

## **Homework 3.2**

The problems discussed this week were a continuation of series and parallel piping systems. We continued our discussion on how to tackle the problems and ended up creating a new way to do them, dubbed "Kyle's Method". We also began talking about how to select pumps and why pump choice is an important factor in piping systems. One of the factors that was discussed was how the RPM of a pump affects the flowrate of a liquid.

## Homework Problems

11.23

11-23) For the system below, compare total head on the pump and power delivered by the pump on the coolant.

$Q = 30 \frac{\text{gal}}{\text{min}} = 6930 \frac{\text{in}^3}{\text{min}} = 115.5 \frac{\text{in}^3}{\text{s}}$   
 $\Rightarrow Q = 0.07 \text{ ft}^3/\text{s}$

1" Schedule 40  
 $D_1 = 2.067 \text{ in} \Rightarrow A_1 = 3.36 \text{ in}^2 = 0.0233 \text{ ft}^2$   
1/4" Schedule 40  
 $D_2 = 1.38 \text{ in} \Rightarrow A_2 = 1.50 \text{ in}^2 = 0.01 \text{ ft}^2$

$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 + P_{\text{del}} = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2 + h_f$   
 $V_{1 \text{ pipe}} = 0.07 \text{ ft}^3/\text{s} / 0.0233 \text{ ft}^2 = 3 \text{ ft/s} = V_1$   
 $V_{1/4 \text{ pipe}} = 0.07 \text{ ft}^3/\text{s} / 0.01 \text{ ft}^2 = 7 \text{ ft/s} = V_2$

$\rho = \gamma/g \Rightarrow 57.4 \frac{\text{lb}}{\text{ft}^3} / 32 \frac{\text{ft}}{\text{s}^2} = 1.79 \frac{\text{lb}}{\text{ft}^3}$   
 $N_{R_1} = \frac{3 \text{ ft/s} \cdot (2.067 \text{ in} / 12 \frac{\text{in}}{\text{ft}}) \cdot 57.4 \frac{\text{lb}}{\text{ft}^3}}{3.6 \cdot 10^{-5} \frac{\text{lb}}{\text{ft} \cdot \text{s}}} = 82392.9$   
 $N_{R_2} = \frac{7 \text{ ft/s} \cdot (1.38 \text{ in} / 12 \frac{\text{in}}{\text{ft}}) \cdot 57.4 \frac{\text{lb}}{\text{ft}^3}}{3.6 \cdot 10^{-5} \frac{\text{lb}}{\text{ft} \cdot \text{s}}} = 128352.8$   
 $\Rightarrow f_{2 \text{ in}} = 0.0185 \quad f_{1/4 \text{ in}} = 0.016$   
 $\Rightarrow h_{f_{2 \text{ in}}} = 0.0185 \cdot \left( \frac{120 \text{ ft}}{2.067 \text{ in}} \right) \cdot \left( \frac{36 \text{ in}^2}{(2.067 \text{ in})^2} \right)$   
 $\Rightarrow h_{f_{2 \text{ in}}} = 1.8 \text{ ft} = 0.15'$   
 $\Rightarrow h_{f_{1/4 \text{ in}}} = 0.016 \cdot \left( \frac{240 \text{ ft}}{1.38 \text{ in}} \right) \cdot \left( \frac{84 \text{ in}^2}{(1.38 \text{ in})^2} \right)$   
 $\Rightarrow h_{f_{1/4 \text{ in}}} = 25.4 \text{ ft} = 2.11'$   
 $\Rightarrow h_{\text{tot}} = 27.2 \text{ ft} = 2.27' \quad \{h_{\text{tot}} = P_{\text{del}}\}$   
 $P_1 = 57.4 \frac{\text{lb}}{\text{ft}^3} \cdot 3 \text{ ft} = 172.2 \frac{\text{lb}}{\text{ft}^2} = 1.2 \text{ PSI} \left( \frac{\text{lb}}{\text{in}^2} \right)$   
 $P_2 = 57.4 \frac{\text{lb}}{\text{ft}^3} \cdot 7 \text{ ft} = 401.8 \frac{\text{lb}}{\text{ft}^2} = 2.77 \text{ PSI} \left( \frac{\text{lb}}{\text{in}^2} \right)$   
 $\Rightarrow \text{total head at pump} = \frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 + P_{\text{del}}$   
 $\Rightarrow \frac{172.2 \frac{\text{lb}}{\text{ft}^2}}{57.4 \frac{\text{lb}}{\text{ft}^3}} + \frac{3 \text{ ft/s}^2}{2 \cdot 32 \frac{\text{ft}}{\text{s}^2}} + 3 \text{ ft} + 2.27 \text{ ft} = 8.41 \text{ ft} = \text{head at inlet of Pump}$

11.24

11-24) For the system in the previous problem, specify the size pipes necessary to remain coolant to the machines. Machine 1 requires 20 gal/min & machine 2 requires 10 gal/min. Fluid leaves at 0 PSI.

$Q = 30 \frac{\text{gal}}{\text{min}} = 6930 \frac{\text{in}^3}{\text{min}} = 115.5 \frac{\text{in}^3}{\text{s}}$   
 $= 0.07 \text{ ft}^3/\text{s} = 4.2 \frac{\text{ft}^3}{\text{min}}$

• Velocity must remain constant, therefore area of the pipes must change to achieve desired flow rates

$\Rightarrow 0.07 \frac{\text{ft}^3}{\text{s}} = 3 \frac{\text{ft}}{\text{s}} \cdot A \Rightarrow A = 0.0233 \text{ ft}^2 \Rightarrow 2 \text{ inch Schedule 40}$   
 $20 \frac{\text{gal}}{\text{min}} = 4620 \frac{\text{in}^3}{\text{min}} = 77 \frac{\text{in}^3}{\text{s}} = 0.045 \frac{\text{ft}^3}{\text{s}}$   
 $\Rightarrow 0.045 \frac{\text{ft}^3}{\text{s}} = 3 \frac{\text{ft}}{\text{s}} \cdot A \Rightarrow A = 0.015 \text{ ft}^2 \Rightarrow 1 \frac{1}{2} \text{ inch Schedule 40 pipe}$   
 $10 \frac{\text{gal}}{\text{min}} = 2310 \frac{\text{in}^3}{\text{min}} = 38.5 \frac{\text{in}^3}{\text{s}} = 0.0222 \frac{\text{ft}^3}{\text{s}}$   
 $\Rightarrow 0.0222 \frac{\text{ft}^3}{\text{s}} = 3 \frac{\text{ft}}{\text{s}} \cdot A \Rightarrow A = 0.0074 \text{ ft}^2 \Rightarrow 1 \text{ inch Schedule 40 pipe}$

Main pipe: 2" Schedule 40  
 to #1: 1 1/2" Schedule 40  
 to #2: 1" Schedule 40

## 12.3

12.3

$D = 0.0525 \text{ m} = 1.41 \times 10^{-3} \text{ m}$   
 $\frac{D}{L} = \frac{1.41 \times 10^{-3}}{4.6 \times 10^{-2}} \rightarrow \approx 0.019$  for  $f_2$  (and  $f_1$ )

$(571.43 f_2 + 0.7) \left( \frac{V_2}{2g} \right) = (1142.86 f_2 + 4.66) \left( \frac{V_2}{2g} \right)$

$V_2 = 0.44 V_1$   $A = 2.168 \times 10^{-3} \text{ m}^2$   $850 \text{ L/min} = 0.0141 \text{ m}^3/\text{s}$   
 $Q_1 = Q_2 = Q_3 \rightarrow Q = A_1 V_1 + A_2 V_2$   
 $0.0141 = (2.168 \times 10^{-3}) V_1 + (2.168 \times 10^{-3}) (0.44 V_1)$   
 $V_1 = 3.97 \text{ m/s}$   
 $V_2 = 0.44 (3.97) = 2.54 \text{ m/s}$

$N_H = \frac{V_2 D}{\nu} \rightarrow \frac{(2.54)(0.0525)}{1.30 \times 10^{-6}} = 102576.9 \rightarrow f_2 = 0.021$

$N_H = \frac{V_1 D}{\nu} = \frac{(3.97)(0.0525)}{1.30 \times 10^{-6}} = 16326.9 \rightarrow f_1 = 0.021$   
 smaller than assumed

$(571.43 (0.021) + 0.7) \left( \frac{V_2}{2g} \right) = (1142.86 (0.021) + 4.66) \left( \frac{V_2}{2g} \right)$   
 $V_2 = 0.444 V_1$   
 $0.0141 = (2.168 \times 10^{-3}) V_1 + (2.168 \times 10^{-3}) (0.444 V_1)$   
 $V_1 = 3.96 \text{ m/s}$   
 $V_2 = 0.444 (3.96) = 2.55 \text{ m/s}$

$Q_1 = A_1 V_1 = (2.168 \times 10^{-3}) (3.96) = 0.008635 \text{ m}^3/\text{s} = 515.15 \text{ L/min}$   
 $Q_2 = A_2 V_2 = (2.168 \times 10^{-3}) (2.55) = 0.005528 \text{ m}^3/\text{s} = 331.7 \text{ L/min}$

$h_L = \frac{(571.43 (0.021) + 0.7) \frac{V_1^2}{2g}}{2g} = 10.15 \text{ m}$

$\Delta p = \gamma h_L$   
 $9.81 \text{ kN/m}^3 (10.15 \text{ m}) = 99.57 \text{ kPa}$

## 12.5

Problem 12.5

160 mm outer diam. 150 mm inner diam. 80 mm outer diam. 150 mm inner diam.

16 W/mK

Water at 10°C

$\nu = 1.30 \times 10^{-4} \text{ m}^2/\text{s}$

Desired flow rate through both pipes = 0.005 m<sup>3</sup>/s

$L = 300 \text{ mm}$

$Y = 9.81 \text{ kN/m}^3$

$\nu = 1.30 \times 10^{-4} \text{ m}^2/\text{s}$

$\frac{P_1 + \frac{V_1^2}{2g} + Z_1}{\gamma} = \frac{P_2 + \frac{V_2^2}{2g} + Z_2}{\gamma} + h_{L, I-2}$

$\frac{P_1 - P_2}{\gamma} = h_{L, I-2} \Rightarrow \frac{\Delta P}{\gamma} = h_{L, I-2}$

$\Rightarrow \frac{\Delta P}{\gamma} = h_{L, I-2}$

$h_{L, I-2} = 2 f_{I-2} \frac{L}{D} \frac{V_1^2}{2g} + h_{f, I-2} + h_{L, I-2} + h_{L, I-2}$

$h_{L, I-2} = 2 f_{I-2} \frac{L}{D} \frac{V_1^2}{2g} + h_{f, I-2} + h_{L, I-2}$

For the pipe network,  $h_{L, I-2} = h_{L, I-2}$

$2 f_{I-2} \frac{L}{D} \frac{V_1^2}{2g} + h_{f, I-2} + h_{L, I-2} = 2 f_{I-2} \frac{L}{D} \frac{V_1^2}{2g} + h_{f, I-2} + h_{L, I-2}$

And LHS =  $h_{L, I-2} + h_{L, I-2} + h_{L, I-2}$

$= f_2 \frac{L}{D} \frac{V_1^2}{2g} + 2 K_{elb} \frac{V_1^2}{2g} + K_{valv} \frac{V_1^2}{2g}$   $V_1 = \frac{16 Q}{\pi D^2}$

$LHS = f_2 \frac{L}{D} \frac{8}{g \pi^2 D^5} Q^2 + 2 K_{elb} \frac{8}{g \pi^2 D^5} Q^2 + K_{valv} \frac{8}{g \pi^2 D^5} Q^2$

$= (f_2 \frac{L}{D} + 2 K_{elb} + K_{valv}) \frac{8}{g \pi^2 D^5} Q^2$

Similarly, RHS =  $(f_2 \frac{L}{D} + 2 K_{elb}) \frac{8}{g \pi^2 D^5} Q^2$

Combine the two equations

$(f_2 \frac{L}{D} + 2 K_{elb} + K_{valv}) \frac{8}{g \pi^2 D^5} Q^2 = (f_2 \frac{L}{D} + 2 K_{elb}) \frac{8}{g \pi^2 D^5} Q^2$

From the second equation

$(f_2 \frac{L}{D} + 2 K_{elb} + K_{valv}) \frac{1}{D^5} = (f_2 \frac{L}{D} + 2 K_{elb}) \frac{1}{D^5}$

For the exact diameter

$(6.6926 + 0.9995 + K_{valv}) \frac{1}{(0.013)^5} = (13.5533 + 1.17192) \frac{1}{(0.013)^5}$

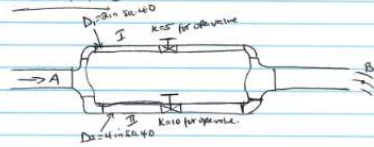
$(7.6926 + K_{valv}) \frac{1}{(0.013)^5} = 302628.1$

$7.6926 + K_{valv} = 226.82$

$K_{valv} = 218.69 \text{ m}$

## 12.6

## Problem 12.6



$$P_A = 20 \text{ psi}$$

$$K_{LB} = 0.9$$

$$\text{Neglect Tee losses}$$

$$\text{Pipe losses}$$

$$10 \text{ m/s } V = 6.24 \text{ m}^3/\text{s}$$

$$D_1 = 0.1733 \text{ m}$$

$$D_2 = 0.1335 \text{ m}$$

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + z_B + h_{L_{A-B}}$$

$$\frac{P_A}{\gamma} = h_{L_{A-B}} \Rightarrow \frac{P_A}{\gamma} = h_{L_{A-B}}$$

$$\Rightarrow \frac{P_A}{\gamma} = h_{L_{A-B}}$$

$$h_{L_{A-B}} = 2h_{L_{I}} + h_{L_{II}}$$

$$h_{L_{A-B}} = 2h_{L_{I}} + h_{L_{II}} = 2K_{LB} \frac{V_I^2}{2g} + K_{LB} \frac{V_{II}^2}{2g}$$

$$V^2 = \frac{16Q^2}{\pi^2 D^5}$$

$$h_{L_{A-B}} = 2h_{L_{I}} + h_{L_{II}} = 2K_{LB} \frac{V_I^2}{2g} + K_{LB} \frac{V_{II}^2}{2g}$$

$$h_{L_{A-B}} = (2K_{LB} + K_{LB}) \frac{8}{g\pi^2 D^5} Q^2 = (2 \times 0.9 + 0.9) \frac{8}{9.81 \pi^2 D^5} Q^2$$

$$h_{L_{A-B}} = (2K_{LB} + K_{LB}) \frac{8}{g\pi^2 D^5} Q^2 = (2 \times 0.9 + 0.9) \frac{8}{9.81 \pi^2 D^5} Q^2$$

$$\frac{P_A}{\gamma} = \left( \frac{2 \times 0.9 + 0.9}{6.24 \times 10^6} \right) Q^2 = 46.15 \text{ ft}$$

To evaluate for  $Q_I$ 

$$46.15 \text{ ft} = \frac{(6.8) \cdot 8}{9.81 \pi^2 (0.1733)^5} Q_I^2$$

$$Q_I = \sqrt{\frac{46.15 \times 9.81 \pi^2 \times (0.1733)^5}{6.8 \times 8}} = 0.487 \text{ ft}^3/\text{s}$$

To evaluate for  $Q_{II}$ 

$$46.15 \text{ ft} = \frac{(11.8) \cdot 8}{9.81 \pi^2 (0.1335)^5} Q_{II}^2$$

$$Q_{II} = \sqrt{\frac{46.15 \times 9.81 \pi^2 \times (0.1335)^5}{11.8 \times 8}} = 1.403 \text{ ft}^3/\text{s}$$

Total flow rate if:

a) Both valves open

$$Q_T = Q_I + Q_{II}$$

$$= 0.487 + 1.403$$

$$Q_T = 1.89 \text{ ft}^3/\text{s}$$

b) Valve II open (only)

$$Q_T = Q_{II}$$

$$Q_T = 1.403 \text{ ft}^3/\text{s}$$

c) Valve I open (only)

$$Q_T = Q_I$$

$$Q_T = 0.487 \text{ ft}^3/\text{s}$$