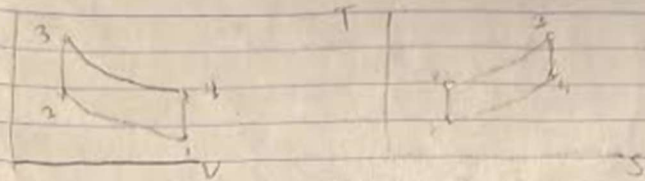


Ch 9 HW

33



- ① $P_1 = 0.287 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$
 $P_1 = 95 \text{ kPa}$
 $T_1 = 25^\circ\text{C} \rightarrow 300 \text{ K}$
 $q = 750 \frac{\text{kJ}}{\text{kg}}$
- ② $P_2 = 1705.19 \text{ kPa}$
 $T_2 = 673.1 \text{ K}$
- ③ $P_3 = 3898.81 \text{ kPa}$
 $T_3 = 1539 \text{ K}$
- ④ $T_4 = 729.5 \text{ K}$

at 300K
 $u_1 = 214.07$
 $v_{r1} = 621.2$
 $v_{r2} = \frac{v_2}{v_1} \cdot v_{r1} \rightarrow \frac{621.2}{8} = 77.65$

at 77.65
 $T_2 = 673.1 \text{ K}$
 $u_2 = 491.2 \frac{\text{kJ}}{\text{kg}}$
 $P_2 = \frac{v_1}{v_2} \cdot \frac{T_2}{T_1} \cdot P_1 = \frac{621.2}{77.65} \cdot \frac{673.1}{300} \cdot 95 = 1705.19 \text{ kPa}$

$u_3 = q_{23} + u_2 = 750 + 491.2 = 1241.2 \frac{\text{kJ}}{\text{kg}}$
 at 1241.2 $\frac{\text{kJ}}{\text{kg}}$
 $T_3 = 1539 \text{ K}$

$P_3 = \frac{T_3}{T_2} \cdot P_2 = \frac{1539}{673.1} \cdot 1705.19 = 3898.81 \text{ kPa}$

$$V_{r1} = \frac{V_1}{V_2} \cdot V_2 = 8 \cdot 6.475 = 51.80$$

$$q_1 = 52.70$$

$$T_4 = 729.5 \text{ K}$$

$$u_4 = 571.69 \frac{\text{kJ}}{\text{kg}}$$

$$q_{out} = u_4 - u_1 = 571.69 - 374.07 = 197.62$$

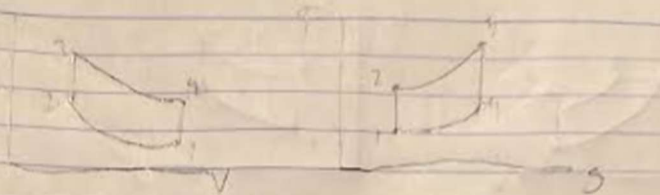
$$w_{net} = q_{in} - q_{out} = 750 - 357.62 = 392.4 \frac{\text{kJ}}{\text{kg}}$$

$$\text{thermal efficiency} = \frac{w_{net}}{q_{in}} = \frac{392.4}{750} = 0.523 = 52.3\%$$

$$V_1 = R \frac{T_1}{P_1} = 0.287 \cdot \frac{300}{1} = 0.861 \frac{\text{m}^3}{\text{kg}}$$

$$V_2 = \frac{V_1}{r} = \frac{0.861}{8} = 0.1076 \frac{\text{m}^3}{\text{kg}}$$

$$MEP = \frac{w_{net}}{V_1 - V_2} = \frac{w_{net}}{V_1 \cdot (1 - \frac{1}{r})} = \frac{392.4}{0.861 \cdot (1 - \frac{1}{8})} = 495.1 \text{ kPa}$$



$$\begin{array}{cccc}
 \textcircled{1} & & \textcircled{2} & & \textcircled{3} & & \textcircled{4} \\
 T_1 = 104\text{K} \rightarrow 40^\circ\text{C} \rightarrow 313\text{K} & & T_2 = 792.47\text{K} & & T_3 = 2000\text{F} \rightarrow 1316\text{C} \rightarrow 1589\text{K} & & T_4 = 627.6\text{K} \\
 P_1 = 14\text{psia} \rightarrow 96.53\text{kPa} & & & & & &
 \end{array}$$

$$r = \frac{V_1}{V_2} = \frac{V_1}{0.098V_1} = 10.20$$

$$\frac{T_2}{T_1} = r^{\gamma-1} \rightarrow T_2 = 313 \cdot 10.20^{1.4-1} = 792.47\text{K}$$

$$\frac{T_4}{T_3} = \left(\frac{V_3}{V_4}\right)^{\gamma-1} \rightarrow \left(\frac{1}{r}\right)^{\gamma-1} \rightarrow T_4 = 1589 \cdot \left(\frac{1}{10.20}\right)^{1.4-1} = 627.6\text{K}$$

$$\begin{aligned}
 \dot{Q}_{\text{net}} &= C_v(T_3 - T_4) - C_v(T_2 - T_1) = 0.718(1589 - 627.6) - 0.718(792.47 - 313) \\
 \dot{Q}_{\text{net}} &= 345.81\text{kJ/kg}
 \end{aligned}$$

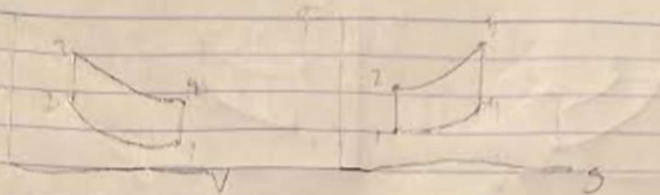
$$14\text{psia} = 96.53\text{kPa}$$

$$m = n p v \rightarrow n = \frac{p}{R \cdot T} \cdot \frac{\pi}{4} d^2 \cdot L = 6 \cdot \frac{96.53}{0.727 \cdot 313} \cdot \frac{\pi}{4} \cdot (0.085)^2 \cdot 0.095$$

$$m = 0.004\text{kg}$$

$$\dot{Q}_{\text{net/cycle}} = 0.004 \cdot 345.81 = 1.383\text{kJ/cycle}$$

$$\dot{Q}_{\text{net}} = \frac{\dot{Q}_{\text{net/cycle}} \cdot N}{N_{\text{rev}}} = \frac{1.383 \cdot \frac{2500}{60}}{2} = 28.81\text{kW}$$



$$\begin{array}{cccc}
 \textcircled{1} & & \textcircled{2} & & \textcircled{3} & & \textcircled{4} \\
 T_1 = 104\text{K} \rightarrow 40^\circ\text{C} \rightarrow 313\text{K} & & T_2 = 792.47\text{K} & & T_3 = 2000\text{F} \rightarrow 1316\text{C} \rightarrow 1589\text{K} & & T_4 = 627.6\text{K} \\
 P_1 = 14\text{psia} \rightarrow 96.53\text{kPa} & & & & & &
 \end{array}$$

$$\gamma = \frac{V_1}{V_2} = \frac{V_1}{0.098V_1} = 10.20$$

$$\frac{T_2}{T_1} = \gamma^{\gamma-1} \rightarrow T_2 = 313 \cdot 10.20^{1.4-1} = 792.47\text{K}$$

$$\frac{T_4}{T_3} = \left(\frac{V_3}{V_4}\right)^{\gamma-1} \rightarrow \left(\frac{1}{10.20}\right)^{\gamma-1} \rightarrow T_4 = 1589 \cdot \left(\frac{1}{10.20}\right)^{1.4-1} = 627.6\text{K}$$

$$\begin{aligned}
 \dot{Q}_{\text{net}} &= C_v(T_3 - T_4) - C_v(T_2 - T_1) = 0.718(1589 - 627.6) - 0.718(792.47 - 313) \\
 \dot{Q}_{\text{net}} &= 345.81\text{kJ/kg}
 \end{aligned}$$

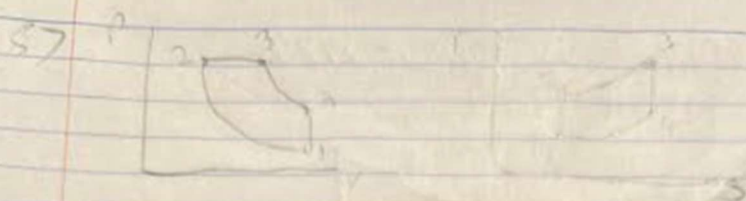
$$14\text{psia} = 96.53\text{kPa}$$

$$m = n p v \rightarrow n = \frac{p}{R \cdot T} \cdot \frac{\pi}{4} d^2 \cdot L = 6 \cdot \frac{96.53}{0.727 \cdot 313} \cdot \frac{\pi}{4} \cdot (0.085)^2 \cdot 0.095$$

$$m = 0.004\text{kg}$$

$$\dot{Q}_{\text{net/cycle}} = 0.004 \cdot 345.81 = 1.383\text{kJ/cycle}$$

$$\dot{Q}_{\text{net}} = \frac{\dot{Q}_{\text{net/cycle}} \cdot N}{N_{\text{rev}}} = \frac{1.383 \cdot \frac{2500}{60}}{2} = 28.81\text{kW}$$



①	②	③	④
$T_1 = 200 \rightarrow 343 \text{ K}$	$T_2 = 1181 \text{ K}$	$T_3 = 2126 \text{ K}$	$T_4 = 781 \text{ K}$
$P_1 = 97 \text{ kPa}$			

$$T_2 = T_1 \left(\frac{V_2}{V_1} \right)^{\gamma-1} = 343 \cdot (22)^{1.4-1} = 1181 \text{ K}$$

$$T_3 = \left(\frac{P_3}{P_2} \right) \cdot T_2 = 1.8 \cdot 1181 = 2126 \text{ K}$$

$$T_4 = T_3 \left(\frac{P_4}{P_3} \right)^{\gamma-1} = 2125.8 \left(\frac{1.8}{22} \right)^{1.4-1} = 781 \text{ K}$$

$$m = \frac{P_1 V_1}{R T_1} = \frac{97 \cdot 0.0024}{287 \cdot 343} = 0.002365 \text{ kg}$$

$$q_{in} = m c_p (T_3 - T_2) = 0.002365 \cdot 1.005 (2126 - 1181)$$

$$q_{in} = 2.246 \text{ kJ}$$

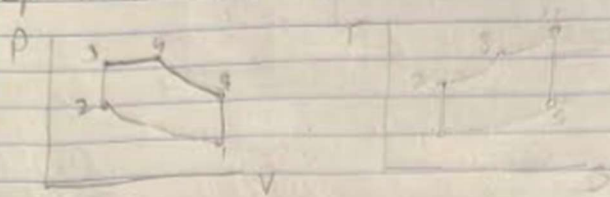
$$q_{out} = m c_v (T_4 - T_1) = 0.002365 \cdot 0.718 (781 - 343)$$

$$q_{out} = 0.7438 \text{ kJ}$$

$$W_{net} = q_{in} - q_{out} = 2.246 - 0.7438 = 1.5023$$

$$\eta_{net} = \frac{W_{net}}{q_{in}} = \left(\frac{1.5023}{2.246} \right) \cdot 100 = 87.6 \%$$

59 $14.2 \text{ psia} = 98 \text{ kPa}$ $75^\circ\text{F} = 24^\circ\text{C} = 297^\circ\text{K}$
 $C_p = 1.005$ $C_v = 0.718$



①	②	③	④	⑤
$P_1 = 98 \text{ kPa}$	$P_2 = 98 \text{ kPa}$	$T_3 = 965.12 \text{ K}$	$P_4 = 4776.904 \text{ kPa}$	$T_5 = 523.69 \text{ K}$
$T_1 = 297 \text{ K}$	$T_2 = 877.39 \text{ K}$	$P_1 = 98 \text{ kPa}$	$P_2 = 1351.16 \text{ kPa}$	

$$v_1 = \frac{RT_1}{P_1} = \frac{0.287 \cdot 297}{98} = 0.8697 \text{ m}^3/\text{kg}$$

$$v_2 = \frac{v_1}{r} = \frac{0.8697}{15} = 0.05798 \text{ m}^3/\text{kg}$$

$$P_2 = P_1 (r)^{\gamma} = 98 (15)^{1.4} = 4342.59 \text{ kPa}$$

$$T_2 = T_1 (r)^{\gamma-1} = 297 (15)^{1.4-1} = 877.39 \text{ K}$$

$$T_3 = T_2 \left(\frac{P_3}{P_2}\right) = 877.39 \cdot 1.1 = 965.12 \text{ K}$$

$$\frac{P_3}{P_2} = 1.1 \quad P_3 = P_2 \quad P_4 = 1.1 \cdot 4342.59 = 4776.904 \text{ kPa}$$

$$v_4 = r \cdot v_3 = 8 \cdot v_3 = 1.4 \cdot 0.05798 = 0.081172 \text{ m}^3/\text{kg}$$

$$T_4 = T_3 \left(\frac{P_4}{P_3}\right) = 965.12 \left(\frac{0.081172}{0.05798}\right) = 1351.16 \text{ K}$$

$$T_5 = T_4 \left(\frac{P_5}{P_4}\right) = 1351.16 \left(\frac{0.081172}{0.8697}\right) = 523.69 \text{ K}$$

$$q_{in} = C_v(T_3 - T_2) + C_p(T_4 - T_3) = 0.718(965.12 - 877.39) + 1.005(1351.16 - 965.12) = 450.96 \text{ kJ/kg}$$

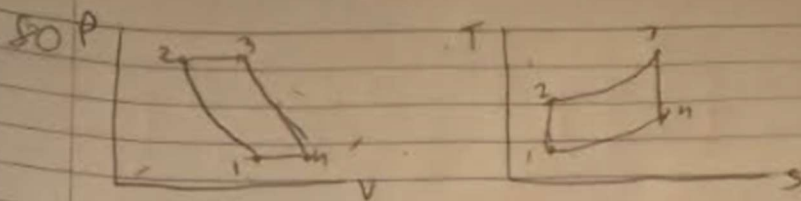
$$q_{in} = 450.96 \text{ kJ/kg}$$

$$q_{out} = C_v(T_5 - T_1) = 0.718(523.69 - 297) = 162.76 \text{ kJ/kg}$$

$$w_{net} = q_{in} - q_{out} = 450.96 - 162.76 = 288.2 \text{ kJ/kg}$$

$$\eta_{th} = \frac{w_{net}}{q_{in}} = \frac{288.2}{450.96} = 0.639 = 63.9\%$$

Went to class for help on this one



$T_1 = 520\text{K}$ ① ② ③ ④
 $T_2 = 996.48\text{K}$ $T_3 = 2000\text{K}$

$P_{r2} = 10 \cdot 1.247 = 12.47$
 $T = 980, h = 236.02, P_r = 11.43$
 $T = 1000, h = 240.98, P_r = 12.30$

$\frac{12.3 - 11.43}{12.3 - 12.47} = \frac{1000 - 980}{1000 - T_2}$ $T_2 = 996.48\text{K}$
 $h_2 = 240.107$

$P_{r4} = \frac{P_4}{P_2} = \frac{17.4}{10} = 1.74$
 $P_r = 16.28, h = 260.97$ $18.60 - 16.28 = 271.03 - 260.97$
 $P_r = 18.60, h = 271.03$ $18.60 - 17.4 = 271.03 - 264.603$
 $h_4 = 265.826$

$W_t = 240.107 - 24.27 = 115.837$

$\eta_{\text{th}} = \frac{115.837}{238.584} = 0.4849$

$q_{\text{in}} = 509.71 - 240.107 = 264.603$

$\eta = \frac{238.584 - 115.837}{264.603} = 46.57\%$