

1/28/2025
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HW 1.2 CH9: 13, 18, 22, 31

Q9-13. Air Standard Cycle, variable specific heats is executed in closed system with 4 processes:

1-2 Isentropic Compression 100 kPa and 22°C to 600 kPa

2-3 V=Constant heat to 1500 K

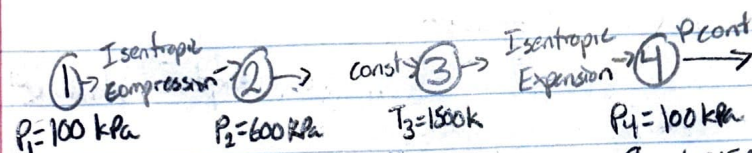
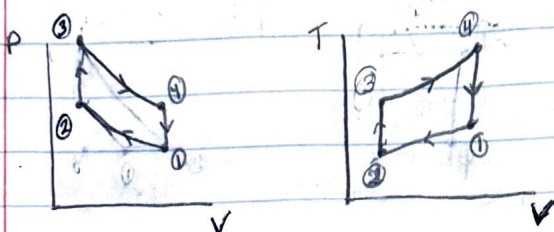
3-4 Isentropic Expansion to 100 kPa

4-1 P=Constant heat rejection

Q's

* Does the isentropic compression lose volume?

* Act more like an Otto cycle



$P_1 = 100 \text{ kPa}$

$P_2 = 600 \text{ kPa}$

$T_3 = 1500 \text{ K}$

$P_4 = 100 \text{ kPa}$

$T_1 = 22^\circ\text{C} = 295.15 \text{ K}$

$T_2 = \frac{P_2}{P_1} T_1$
 $T_2 = \frac{600 \text{ kPa}}{100 \text{ kPa}} \cdot 295.15 \text{ K}$

$T_2 = 1770.9 \text{ K}$

$Q_{\text{out}} = 1500 \text{ K} - 295.15 \text{ K}$
 $Q_{\text{out}} = 1204.85 \text{ K}$

$\eta = \frac{W_{\text{net}}}{Q_{\text{in}}} = 1 - \frac{Q_{\text{out}}}{Q_{\text{in}}}$

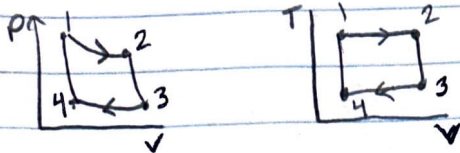
$Q_{\text{in}} - Q_{\text{out}} + W_{\text{in}} - W_{\text{out}} = \Delta U \left[\frac{\text{kJ}}{\text{kg}} \right]$

$W_{\text{in}} = 1204.85 \text{ kJ} \cdot 100 \text{ kPa}$

$\frac{T_4}{T_3} = \left(\frac{P_4}{P_3} \right)^{\frac{\gamma-1}{\gamma}}$

$\frac{T_4}{1500 \text{ K}} = \left(\frac{100 \text{ kPa}}{600 \text{ kPa}} \right)^{\frac{\gamma-1}{\gamma}}$

Q. 18 Air Standard Carnot Cycle is executed in a closed system between temps 350 k and 1200 k. Pressure before and after isothermal compression are 150 kPa and 300 kPa. Net work out is 0.5 kJ.



$$\Delta W_{net} = 0.5 \text{ kJ}$$

① Isothermal \rightarrow Expansion \rightarrow ② Expansion \rightarrow ③ Isothermal compression \rightarrow ④ compression \rightarrow compression \rightarrow compression
 $P_1 = 150 \text{ kPa}$ $T_2 = 1200 \text{ K}$ $T_3 = 350 \text{ K}$ $P_2 = 300 \text{ kPa}$ $T_4 = 350 \text{ K}$ $\gamma_{air} = 1.4$

$$\eta = 1 - \frac{T_L}{T_H} = 1 - \frac{350}{1200} = 1 - 0.2917$$

$$\eta = 0.7083$$

$$0.7083 = \frac{W}{Q_{in}}$$

$$\frac{T_3}{T_2} = \left(\frac{P_3}{P_2} \right)^{\frac{\gamma-1}{\gamma}}$$

$$\frac{350}{1200} = \left(\frac{P_3}{300} \right)^{\frac{1.4-1}{1.4}}$$

$$0.2917 = \left(\frac{P_3}{300} \right)^{0.286}$$

$$0.2917^{1/0.286} = \frac{P_3}{300}$$

$$\frac{0.2917^{1/0.286}}{300} = \frac{P_3}{300}$$

$$\frac{P_3}{300} = 10.67$$

Q 22 An Ideal gas is contained in a piston cylinder device and undergoes power cycle.

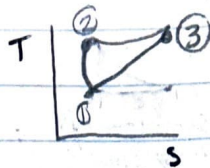
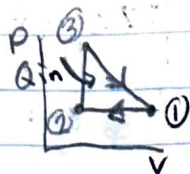
① Isentropic compression → ② Constant Pressure / heat add → ③ → Constant Volume / heat rejection

$T_1 = 20^\circ\text{C}$ * need T_2

$r = 5$

$$C_v = 0.7 \text{ kJ/kg}\cdot\text{K}$$

$$R = 0.3 \text{ kJ/kg}\cdot\text{K}$$



$$T_2 = T_1 r^{\gamma}$$

$$W_{1-2} = C_v (T_2 - T_1)$$

$$Q_{2-3} = C_p (T_3 - T_2)$$

$$r = 5 \Rightarrow T_2 = 1.0 \text{ kJ/kg}$$

$$Q_{3-1} = 0.7 (T_3 - T_2)$$

$$W_{\text{net}} = Q_2 - Q_1$$

$$\eta = \frac{W_{\text{net}}}{Q_{\text{in}}}$$

$$W_{\text{net}} =$$

Q 31. Ideal Otto cycle has compression ratio of 10.5, takes air at 90 kPa and 40°C, 2500 rpm. Find Thermal Efficiency to produce 90 kW of Power.

①

②

$$P_1 = 90 \text{ kPa}$$

$$T_1 = 40^\circ\text{C} = 313.5 \text{ K}$$

$$\eta = 1 - \frac{1}{r^{\gamma-1}}$$

$$\eta = 1 - \frac{1}{10.5^{1.4-1}}$$

$$\eta = 1 - 0.60$$

$$\eta = 0.39$$