

4) GIVEN

$$D = 10'' \quad D_{o1} = 1'' \quad D_{o2} = 7''$$

$$Q = 25 \text{ gal/min} \quad S_g = 0.83 \quad m_A = 2.5 \times 10^{-6}$$

$$A) \quad Q = \frac{25}{449} = 0.056 \text{ F/s} \quad A = \frac{\pi D^2}{4} = \frac{\pi (0.83)^2}{4} = 0.541''^2$$

$$A_1 = \frac{\pi (0.083)^2}{4} = 0.00541 \text{ ft}^2 \quad A_2 = \frac{\pi (5.83)^2}{4} = 0.267$$

$$\gamma = 0.83 \cdot 62.4 = 51.792$$

$$Q = C_{A1} \sqrt{\frac{2gh(\gamma_m - \gamma_A) - 1}{\left(\frac{A_1}{A_2}\right)^2 - 1}} = h = \frac{\left(\frac{Q}{C_{A1}}\right)^2 \cdot \left(\left(\frac{A_1}{A_2}\right)^2 - 1\right)}{2g \left(\frac{\gamma_A}{\gamma_m} - 1\right)}$$

$$V = \frac{0.056}{0.541} = 0.1035 \text{ F/s}$$

$$P = S_g A \quad p_w = 0.83 \cdot 1.94 = 1.6102$$

$$\gamma = \frac{m}{P} = \frac{2.5 \times 10^{-6}}{1.6102} = 1.553 \times 10^{-7}$$

$$N_R = \frac{VD}{\gamma}$$

$$N_R = \frac{0.1035(83)}{1.553 \times 10^{-7}} = 55315.518 \quad C = 0.594$$

$$h = \frac{\left(\frac{0.056}{594.541}\right)^2 \cdot \left(\left(\frac{.541}{0.00541}\right)^2 - 1\right)}{64.4 \left(\frac{62.4}{51.792} - 1\right)} = \boxed{23.021 \text{ ft}}$$

$$B) \quad \frac{d}{D} = \frac{7}{10} = 0.7 \quad C = 0.618$$

$$h = \frac{\left(\frac{0.056}{0.618 \cdot 541}\right)^2 \cdot \left(\left(\frac{.541}{.267}\right)^2 - 1\right)}{64.4 \left(\frac{62.4}{51.792} - 1\right)} = \boxed{0.0066'}$$

(2)

9) given: $D_t = 5''$ $T = 77^\circ\text{F}$ $h = 8''$ $A_t = 0.1259 \text{ ft}^2$

$Q = 700 \text{ gpm} \rightarrow 1000 \text{ gpm}$ $V_{H_2O} = 3.84 \times 10^{-4}$

$A_1 = \frac{A}{\sqrt{2gh \left(\frac{z_m}{z_H} - 1 \right)}}$

$\gamma_m = 58 \text{ lb/ft}^3$

$\gamma_{Hg} = 844.9$

$= \frac{0.1259}{\sqrt{\frac{(0.667)^2 + 1}{64.4(0.667) \left(\frac{844.9}{58} \right) - 1}}}$

$= 0.074 \text{ ft}^2$

$D = \sqrt{\frac{A \cdot 4}{\pi}} = \sqrt{\frac{0.079 \cdot 4}{\pi}}$

$D = 0.307'$

15) given: $T = 80^\circ\text{F}$ $h = 0.024''$ $\gamma_{air} = 0.0736 \text{ lb/ft}^3$

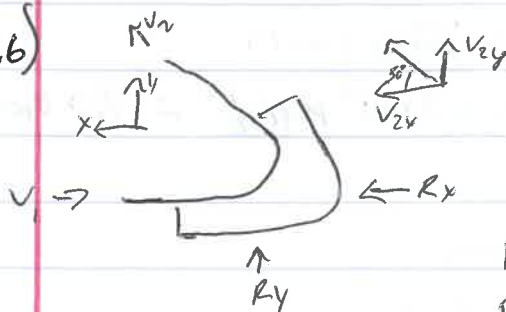
$\gamma_w = 62.4 \text{ lb/ft}^3$

$V_1 = \sqrt{2gh (\gamma_w - \gamma_{air}) / \gamma}$

$= \sqrt{64.4 \cdot (0.02) \cdot (62.4 - 0.0736) / 0.0736}$

$V_1 = 33.026 \text{ ft/s}$

16.6)



$$Q = AV = (2.95 \text{ in}^2) (22.0 \text{ ft/s}) (1 \text{ ft}^3 / 144 \text{ in}^2) \quad (3)$$

$$Q = 0.451 \text{ ft}^3/\text{s}$$

$$R_x = \rho Q (v_2 - v_1) = \rho Q [v_2 \cos 50 - (-v_1)]$$

$$R_x = \rho Q [v_2 \cos 50 + v_1] ; v_2 = v_1$$

$$R_x = \rho Q v_1 [\cos 50 + 1]$$

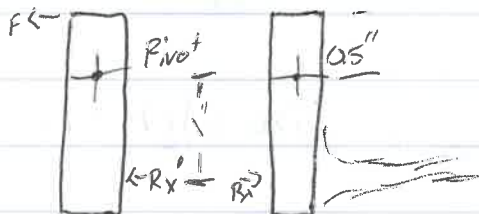
$$R_x = \left(\frac{1.88 \text{ lb} \cdot \text{s}^2}{\text{ft}^4} \right) \left(\frac{0.451 \text{ ft}^3}{\text{s}} \right) \left(\frac{22.0 \text{ ft}}{\text{s}} \right) (1.643)$$

$$R_x = 30.6 \text{ lb}$$

$$R_y = \rho Q (v_2 - v_1) \rightarrow \rho Q [v_2 \sin 50 - 0] = (1.88)(0.451)(22 \sin 50)$$

$$R_y = 14.5 \text{ lb}$$

16.11)



$$Q = 100 \text{ gal/min} \left(\frac{1 \text{ ft}^3/\text{s}}{449 \text{ gal/min}} \right) = 0.223 \text{ ft}^3/\text{s}$$

$$v_1 = \frac{Q}{A} = \frac{0.223}{0.0060} = 37.1 \text{ ft/s}$$

$$R_x = \rho Q (v_2 - v_1) = \rho Q [0 + v_1] = (\rho Q v_1)$$

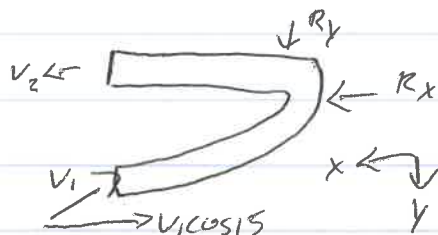
$$R_x = \left(\frac{1.94 \text{ lb} \cdot \text{s}^2}{\text{ft}^4} \right) \left(\frac{0.223 \text{ ft}^3}{\text{s}} \right) \left(\frac{37.1 \text{ ft}}{\text{s}} \right) = 16 \text{ lb}$$

$$R_x = R_x' \quad \sum M_A = 0 \rightarrow F_s(0.5) - R_x'(1.0)$$

$$F_s = R_x \left(\frac{1.0}{0.5} \right) = 2 R_x' = 2(16 \text{ lb}) = 32.0 \text{ lb}$$

16.29)

$$Q = AV = (3.142 \times 10^{-2}) (30) = 0.942 \text{ m}^3/\text{s}$$



$$R_x = \rho Q (v_2 - v_1) = \rho Q (v_2 - (-v_1 \cos 15))$$

$$R_x = \rho Q v (1 + \cos 15) = 1.966 \rho Q v$$

$$R_x = (1.966) \left(\frac{1000 \text{ kg}}{\text{m}^3} \right) \left(\frac{0.943 \text{ m}^3}{\text{s}} \right) \left(\frac{30 \text{ m}}{\text{s}} \right) = 55.6 \text{ kN}$$

(4)

$$R_y = \rho Q (v_2 - v_1) = \rho Q (0 - (-v_1 \sin 15)) = \rho Q v_1 \sin 15$$

$$R_y = (1000)(0.943)(30)(0.259) = 7.32 \times 10^3 \text{ kg/m/s}^2 = 7.32 \text{ kN}$$

$$b) \quad v_{ix} = v_1 \cos(15) = 30 \text{ m/s} (0.966) = 28.98 \text{ m/s}$$

$$v_{iy} = v_1 \sin(15) = 30 \text{ m/s} (0.259) = 7.76 \text{ m/s}$$

$$v_{elx} = v_{ix} - 12 \text{ m/s} = 16.98 \text{ m/s}$$

$$v_{ely} = \sqrt{16.98^2 + 7.76^2} = 18.67 \text{ m/s}$$

$$m_e = \rho Q_e = \rho A v_{e1} = (1000)(3.142 \times 10^{-2})(18.67) = 586.6 \text{ kg/s}$$

$$\alpha = \tan^{-1}(7.76/16.98) = 24.58^\circ$$

$$\beta = 24.58^\circ - 15^\circ = 9.58^\circ$$

$$v_{elx} = (v_{el}) \cos(9.58) = (18.67)(0.986) = 18.41 \text{ m/s}$$

force in x

$$R_x = m_e (\Delta v_{ex}) = m_e (v_{ex2} - v_{ex1}) = (586.6)[18.41 - (-16.98)]$$

$$R_x = 20.76 \text{ kN}$$

force in y

$$R_y = m_e (\Delta v_{ey}) = m_e (v_{ey2} - v_{ey1}) = (586.6)[0 - (-7.76)]$$

$$R_y = 4.55 \text{ kN}$$



$$m = \rho A V$$

$$R_x = M(\Delta V_x) = M(V_{2x} - V_{1x})$$

$$A = \pi D^2 / 4 = \pi (0.0075)^2 / 4 = 4.418 \times 10^{-5} \text{ m}^2$$

$$M = \rho A V = (1000)(4.418 \times 10^{-5})(25) = 1.105 \text{ kg/s}$$

$$V_{1x} = V_1 \cos(10) = (25)(0.985) = 24.62 \text{ m/s}$$

$$V_{1y} = V_1 \sin(10) = (25)(0.174) = 4.34 \text{ m/s}$$

$$V_2 = V = 25 \text{ m/s}$$

$$V_{2x} = V_2 \cos(60) = (25 \text{ m/s})(0.5) = 12.5 \text{ m/s} \quad V_{2y} = V_2 \sin(60) = (25)(0.866) = 21.65 \text{ m/s}$$

Force in x

$$R_x = M(\Delta V_x) = M(V_{2x} - V_{1x}) = 1.105 \text{ kg/s} [12.5 - (-24.62)]$$

$$R_x = 41.0 \text{ N}$$

Force in y

$$R_y = M(\Delta V_y) = M(V_{2y} - V_{1y}) = (1.105 \text{ kg/s}) [21.65 - 4.34]$$

$$R_y = 19.1 \text{ N}$$