

Colby Watts
Professor Ayala
2/18/24
MET 350 HW 1.2

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$$\begin{aligned} \text{Const } C_V &= 0.718 \text{ kJ/kg}\cdot\text{K} & R &= 0.287 \text{ kJ/kg}\cdot\text{K} \\ \text{Const } C_P &= 1.005 \text{ kJ/kg}\cdot\text{K} & \gamma &= 1.4 \end{aligned}$$

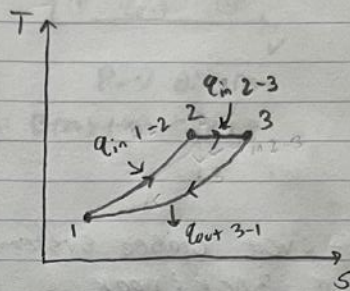
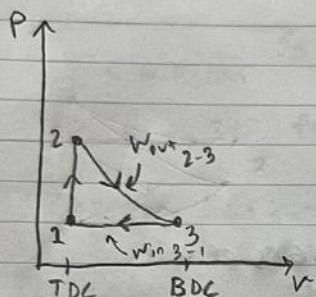
9-13 - air standard cycle closed piston-cylinder system and consists of 3 processes

1-2 $V = \text{const}$ heat add. from 100 kPa and 27°C to 850 kPa

2-3 isothermal expansion until $V_3 = 7V_2$

3-1 $P = \text{const}$ heat rejection to the initial state

$$27^\circ\text{C} = 300 \text{ K}$$



$$\begin{aligned} & \text{1} \xrightarrow{V \text{ const}} \text{2} \xrightarrow{\text{Isothermal}} \text{3} \xrightarrow{P \text{ const}} \text{1} \\ & P_1 = 100 \text{ kPa} \quad \gamma_1 = \gamma_2 \quad \gamma_3 = 7\gamma_2 \\ & T_1 = 300.15 \text{ K} \quad P_2 = 850 \text{ kPa} \quad P_3 = 100 \text{ kPa} \\ & \gamma_1 = \frac{RT_1}{P_1} \quad T_2 = T_3 \end{aligned}$$

$$\frac{P_1}{T_1} = \frac{P_2}{T_2} = \left(\frac{850}{100}\right) \cdot 300 = 2,550 \text{ (K)}$$

$$Q_{1-2} = U_{1-2} + W_{1-2}$$

$$\begin{aligned} Q_{1-2} &= C_V (T_2 - T_1) \\ &= 0.718 \text{ kJ/kg}\cdot\text{K} (2,550 - 300) \\ &= 1,615.5 \text{ (kJ/kg)} \end{aligned}$$

$$\text{B.W.R.} = \frac{W_{3-1}}{W_{2-3}} = \frac{-65.75 \text{ (kJ/kg)}}{1,424.11 \text{ (kJ/kg)}} = \boxed{0.453}$$

$$\begin{aligned} W_{2-3} &= RT_2 \ln \left(\frac{\gamma_3}{\gamma_2} \right) \\ W_{2-3} &= 0.287 \text{ (kJ/kg}\cdot\text{K)} (2,550) (7) \\ &= 1,424.11 \text{ (kJ/kg)} \\ Q_{2-3} &= 1,424.11 \text{ (kJ/kg)} \end{aligned}$$

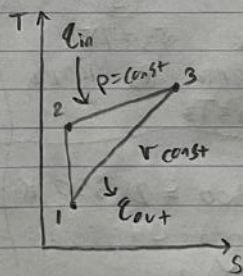
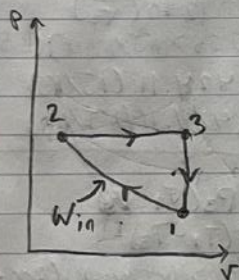
$$\begin{aligned} W_{3-1} &= P_3 (\gamma_1 - \gamma_3) \\ &= P (T_1 - T_3) \\ &= 0.287 \text{ (kJ/kg}\cdot\text{K)} (300 - 2,550) \\ W_{3-1} &= -65.75 \text{ (kJ/kg)} \end{aligned}$$

$$W_{\text{net}} = W_{2-3} - W_{1-3} = 1,424 \text{ (kJ/kg)} - 65.75 \text{ (kJ/kg)} = 1,358.25 \text{ (kJ/kg)}$$

$$Q_g = Q_{1-2} + Q_{2-3} = 1,615.5 \text{ kJ/kg} + 1,424 = 3,039.61 \quad \eta_{\text{th}} = \frac{1,358.25}{3,039.61} = \boxed{25\%}$$

- 9-31c The difference between is how the explosions occur. Gas engines use a mixture of fuel and air and it is compressed to hit spark plugs and ignite. In diesel the process of compression is before fuel is added into the chamber.

- 9-22 Carnot cycle closed system w/ 0.6 kg of air.
 Temp limits 300K & 1100K $K=1.4$
 Min pressure = 20 kPa max pressure = 3000 kPa



$$T_1 = 300 \text{ K} \quad T_2 = 1100 \text{ K} \quad P_2 = P_3 \left(\frac{T_2}{T_1} \right)^{\frac{1}{K}} = (20 \text{ kPa}) \left(\frac{1100 \text{ K}}{300 \text{ K}} \right)^{\frac{1}{1.4}} = 1.888 \text{ kPa}$$

$$P_3 = 20 \text{ kPa} \quad P_1 = 3000 \text{ kPa}$$

$$\Delta s = C_p \ln \left(\frac{T_2}{T_1} \right) - R \ln \left(\frac{P_2}{P_1} \right) = (0.287 \text{ kJ/kg} \cdot \text{K}) \ln \left(\frac{1100}{300} \right) - (0.287 \text{ kJ/kg} \cdot \text{K}) \ln \left(\frac{1.888}{3000} \right) = 0.1329 \text{ kJ/kg} \cdot \text{K}$$

$$Q_{in} = m T_2 \Delta s = (0.6 \text{ kg}) (1100 \text{ K}) (0.1329 \text{ kJ/kg} \cdot \text{K}) = 87.73 \text{ kJ}$$

$$\eta_{th} = 1 - \frac{T_1}{T_2} = 1 - \frac{300}{1100} = 72.7\% \quad W_{net} = \eta_{th} \cdot Q_{in} = (0.727) (87.73) = 63.9 \text{ kJ}$$