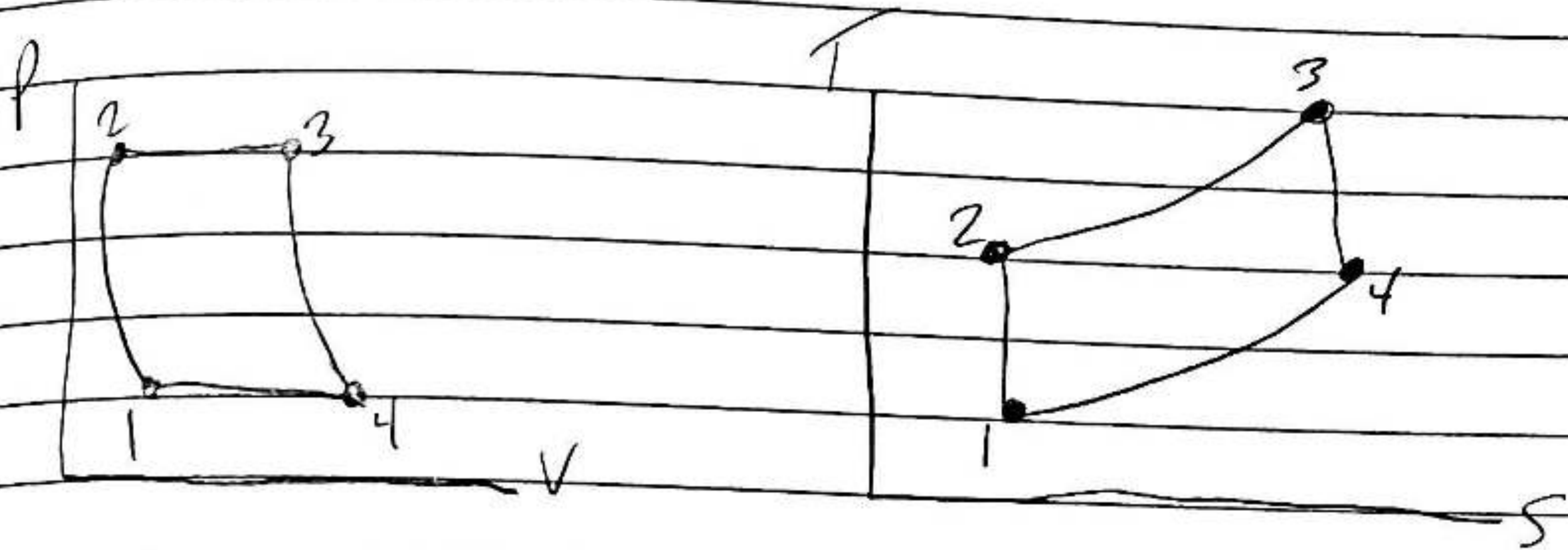


ROY SHEPARD MET 331 HW 1.4 88, 99, 107, 119, 121

Problem 88



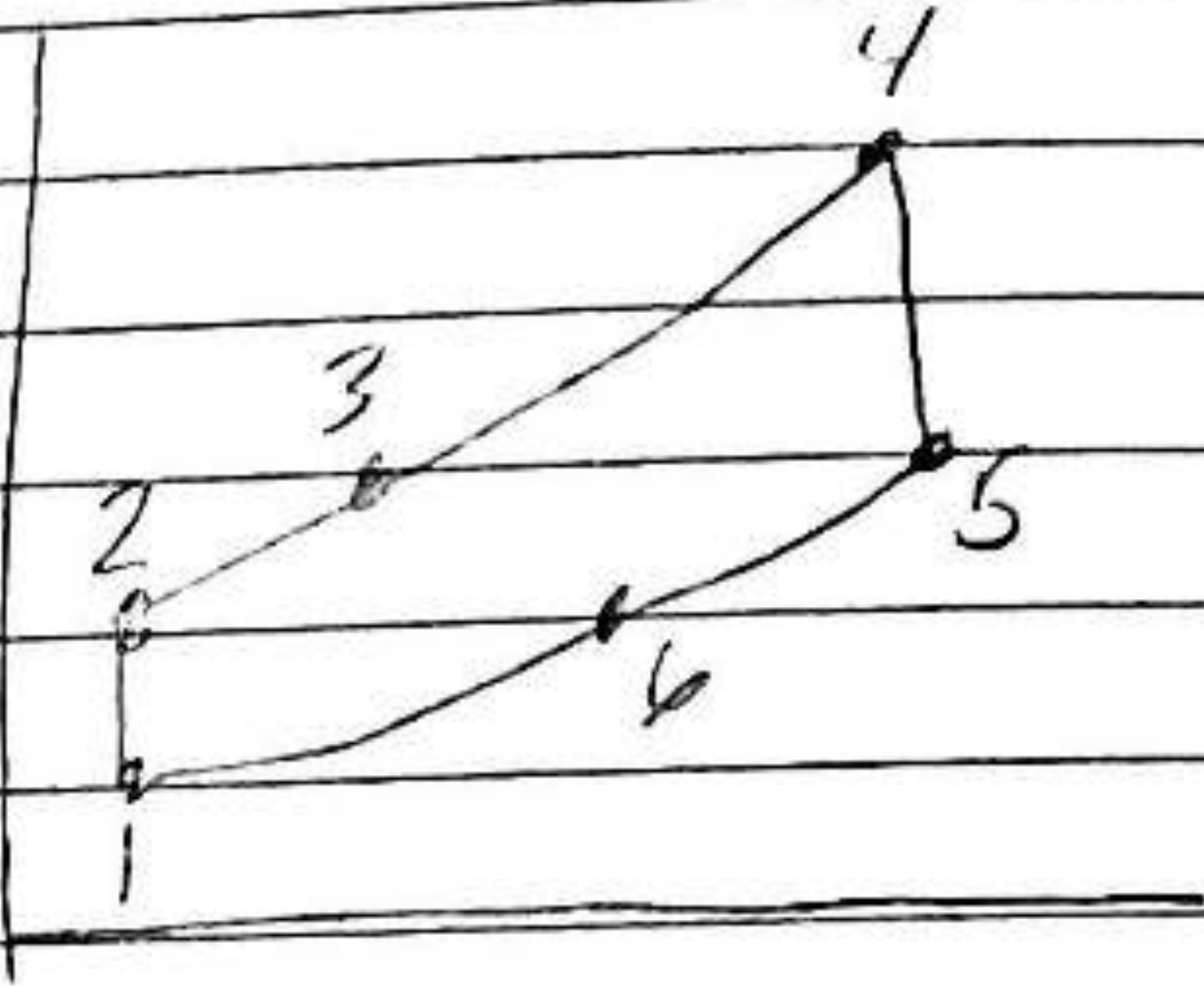
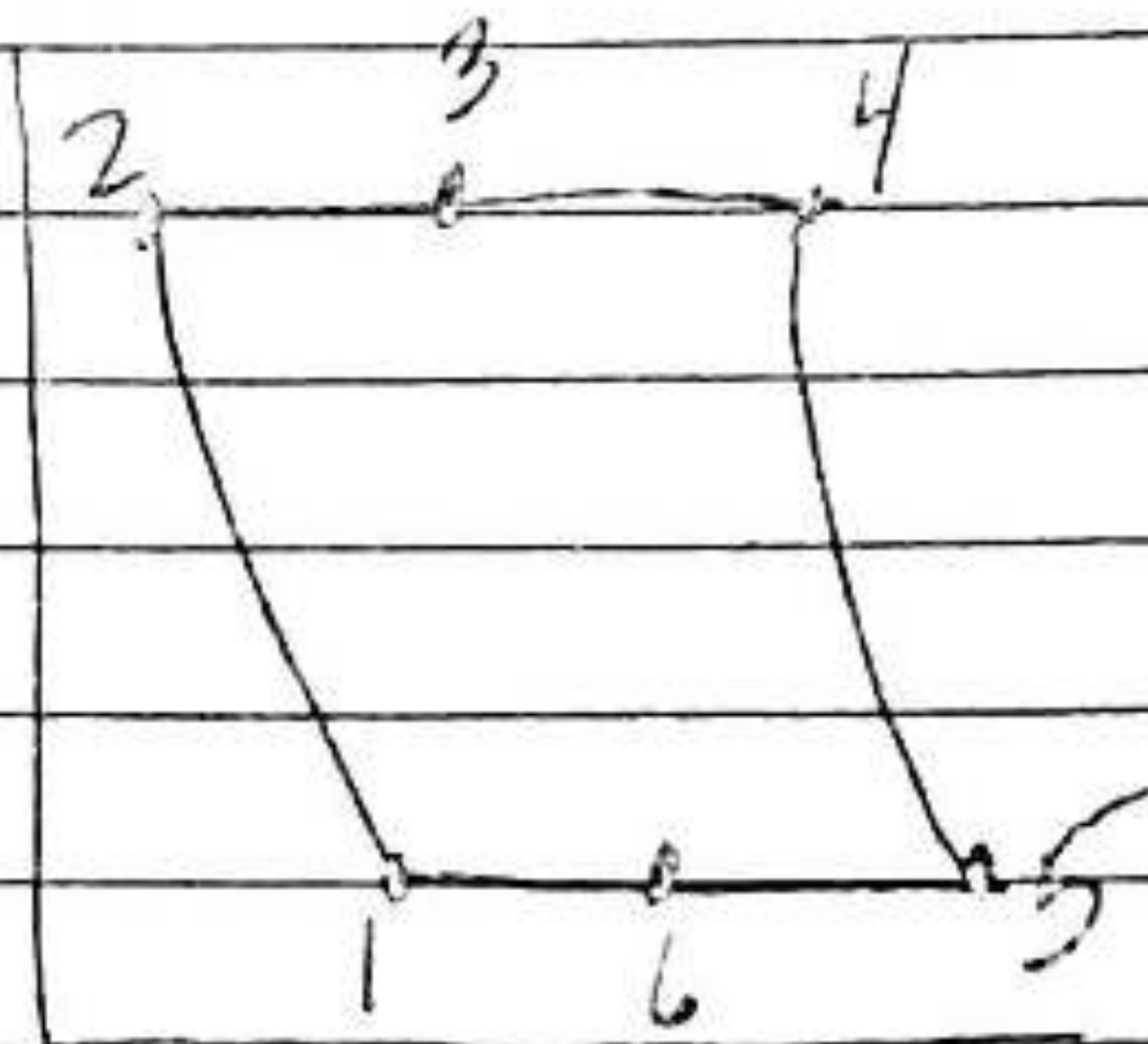
$$\gamma = 1.4$$

$$Q_{in} = 500 \text{ kW}$$

$$\eta = 1 - \frac{1}{r_p^{(k-1)/k}} = 1 - \frac{1}{10^{(1.4-1)/1.4}} = [0.482]$$

$$W = \eta Q_{in} = 0.482 \cdot 500 = \boxed{241 \text{ kW}}$$

Problem 99



$$\begin{aligned} \textcircled{1} \quad P_1 &= 100 \text{ kPa} & \frac{T_2}{T_1} &= \left(\frac{P_2}{P_1} \right)^{\frac{k-1}{k}} & T_2 &= 303(10)^{\frac{0.4}{1.4}} = 585 \text{ K} \\ T_1 &= 303 \text{ K} \end{aligned}$$

$$\begin{aligned} \textcircled{2} \quad P_2 &= 1000 \text{ kPa} \\ T_2 &= 585 \text{ K} \end{aligned}$$

$$\begin{aligned} \textcircled{3} \quad P_3 &= 1000 \text{ kPa} & T_3 &= T_2 - 10 = 585 - 10 = 575 \text{ K} \\ T_3 &= 575 \text{ K} \end{aligned}$$

$$\begin{aligned} \textcircled{4} \quad P_4 &= 1000 \text{ kPa} & \frac{T_4}{T_5} &= \left(\frac{P_4}{P_5} \right)^{\frac{k-1}{k}} = 1073 \left(\frac{1}{10} \right)^{\frac{0.4}{1.4}} = 556 \text{ K} \\ T_4 &= 1073 \text{ K} \end{aligned}$$

$$\begin{aligned} \textcircled{5} \quad P_5 &= 100 \text{ kPa} \\ T_5 &= 556 \text{ K} \end{aligned}$$

$$\begin{aligned} \textcircled{6} \quad P_6 &= 100 \text{ kPa} & T_6 &= T_5 - (T_3 - T_2) = 556 - (575 - 585) \\ T_6 &= 566 \text{ K} & &= 566 \text{ K} \end{aligned}$$

$$\dot{m} = \frac{\dot{W}}{v} = \frac{\dot{W}}{h_3 - h_4 - (h_2 - h_1)}$$

$$= \frac{\dot{W}}{C_p (T_3 - T_2 r_p^{-(k-1)/k} - T_{1,r} (k-1)^{1/k} + T_1)}$$

$$\dot{W}$$

$$= \frac{\dot{W}}{C_p (T_3 (1 - r_p^{-(k-1)/k}) + T_1 (1 - r_p^{(k-1)/k}))}$$

$$115$$

$$1.005 (1073 (1 - 10^{-(1.4-1)/1.4}) + 303 (1 - 10^{(1.4-1)/1.4}))$$

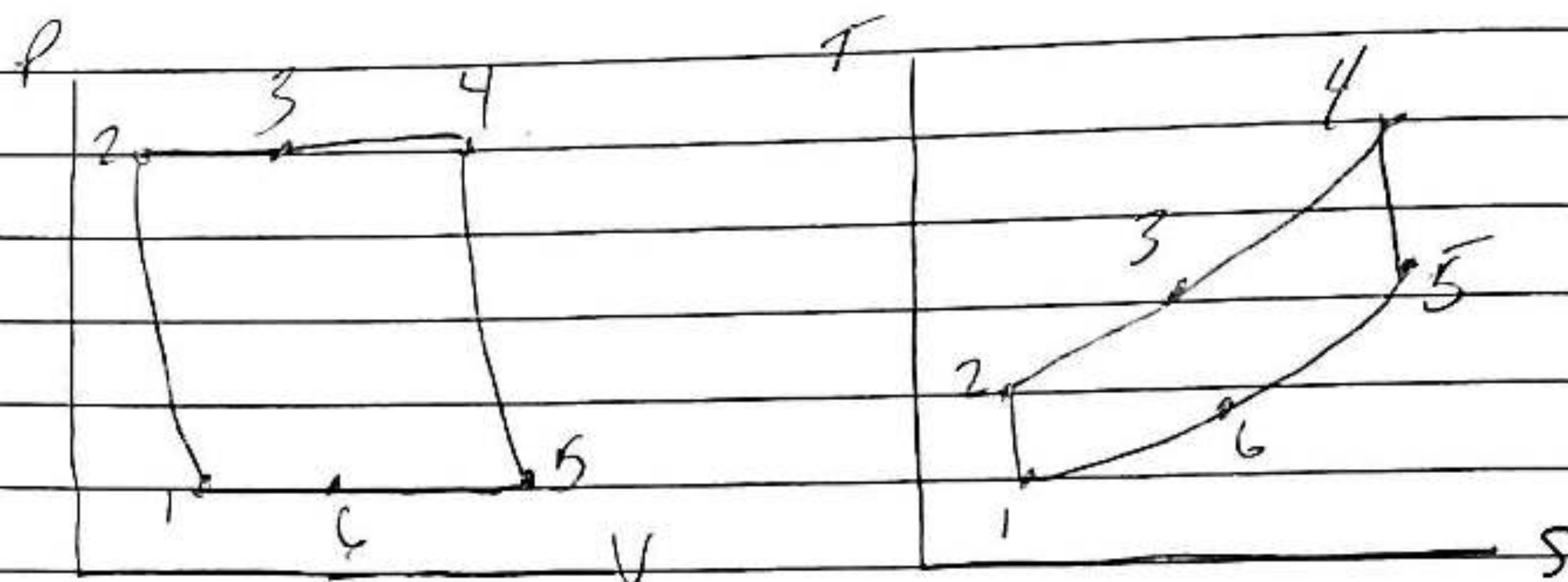
$$= 0.486 \text{ kg/s}$$

$$Q_{out} = \dot{m} (T_6 - T_1) = 0.486 \cdot 1.005 (595 - 303)$$

$$= 143 \text{ kW}$$

$$Q_{in} = \dot{W} + Q_{out} = 115 + 143 = 258 \text{ kW}$$

Problem 107



① $P_1 = 100 \text{ kPa}$

$T_1 = 310 \text{ K}$

$h_1 = 310.24$

$P_{r1} = 1.555$

② $P_2 = 700 \text{ kPa}$

$T_2 = 612 \text{ K}$

$h_2 = 618.3$

$P_{r2} = 17.4$

$P_{r2} = P_2 \cdot P_{r1} = 70 \cdot 1.555 = 10.885$

$h_{2s} = 541.3$

$h_2 = 310.24 \left(\frac{541.3 - 310.24}{.75} \right) + 310.24 = 618.3$

③ $P_3 = 700 \text{ kPa}$

$T_3 = 724 \text{ K}$

$h_3 = 738.4$

$h_3 = 618.3 + .65(803 - 618)$

$h_3 = 738.4$

④ $P_4 = 700 \text{ kPa}$

$T_4 = 1150 \text{ K}$

$h_4 = 1219.3$

$P_{r4} = 200$

⑤ $P_5 = 100 \text{ kPa}$

$T_5 = 783.6$

$h_5 = 803.3$

$P_{r5} = \frac{1}{P_{r1}} \cdot P_{r4} = P_{r2} = \frac{1}{7} \cdot 200 = 28.6$

$h_{5s} = 712$

$h_5 = 1219 - .52(1219 - 712) = 803.3$

⑥ $P_6 = 100 \text{ kPa}$

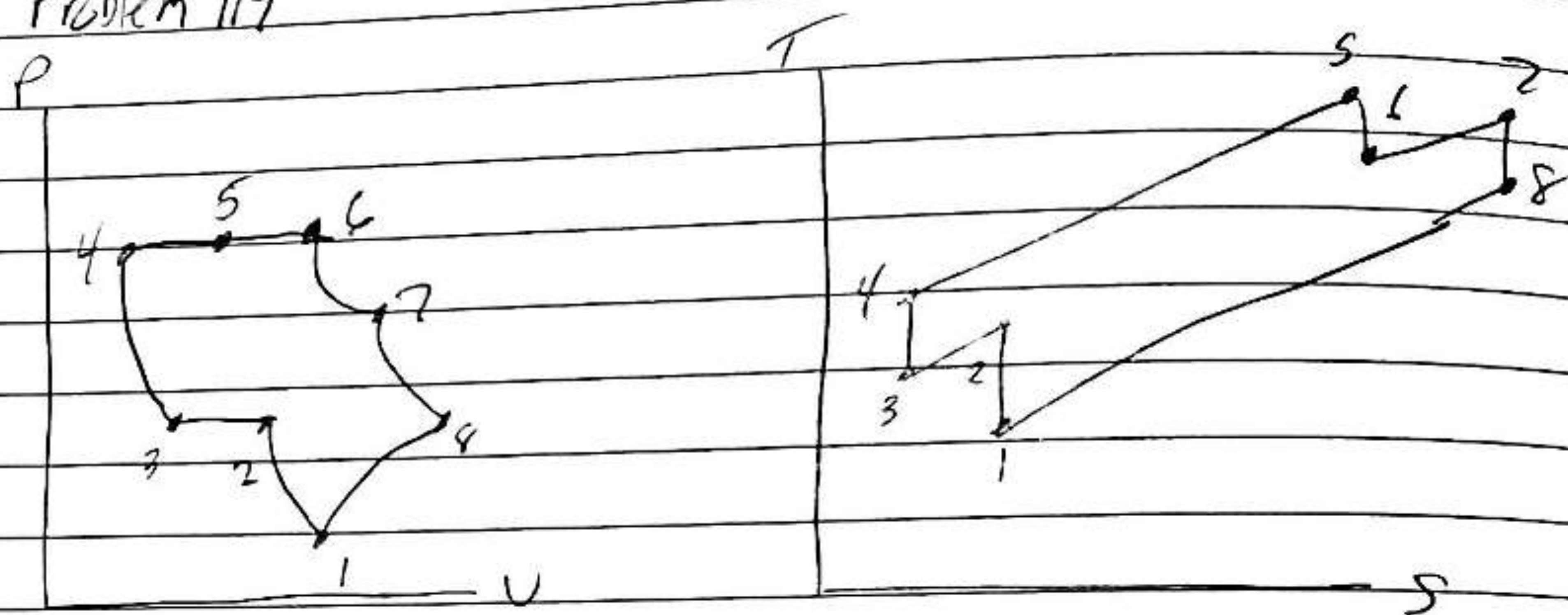
$$T_g = 783 \text{ K} \quad (a)$$

$$w_{net} = w_{in} - w_{out}$$

$$= (1719 - 803) - (618.3 - 310) = 108 \text{ kJ/kg} \quad (b)$$

$$\eta_H = \frac{w_{net}}{h_{in} - h_3} = \frac{108}{480.8} = 0.225 = 22.5\% \quad (c)$$

Problem 119



① $P_1 = 100 \text{ kPa}$

$T_1 = 300 \text{ K}$

$h_1 = 300$

$P_{r1} = 1.386$

② $T_2 = 410 \text{ K}$ $P_{r2} = (P_r)(P_{r1}) = (3)(1.386) = 4.158$

$h_2 = 411.3$

$P_{r2} = 4.158$

③ $T_3 = 300 \text{ K}$
 $h_3 = 300$

④ $T_4 = 410 \text{ K}$

$h_4 = 411.3$

⑤ $T_5 = 1200 \text{ K}$

$h_5 = 1278 \text{ K}$

$P_{r5} = 238$

⑥ $T_6 = 910 \text{ K}$

$h_6 = 946.4$

$P_{r6} = 79.3$

⑦ $T_7 = 1200 \text{ K}$

$h_7 = 1278$

⑧ $T_8 = 910 \text{ K}$

$P_{r6} = \left(\frac{1}{P_r}\right)(P_{r5}) = \left(\frac{1}{3}\right)(238) = 79.3$

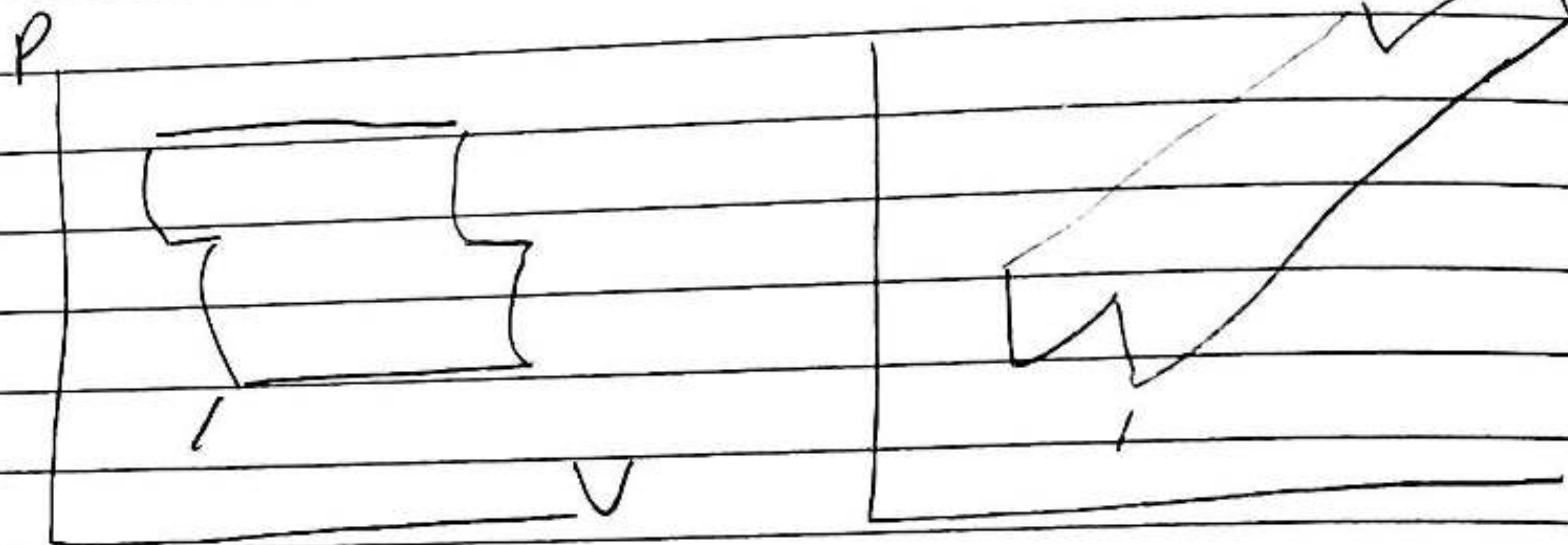
$$W_{in} = 2(h_2 - h_1) = 2(411 - 300) = 222$$

$$W_{out} = 2(h_5 - h_6) = 2(127 - 945) = 653$$

$$W_{net} = 653 - 222 = 441$$

$$\dot{m} \frac{w}{W_{net}} = \frac{110,000}{441} = 250 \text{ kg/s}$$

Problem 121



$$\textcircled{1} \quad h_1 = 300.19 \frac{\text{kJ}}{\text{kg}} \\ p_{r1} = 1.386$$

$$\textcircled{2} \quad p_{r2} = 4.158 \quad p_{r2} = \frac{p_2}{p_1} p_{r1} = 3.1386 = 4.158 \\ h_2 = 411.20 \frac{\text{kJ}}{\text{kg}}$$

$$\textcircled{3} \quad h_3 = 300.19 \frac{\text{kJ}}{\text{kg}} \\ p_{r3} = 1.386$$

$$\textcircled{4} \quad h_4 = 411.20 \frac{\text{kJ}}{\text{kg}}$$

$\textcircled{5}$

$$\textcircled{6} \quad p_{r6} = 238 \\ h_6 = 1277.75 \frac{\text{kJ}}{\text{kg}}$$

$$\textcircled{7} \quad p_{r7} = 79.33 \\ h_7 = 946.35 \frac{\text{kJ}}{\text{kg}}$$

$$p_{r7} = \frac{p_7}{p_6} p_{r6} = \frac{238}{3} = 79.33$$

$$\textcircled{8} \quad p_{r8} = 238 \\ h_8 = 1277.5 \frac{\text{kJ}}{\text{kg}}$$

$$\textcircled{9} \quad h_9 = 946.38 \frac{\text{kJ}}{\text{kg}}$$

(a)

$$\frac{h_w}{w_t} = \frac{w_c}{w_t} = \frac{2(h_2 - h_1)}{2(h_6 - h_7)} = \frac{411.26 - 300.19}{1277.79 - 946.35}$$
$$\boxed{= 0.335}$$

$$n = \frac{w}{q_{in}} = \frac{2(h_6 - h_7) - 2(h_2 - h_1)}{h_6 - h_4 + h_8 - h_7}$$

$$\frac{2(1277.79 - 946.35) - 2(411.26 - 300.19)}{1277.79 - 411.26 + 1277.79 - 946.35}$$

$$\boxed{= 0.368}$$

(b)

$$n = \frac{w}{q_{in} - q_{out}}$$

$$\frac{2(h_6 - h_7) - 2(h_2 - h_1)}{h_6 - h_4 + h_8 - h_7 - 0.75(h_5 - h_4)}$$

$$\frac{2(1277.79 - 946.35) - 2(411.26 - 300.19)}{1277.79 - 411.26 + 1277.79 - 946.25 - 0.75(946.35 - 411.26)}$$

$$\boxed{= 0.553}$$