

HW 2.3

15.4 $D = 10 \text{ in}$, $Q = 25 \text{ gpm}$, $SG_{\text{mercury}} = 0.83$

$\mu = 2.5 \times 10^{-6} \text{ lb-s/ft}^2$, $d_1 = 1.0 \text{ in}$, $d_2 = 7.0 \text{ in}$

a) $A_1 = \pi(0.83)^2/4 = 0.541 \text{ ft}^2$

$A_2 = \pi(0.083)^2/4 = 0.00541 \text{ ft}^2$

$\gamma_A = (0.83)(62.4 \text{ lb/ft}^3) = 51.79 \text{ lb/ft}^3$

$V_1 = 0.056 \text{ ft}^3/\text{s} / 0.541 \text{ ft}^2 = 0.104 \text{ ft/s}$

$\nu = \mu/\rho \rightarrow \rho = SG_A \times \text{density}_w = 0.83 \times 1.94 = 1.61 \text{ slug/ft}^3$

$\rightarrow V = 2.5 \times 10^{-6} \text{ lb-s/ft}^2 / 1.61 \text{ slug/ft}^3 = 1.55 \times 10^{-6} \text{ ft}^2/\text{s}$

$N_R = (0.104 \text{ ft/s})(0.83) / 1.55 \times 10^{-6} \text{ ft}^2/\text{s} = 55690.3$

$V_1 = C \sqrt{2gh((\gamma_m/\gamma_A) - 1) / (A_1/A_2)^2 - 1}$

$\rightarrow h = (V_1/C)^2 ((A_1/A_2)^2 - 1) / 2g((\gamma_m/\gamma_A) - 1)$

$h = (0.104 \text{ ft/s} / 0.599)^2 ((0.541 \text{ ft}^2 / 0.00541 \text{ ft}^2)^2 - 1) / 2(32.2 \text{ ft/s}^2)((62.4/51.79) - 1)$

$h = 23.23 \text{ ft}$

b) $A_2 = \pi(0.58 \text{ ft})^2/4 = 0.264 \text{ ft}^2$

$h = (0.104 / 0.618)^2 ((0.541 / 0.264)^2 - 1) / 2(32.2)((62.4/51.79) - 1)$

$h = 0.0069 \text{ ft}$

15.9 From Appendix H: $A = 0.1259 \text{ ft}^2$, $D = 4.805 \text{ in}$

$V_{\text{max}} = 1.558 \text{ ft}^3/\text{s} / 0.1259 \text{ ft}^2 = 12.38 \text{ ft/s}$

From Appendix B: $\nu = 3.84 \times 10^{-4} \text{ ft}^2/\text{s}$, $\gamma = 58 \text{ lb/ft}^3$

$N_R = (12.38 \text{ ft/s})(0.4 \text{ ft}) / 3.84 \times 10^{-4} \text{ ft}^2/\text{s} = 12,895.83$

$V_{\text{max}} = 2.227 \text{ ft}^3/\text{s} / 0.1259 \text{ ft}^2 = 17.686 \text{ ft/s}$

$N_R = (17.686 \text{ ft/s})(0.4 \text{ ft}) / 3.84 \times 10^{-4} \text{ ft}^2/\text{s} = 18,422.92$

$A_1 = A / \sqrt{2gh((\gamma_m/\gamma)(C)^2 / V_{\text{max}}^2 + 1)} = 0.0746 \text{ ft}^2$

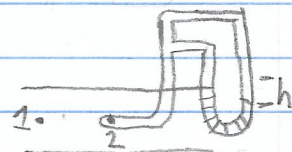
$d = \sqrt{0.0746 \text{ ft}^2 \times 4 / \pi} = 0.3082 \text{ ft} = 3.70 \text{ in}$

15.15 $\gamma_a = 0.0685 \frac{\text{lb}}{\text{ft}^3}$ $\gamma_w = 61.7 \frac{\text{lb}}{\text{ft}^3}$ $h = 0.24 \text{ in}$ Find V_1 .

$$P_1 + \gamma_w \cdot h - \gamma_a \cdot h = P_2 \quad P_2 - P_1 = h(\gamma_w - \gamma_a)$$

$$P_1 = 0 \text{ psig} \quad \frac{P_1}{\gamma_a} + \frac{V_1^2}{2g} = \frac{P_2}{\gamma_a} \quad V_1 = \sqrt{2g \cdot \frac{P_2 - P_1}{\gamma_a}}$$

$$V_1 = \sqrt{2 \cdot g \cdot \frac{h(\gamma_w - \gamma_a)}{\gamma_a}} = 34.03 \frac{\text{ft}}{\text{s}}$$



16.6 $\theta = 50^\circ$ $V_1 = 22 \frac{\text{ft}}{\text{s}}$ $A = 2.95 \text{ in}^2 = 0.021 \text{ ft}^2$ Find F_x and F_y .

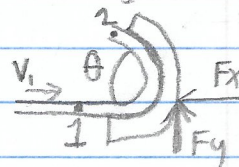
$$\rho = 1.88 \frac{\text{slug}}{\text{ft}^3} \quad Q = V_1 \cdot A = 0.451 \frac{\text{ft}^3}{\text{s}}$$

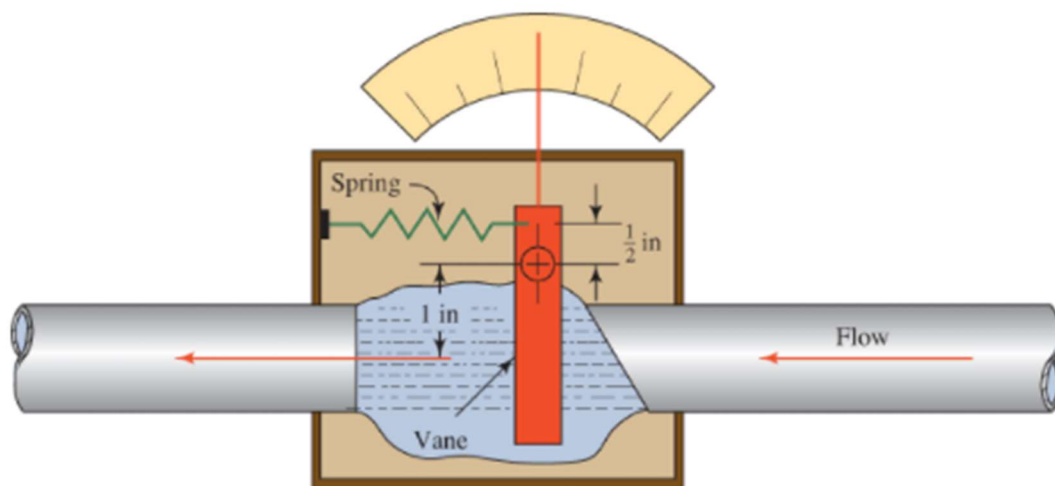
$$F_x = \rho \cdot Q \cdot (V_{2x} - V_{1x}) \quad V_{1x} = 22 \frac{\text{ft}}{\text{s}} \quad V_{2x} = V_1 \cdot \cos 180 - \theta$$

$$V_{2x} = -14.14 \frac{\text{ft}}{\text{s}} \quad F_x = -30.64 \text{ lb}$$

$$F_y = \rho \cdot Q \cdot (V_{2y} - V_{1y}) \quad V_{1y} = 0 \frac{\text{ft}}{\text{s}} \quad V_{2y} = V_1 \cdot \sin 180 - \theta$$

$$V_{2y} = 16.85 \frac{\text{ft}}{\text{s}} \quad F_y = 14.29 \text{ lb}$$





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$$\text{Flow rate} = 0.2228 \text{ ft}^3/\text{s}$$

$$\text{area } 1 \text{ in pipe} = 0.006 \text{ ft}^2$$

$$\text{water density} = 1.94 \text{ lb/ft}^3$$

$$\text{Velocity} = 37.1 \text{ ft/s}$$

$$\text{Force} = 1.94 \cdot 0.2228 \cdot (37.1 - (-37.1))$$

$$\boxed{F = 32.07 \text{ lb}}$$

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Flow into water

$$Q = Av$$

$$Q = \frac{\pi}{4} \times 0.2^2 \times 30$$

$$Q = 0.943 \text{ m}^3/\text{s}$$

Force water y

$$R_y = \rho Q v (0 + \sin \theta)$$

$$R_y = 0.25 \times 1000 \times 0.943 \times 30$$

$$R_y = 7072.5 \text{ N}$$

Force water x

$$R_x = \rho Q v (0 + \cos \theta)$$

$$R_x = 1.966 \times 1000 \times 0.943 \times 30$$

$$R_x = 55618.14 \text{ N}$$

Velocity x

$$V_x = V \cos \theta$$

$$V_x = 30 \cos 15$$

$$V_x = 28.98 \text{ m/s}$$

Velocity y

$$V_y = V \sin \theta$$

$$V_y = 30 \sin 15$$

$$V_y = 7.76 \text{ m/s}$$

Velocity X car

$$28.98 \text{ m/s} - 12 \text{ m/s} = 16.98 \text{ m/s}$$

Velocity

$$V = \sqrt{16.98^2 + 7.76^2}$$

$$V = 18.67 \text{ m/s}$$

Mass

$$m = 1000 \cdot \frac{\pi}{4} \cdot 0.2^2 \cdot 18.67$$

$$m = 586.6 \text{ kg/s}$$

Angle Velocity

$$\alpha = \tan^{-1}\left(\frac{7.76}{16.98}\right)$$

$$\alpha = 24.56^\circ$$

True angle

$$24.56 - 15 = 9.56^\circ$$

True Velocity

$$18.67 \cos 9.56^\circ = 18.4 \text{ m/s}$$

$$\text{force } X \text{ car} \\ = 586.6 \cdot (18.4 - 16.98)$$

$$\underline{832.97 \text{ N}}$$

$$\text{force } Y \text{ car} \\ = 586.6 \cdot 7.76$$

$$\underline{4552 \text{ N}}$$

16.29 Water @ 15°C

$$D = 7.50 \text{ mm} = 0.0075 \text{ m}$$

$$v = 25 \text{ m/s}$$

$$A = \pi(0.0075)^2/4 = 4.418 \times 10^{-5} \text{ m}^2$$

$$Q = (4.418 \times 10^{-5} \text{ m}^2)(25 \text{ m/s})$$

$$Q = 0.0011 \text{ m}^3/\text{s}$$

$$R_x = \rho Q (v_2 \cos 60^\circ + v_1 \cos 10^\circ)$$

$$R_x = 1000 \times 0.0011 \text{ m}^3/\text{s} ((25 \text{ m/s} \cos 60^\circ) + (25 \text{ m/s} \cos 10^\circ)) = \boxed{40.83 \text{ N}}$$

$$R_y = 1000 \times 0.0011 ((25 \sin 60^\circ) - (25 \sin 10^\circ)) = \boxed{19.04 \text{ N}}$$

