

23. $Q = 30 \frac{\text{gal}}{\text{min}}$ S.G. = 0.92 $\eta = 3.6 \cdot 10^{-5} \frac{\text{lb} \cdot \text{s}}{\text{ft}^2}$

Find pump head and pump power. $E = 1.5 \cdot 10^{-4} \text{ ft}$

$$h_a + z_1 = h_L + z_2 \quad h_a = h_L + z_2 - z_1$$

$$z_1 = 3 \text{ ft} \quad z_2 = 22 \text{ ft} \quad Q = 0.067 \frac{\text{ft}^3}{\text{s}}$$

$$\rho = 0.92 \cdot 1.94 = 1.78 \frac{\text{slug}}{\text{ft}^3} \quad V = \frac{Q}{\pi \cdot d^2}$$

Suction line: $d = 0.1723 \text{ ft}$ $Re = \frac{Q \cdot \rho}{\eta \cdot \pi \cdot d} = 24980$

$$f = 0.25 / \left(\log \left(\frac{1}{3.7 \cdot d / \epsilon} + \frac{5.74}{Re^{0.4}} \right) \right)^2 = 0.0268 \quad h_{Ls} = \left(f \cdot \frac{L}{d} + 8 \cdot f_t \right) \frac{Q^2}{\pi^2 \cdot g \cdot d^5}$$

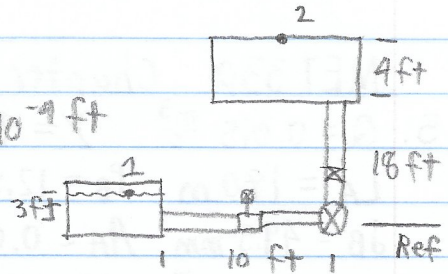
$$f_t = 0.019 \text{ from Table 10.5} \quad h_{Ls} = 0.219 \text{ ft}$$

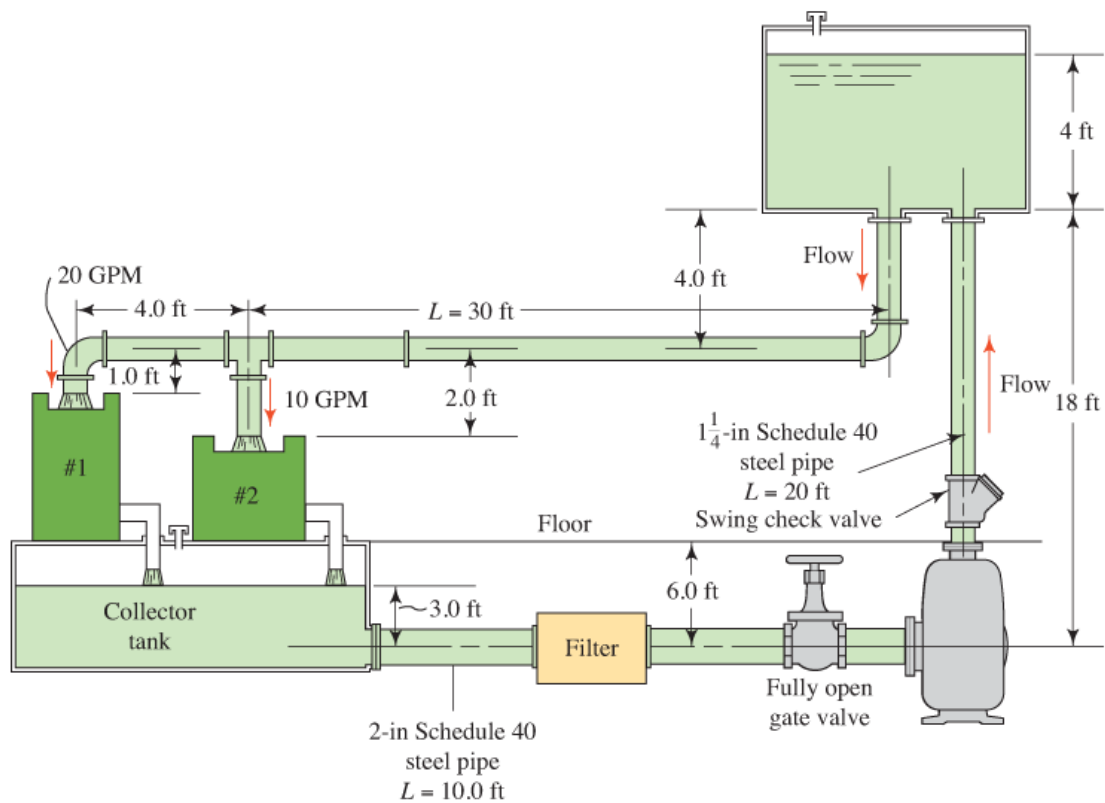
Discharge line: $d = 0.115 \text{ ft}$ $Re = 36678$ $f = 0.026$ $f_t = 0.021$

$$h_{Ld} = \left(f \cdot \frac{L}{d} + 100 \cdot f_t \right) \frac{Q^2}{\pi^2 \cdot g \cdot d^5} = 4.28 \text{ ft}$$

$$h_a = h_{Ls} + h_{Ld} + z_2 - z_1 = 23.5 \text{ ft} \quad P = h_a \cdot \gamma \cdot Q = 90.4 \frac{\text{ft} \cdot \text{lb}}{\text{s}}$$

$$P = 0.16 \text{ hp}$$





Flow Rate			Length Pipe			Pipe thickness			Specifit gravity		0.92	
Q	30 gal/min		L	39 ft		E	0.00015 ft		Water density		62.427	
	0.0668 ft^3/s											
P1	0 psig		Density			Kinematic Viscosity						
P2	0 psig		d	57.43284 lb/ft^3		v	2.01836E-05 ft^2/s					
Z1	9 ft											
Z2	0 ft		Dynamic Viscosity									
			Dv	0.0011592 lbs/ft^2								
Head Loss												
HL	9 ft											
Diameter												
D	0.10591 ft											

Equation 11-8				
E ^{1.25}	(LQ ² /HLg) ^{4.75}	v	Q ^{9.4}	(L/HLg) ^{5.2}
1.66002E-05	4.98845E-16	2.01836E-05	8.9722E-12	2.95546E-05

24

Head loss

$$HL = Z_1 - Z_2$$

$$HL = 9.4$$

Density = $S_g \cdot \rho_{water}$

$$\text{Density } \rho = 57.43 \text{ lb/ft}^3$$

Kinematic viscosity

$$V = \frac{\text{Dynamic viscosity}}{\rho}$$

$$\text{Kinematic viscosity } V = 2.018 \cdot 10^{-5} \text{ ft}^2/\text{s}$$

Diameter =

$$D = 0.66 \left(1.75 \left(\frac{LQ^2}{gHL} \right)^{4.75} + VQ^{9.4} \left(\frac{L}{gHL} \right)^{5.2} \right)^{0.04}$$

$$D = 0.106 \text{ ft}$$

123

$$h_L = f \frac{L}{D} \frac{V^2}{2g}$$

$$\frac{P_A}{\gamma} + \frac{V_A^2}{2g} + Z_A = \frac{P_B}{\gamma} + \frac{V_B^2}{2g} + Z_B + h_{LAB}$$

$$\frac{P_A - P_B}{\gamma} = h_{LAB}$$

$$a) R_r = D/\epsilon = 0.0525 \text{ m} / 4.6 \times 10^{-5} \text{ m}$$

$$R_r = 1141.3, (L_e/D)_{\text{elbow}} = 30, (L_e/D)_{\text{valve}} = 150$$

$$h_{LAB1} = f_1 \left(\frac{30 \text{ m}}{0.0525 \text{ m}} \right) \frac{V_A^2}{2g}$$

$$h_{LAB2} = h_f + h_{vr} + 3h_e$$

$$= f_2 \left(\frac{L}{D} \right) \frac{V_2^2}{2g} + f_{2T} \left(\frac{L_e}{D} \right) \frac{V_2^2}{2g} + 3f_{2T} \left(\frac{L_e}{D} \right) \frac{V_2^2}{2g}$$

$$= (1142f_2 + 4.56) \frac{V_2^2}{2g}$$

$$h_{LAB1} = h_{LAB2}$$

$$V_1 = 1.55 V_2 \rightarrow V_1 = 3.97 \text{ m/s}$$

$$N_R = \frac{V_2 D_2}{\nu} = 1.3 \times 10^5$$

$$N_R = \frac{V_1 D_1}{\nu} = 1.6 \times 10^5$$

$$\text{From moody diagram} \rightarrow f_1 = f_2 = 0.0215$$

$$V_2 = 2.55 \text{ m/s}, V_1 = 3.98 \text{ m/s}$$

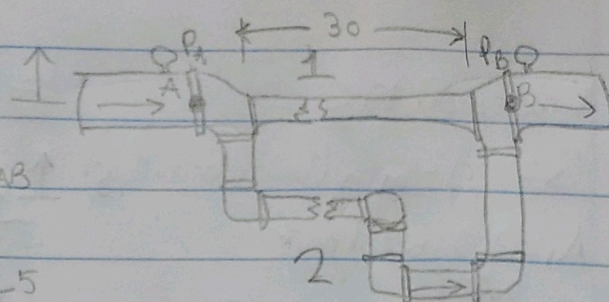
$$f_1 = f_2 = 0.0215$$

$$Q_1 = AV = 518 \text{ l/min}$$

$$Q_2 = 332 \text{ l/min}$$

$$b) \frac{\Delta P}{\gamma} = h_{LAB} \rightarrow \Delta P = \gamma h_{LAB}$$

$$\Delta = 95.06 \text{ kPa}$$



12.5 Water @ 10°C

$Q = 500 \text{ L/min}$ (both branches)

$$A_1 = 0.00679 \text{ m}^2$$

$$V_1 = \frac{0.00833 \text{ m}^3/\text{s}}{0.00679 \text{ m}^2}$$

$$V_1 = 1.22 \text{ m/s}$$

$$N_R = \frac{V_1 D_1}{\nu} = 87276.9$$

$$R_r = D/\epsilon = 1.61 \times 10^5$$

from moody diagram: $f_1 = 0.018$

$$A_2 = 0.00173 \text{ m}^2$$

$$V_2 = Q/A_2 = 4.02 \text{ m/s}$$

$$N_R = \frac{V_2 D_2}{\nu} = 174080$$

$$R_r = D/\epsilon = 3.19 \times 10^5$$

from moody diagram: $f_2 = 0.016$

$$h_{L1} = h_f + h_{vt} + 2h_{le}$$

$$\hookrightarrow = f_1 \left(\frac{L}{D} \right) \frac{V_1^2}{2g} + k \frac{V_1^2}{2g} + 2f_{rt} \left(\frac{L_e}{D} \right) e \frac{V_1^2}{2g}$$

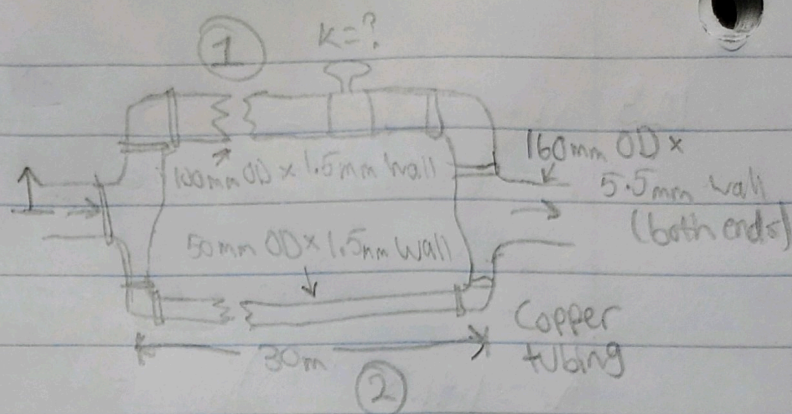
$$\hookrightarrow = (6.56 + k) \frac{V_1^2}{2g}$$

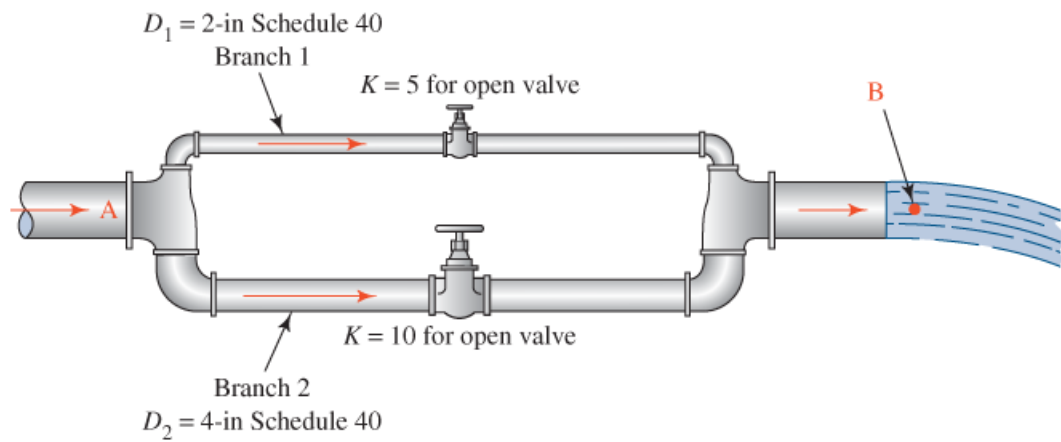
$$h_{L2} = h_f + 2h_{le} \rightarrow f_2 \left(\frac{L}{D} \right) \frac{V_2^2}{2g} + 2f_{rt} \left(\frac{L_e}{D} \right) e \frac{V_2^2}{2g}$$

$$\hookrightarrow = 10.81 \frac{V_2^2}{2g}$$

$$(6.56 + k) \left(\frac{(1.22 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} \right) = 10.81 \left(\frac{(4.02 \text{ m/s})^2}{2(9.81 \text{ m/s}^2)} \right)$$

$$k = 161.85$$





K elbow	0.9	Diameters		Pipe Area	
Kvalve up	5	branch 1	2 in	Branch 1	0.021806 ft ²
Kvalve low	10	branch 1	0.166667 ft	Branch 2	0.087222 ft ²
Gravity		branch 2	4 in		
32.2 ft/s ²		branch 2	0.333333 ft		
		Head loss		Velocity	
		HL upper	46.15 ft	Vupper	20.90616 ft/s
		HL lower	46.15 ft	Vlower	15.8704 ft/s
				Flow Rate	
				Both open	1.840122 ft ³ /s
				Branch 1	0.45587 ft ³ /s
				Branch 2	1.384251 ft ³ /s

$$b \quad A_{upper} = \frac{\pi \cdot 0.166^2}{4}$$

$$A_{upper} = 0.0218 \text{ ft}^2$$

$$A_{lower} = \frac{\pi \cdot 0.333^2}{4}$$

$$A_{lower} = 0.0872 \text{ ft}^2$$

$$h_{upper} = 2 \cdot K_e \frac{V_u^2}{2g} + K_v \frac{V_u^2}{2g}$$

$$h_{upper} = 6.8 \frac{V_u^2}{2g}$$

$$h_{lower} = 2 \cdot K_e \frac{V_L^2}{2g} + K_v \frac{V_L^2}{2g}$$

$$h_{lower} = 11.8 \frac{V_L^2}{2g}$$

$$h_{upper} = h_{lower} = 46.15 \text{ ft}$$

$$V_u^2 = \frac{46.15 \cdot 32.2 \cdot 2}{6.8}$$

$$V_u = 20.906 \text{ ft/s}$$

$$V_L^2 = \frac{46.15 \cdot 32.2 \cdot 2}{11.8}$$

$$V_L = 15.87 \text{ ft/s}$$

$$A. \quad \underline{Q_u + Q_L = 1.84 \text{ ft}^3/\text{s}}$$

$$Q_u = A_u \cdot V_u$$

$$C \quad \underline{Q_u = 0.455 \text{ ft}^3/\text{s}}$$

$$Q_L = A_L \cdot V_L$$

$$B \quad \underline{Q_L = 1.384 \text{ ft}^3/\text{s}}$$